AM - Between Copenhagen, PARIS & Cracow: Towards Statistical Model of the New Generation

JD

IPHC - Department of Subatomic Research, $CNRS/IN_2P_3$ and University of Strasbourg, F-67037 Strasbourg, FRANCE

Monday 14th September, 2015

• Adam, friend and collaborator, was born

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 $\mathcal{N} \approx (2.5 \pm 0.02) \times 10^2$ articles

which to a leading order are distributed as follows:

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which to a leading order are distributed as follows:

- Giant Dipole Resonances: (56 ± 2) counts in the peak;
- Jacobi, Poincaré and other shape transitions: (35 ± 2) ;
- Isomers and isomerism: (30 ± 1) ;
- Super-deformation and/or hyper-deformation: (20 ± 1)



At this point I would like to use the opportunity and most cordially wish all the best to the birth-day girl!

Sto lat Angela!! Sto lat [in Polish]: Hundred years

JD, Strasbourg University, CNRS France

As a good friend and collaborator of the birthday-boy, my Good Friend and Collaborator...



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*)O Nieba!

Chrońcie mnie przez przyjaciółmi !! Przed wrogami obronię się sam !!!

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Here We Arrive at the Symbol of an Efficient, Hard Work



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About Presenting the Efficient, Hard Work

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• Therefore we will just improvise during the rest of this story...

Before becoming a professor, our birthday boy, as often happens, had to obtain a University diploma, and even before, oh heck! – he had to go to school!

Well - well, let us see more in detail...

All of us of *that generation*, who happened to live in Poland, spent over 50% of their life-time, in the environment called: Pe-Er-El.

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Many who have never seen Pe-Er-El may not know about this environment. We will recall some of its characteristics using a few (over-)simplified illustrations.

Part I

The Very Beginning: Times, Facts, Snap-shots from the History...

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• Polska Rzeczpospolita Ludowa (PRL) [Read: Pe-Er-El] was also known under the names:

> Volksrepublik Polen Republique Populaire Polonaise Polish People's Republik

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On the left:

The first page of the text of the constitution of the Pe-Er-El, typed in Russian, with the hand-written corrections by J. Stalin

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From WIKIPEDIA:

During the so-called socialist times in Poland, people used humour to cope with all the crazy party lies and the empty shelves in shops.





This gave rise to a huge collection of jokes about the economic crisis, the party, the Soviets and the system. Of course people had to be careful who they shared the jokes with. There was a big official competition for the best anti-Soviet joke: The prize was 5 years in Siberia.

• Communism vs. Capitalism

Example 1

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• Communism vs. Capitalism

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Example 2

- Capitalism is a system in which man exploits man.
- In communism exactly the opposite happens.
• Freedom vs. Prison

Example 1: The 5 commandments for a Polish citizen

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- The third prisoner: "I didn't do anything and they sentenced me to 5 years!"

"Don't bs us. For nothing you get two years !!"

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Time to Go to School or, in other words, The Hard Work at School

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We Look for Adam



• Where is the birthday boy? Who will tell us?

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Very good ... Very good ...

Let us see ...

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• Please give the position: Left - 1, 2, or 3? Right: 1, 2, 3 or 4?

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LEFT. 1: Adam, 2: Witek, 3: Marek

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- Please give the position: Left 1, 2, or 3? Right: 1, 2, 3 or 4?
- LEFT. 1: Adam, 2: Witek, 3: Marek
- RIGHT. 1: Paul (McCartney), 2: Ringo (Starr), 3: George (Harrison), 4: John (Lennon)

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As one can see

Adam was doing very well at school.

No wonder that $\rightarrow \rightarrow \rightarrow$

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He Received the Professor Nomination



• from the Polish President, Lech Kaczyński, in 2006.

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But before the Professor Nomination...

... he had to publish some papers (better: articles)...

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JD, Strasbourg University, CNRS France E

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... he had to publish some papers (better: articles)... You mean to say that you know? ... all of them?

Do not worry! You will be kindly invited to listen anyway!!

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Part II

Nuclear Isomers: Strong Signals from Nucleonic Configurations

JD, Strasbourg University, CNRS France Betw

Z. Phys. A - Atoms and Nuclei 314, 89-95 (1983)



Isomeric Transitions in ²⁰³Bi and ²⁰⁵Bi

H. Hübel, M. Guttormsen*, K.P. Blume, J. Recht, A. von Grumbkow, K. Hardt, P. Schüler, and Y.K. Agarwal** Institut für Strahlen- und Kernphysik, Universität Bonn, Federal Republic of Germany

A. Maj*** Hahn-Meitner-Institut für Kernforschung, Berlin, Germany

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The First Publications: from Berlin



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• Notice isomers here-and-there, of course, but also another beauty:

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• Notice isomers here-and-there, of course, but also another beauty:

• Nearly 'hidden' $\Delta I = 1\,\hbar$ doublets

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Nuclear Physics A436 (1985) 311-337 © North-Holland Publishing Company

DECAY OF THE GROUND STATE AND THE $\frac{29}{2}$ ⁺ ISOMER IN ²¹⁷Ac AND *g*-FACTOR MEASUREMENTS FROM PERTURBED α -PARTICLE ANGULAR DISTRIBUTIONS

D. J. DECMAN[†], H. GRAWE, H. KLUGE, K. H. MAIER, A. MAJ^{††} and N. ROY*

Hahn-Meitner-Institut für Kernforschung, Berlin GmbH, Bereich Kern- und Strahlenphysik, 1000 Berlin 39, West Germany

and

Y. K. AGARWAL**, K. P. BLUME, M. GUTTORMSEN***, H. HÜBEL and J. RECHT Institut für Strahlen- und Kernphysik, Universität Bonn, D-5300 Bonn, West Germany

Received 5 September 1984

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• This illustration summarises the systematic appearance of the doublets:

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• This illustration summarises the systematic appearance of the doublets: interpreted as the result of the coupling $I \otimes g_{9/2}$: I=0, 2, 4, ...

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Isomers and the Nuclear Mean-Field Theory

• The preceding illustrations show in a convincing manner the validity of the "core-and-particle(s)" quantum structures, here a single neutron

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• Some years earlier, Aage Bohr and Ben Mottelson suggested a generalisation: A few nucleons + core represented by the nuclear mean-field



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 \bullet Some years earlier, Aage Bohr and Ben Mottelson suggested a generalisation: A few nucleons + core represented by the nuclear mean-field



• The approach was nick-named the "Tilted Fermi-Surface Method". Following the encouragement form Aage it has been developed further within Copenhagen-Warsaw collaboration \rightarrow 'Universal Woods-Saxon'

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• One uses a mean-field approach and the fact that in case of an axial symmetry, say \mathcal{O}_{z} -axis we have

$$[\hat{H}, \hat{\jmath}_z] = 0$$

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• Consequently

$$\hat{H}\,\varphi_{\nu,m_{\nu}}=e_{\nu,m_{\nu}}\,\varphi_{\nu,m_{\nu}}$$

$$\hat{\jmath}_z \, \varphi_{\nu,m_\nu} = m_\nu \, \varphi_{\nu,m_\nu}$$

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Projections of Angular Momenta Are Conserved in the Presence of Axial Symmetry



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For the particle hole excited states we obtain at the same time the model energy and model spin:

$$E^* = \sum_p e_{p,m_p} - \sum_h e_{h,m_h}$$
 and $M^* \approx Spin = \sum_p m_p - \sum_h m_h$

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How Powerful Service the Mean-Field Offers



• Theoretical prediction of the isomers at $I^{\pi} = \frac{21}{2}^+$ [4.8 ns]; at $I^{\pi} = \frac{27}{2}^-$ [27 ns] and at $I^{\pi} = \frac{49}{2}^+$ [530 ns]

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How Powerful Service... Inverted Parabolas



• Since the single-j orbitals have inverted-parabolic energy dependence $[e_j \propto -j(j+1)]$, the excitations involving such an orbital lead to inverted parabola schemes [abundant in nuclei]

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Inverted Parabolas Revisited

PRL 99, 132501 (2007)

PHYSICAL REVIEW LETTERS

week ending 28 SEPTEMBER 2007

Observation of Isomeric Decays in the r-Process Waiting-Point Nucleus ¹³⁰Cd₈₂

A. Jungclaus,¹ L. Cáceres,^{1,2} M. Górska,² M. Pfützner,³ S. Pietri,⁴ E. Werner-Malento,³ H. Grawe,² K. Langanke,²
 G. Martínez-Pinedo,² F. Nowacki,⁵ A. Poves,¹ J. J. Cuenca-García,² D. Rudolph,⁶ Z. Podolyak,⁴ P. H. Regan,⁴ P. Detistov,⁷
 S. Lalkovski,^{8,7} V. Modamio,¹ J. Walker,¹ P. Bednarczyk,² P. Doormenbal,⁷ H. Geissel,² J. Gerl,² J. Grebosz,^{2,9}
 I. Kojouharov,² N. Kurz,² W. Prokopowicz,² H. Schaffner,² H. J. Wollersheim,¹⁰ K. Andgren,¹⁰ J. Benlliure,¹¹ G. Benzoni,¹²
 A. M. Bruce,⁸ E. Casarejos,¹¹ B. Cederwall,¹⁰ F. C. L. Crespi,¹² B. Hadinia,¹⁰ M. Hellström,⁶ R. Hoischen,^{6,2} G. Ilie,^{13,14}
 J. Jolie,¹³ A. Khaplanov,¹⁰ M. Kmiecik,⁹ R. Kumar,¹⁵ A. Maj,⁹ S. Mandal,¹⁶ F. Montes,² S. Myalski,⁹ G. S. Simpson,¹⁷
 S. J. Steer,⁴ S. Tashenov,² and O. Wieland¹²

• Example of the research by a large collaboration [birthday-boy included] which can be seen as a textbook example (see below)

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Inverted Parabolas Revisited



FIG. 4. Proposed level scheme of ¹³⁰Cd compared to the known level schemes of ⁷⁶Ni [29] and ⁹⁸Cd [13]. The solid arrows indicate the observed A^{-1} scaling, whereas the dashed arrows correspond to an $A^{-1/3}$ scaling of the $2^+ - 8^+$ energy spread.

• To notice the decreasing transition energies with increasing spin giving rise to the characteristic inverted parabola patterns [here of the j^2 (alternatively j^{-2}) configurations]

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Part III

Large Nuclear Deformations as a Test-Laboratory for the Giant-Dipole Resonances

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Extreme Deformations: Super-, and Hyper-defs.



Nuclear Physics A687 (2001) 237c-244c



www.elsevier.nl/locate/npe

The Giant Dipole Resonance in superdeformed nuclei and the feeding of superdeformed bands

A. Bracco, F. Camera, S. Leoni, B. Million, ^aand A. Maj, M. Kmiecik ^b

^aDipartimento di Fisica, Universitá degli Studi di Milano and Istituto Nazionale di Fisica Nucleare, Sezione di Milano, via Celoria 16, 20133 Milano, Italy

^b Niewodniczanski Institute of Nuclear Physics, 31-342 Krakow, Poland.

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Extreme Deformations: Super-, and Hyper-defs.



Nuclear Physics A599 (1996) 123c-128c



Collective Motion in Hot Superheavy Nuclei

T. S. Tveter^{a,*}, J. J. Gaardhøje^a, A. Maj^{a,b}, T. Ramsøy^{a,†}, A. Atac^{a,‡}, J. Bacelar^e, A. Bracco^d, A. Buda^c, F. Camera^d, B. Herskind^a, W. Korten^{a,§}, W. Królas^b, A. Menthe^e, B. Million^d, H. Nifenecker^e, M. Pignanelli^d, J. A. Pinston^e, H. v. d. Ploeg^e, F. Schussler^e and G. Sletten^a.

^aNiels Bohr Institute, Tandem Accelerator Laboratory, Risø, DK-4000 Roskilde, Denmark

^bNiewodniczanski Institute of Nuclear Physics, Radzikowskiego 152, PL-31-342 Krakow, Poland

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Whereas Adam Is Travelling: Berlin \leftrightarrow Bonn

PHYSICAL REVIEW C

VOLUME 31, NUMBER 1

JANUARY 1985

Shape evolution in the transitional gadolinium, dysprosium, erbium, and ytterbium nuclei

J. Dudek Centre de Recherches Nucléaires, F-67037 Strasbourg Cedex, France

W. Nazarewicz* Department of Mathematical Physics, Lund Institute of Technology S-22007 Lund, Sweden (Received 25 June 1984)

Shape evolution in $I \ge 30$ h high-spin states of $^{144-150}$ Gd, $^{150-156}$ Dy, $^{152-158}$ Er and $^{154-160}$ Yb is predicted theoretically within the cranking approximation using the generalised Strutinsky method. A comparison with available experimental data is provided.

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Whereas Adam Is Travelling: Berlin \leftrightarrow Bonn

• One of four original figures predicting the existence of an island of super-deformed Gadolinium, Dysprosium, Erbium as well as Ytterbium nuclei – in competition with normal-deformed ones.



• Predicted competition between the super-deformed, together with normal-deformed (in particular triaxial) and non-collective states, the latter marked with circles.

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Whereas Adam Is Travelling: Berlin \leftrightarrow Cracow

VOLUME 57, No. 7 PHYSICAL REVIEW LETTERS AUGUST 1986 Observation of a Discrete-Line Superdeformed Band up $60\hbar$ in 152 Dy

P. J. Twin, B. M. Nyakó, A. H. Nelson, J. Simpson, M. A. Bentley, H. W. Cranmer-Gordon, P. D. Forsyth, D. Howe, A. R. Mokhtar, J. D. Morrison, J. F. Sharpey-Schafer, and G. Sletten

A rotational band of nineteen transitions with a moment of inertia Jband(2) of $84h^2$ MeV⁻¹ has been observed in ¹⁵²Dy. The band feeds into the oblate yrast states between 19⁻ and 25⁻ and it is proposed that the lowest member of the band has a spin of 22⁺ and thus the band extends up to 60ħ. It is identified as the yrast superdeformed band and its intensity accounts for the whole of the ridge structure seen previously in continuum E_{γ} - E_{γ} correlations.

The first SD Band is in our hands. It is 1986.

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Whereas Adam Is Travelling: Berlin \leftrightarrow Cracow

VOLUME 57, No. 7 PHYSICAL REVIEW LETTERS SEPTEMBER 1987

Abundance and systematics of nuclear superdeformed states; relation to the pseudospin and pseudo-SU(3) symmetries

J. Dudek, W. Nazarewicz, Z. Szymański and G. A. Leander



JD, Strasbourg University, CNRS France

Read the Figure - and Write in Words What It Says





Theoretical Predictions for SD's

- 1. Existence Z=28, 30, 32
- 2. Absence Z=34, 36
- 3. Existence Z=38, 40, 42, 44, 46
- 4. Absence Z=48, 50, 52, 54, 56
- 5. Existence Z=58, 60, 62, 64, 66
 6. Absence Z=68, 70
- 7. Existence Z=72
- 8. Absence Z=74, 76, 78
- 9. Existence Z=80, 82, ... Actinide

• This diagram is published at the time when only one SD band is known experimentally, using the no-fit 'Universal Woods-Saxon'

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Comparison: Theory-Experiment, Data of 2008

Experimental Situation

Z=30, Zn. N=30, 32, 32, 34 absent, 38 (1) Z=32, 34, 36, absent Z=44, Cd , absent Z=48, 50, 52, 54, 56, absent Z-62, Sm, N-74, 76, 78 absent, 80 Z=70, Yb, absent Z=74, 76, 78, absent

Theoretical Predictions

- 1. Existence Z=28, 30, 32
- 2. Absence Z=34, 36
- 3. Existence Z=38, 40, 42, 44, 46
- 4. Absence Z=48, 50, 52, 54, 56
- 5. Existence Z=58, 60, 62, 64, 66
- 6. Absence Z=68, 70
- 7. Existence Z=72
- 8. Absence Z=74, 76, 78
- 9. Existence Z=80, 82, ...

10. Actinide

• This comparison illustrates the 'predictive power' over the stretch of about 20 years – ahead of time: Prediction is prediction

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Level Degeneracies and Underlying Symmetries

- The key factor in obtaining the large gaps are degeneracies
- The above scheme of shell structures has been fully confirmed by the super-deformations studies 1985 - to date





 \bullet In the jargon of theorists this mechanism is associated with the so-called SU(3) [pseudo-SU(3)] symmetries of nuclear mean-field

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Prediction of the Nuclear Hyperdeformation

• Some years later, using similar techniques, the prediction of the existence of the super- and hyper-deformation mechanisms has been formulated.

• This nostalgic/historical diagram (right) was made in Strasbourg, France, and printed in Oak-Ridge, USA.

• The figure was the cover illustration of the Document: Scientific Motivation for the US-American Germanium detector Gammasphere.



Between Copenhagen, PARIS and Cracow

Extreme Deformations: Super-, and Hyper-defs.

Vol. 36 (2005)

ACTA PHYSICA POLONICA B

No 4

SEARCH FOR HYPERDEFORMATION IN LIGHT Xe NUCLEI*

B.M. NYAKÓ^a, F. PAPP^{a†}, J. GÁL^a, J. MOLNÁR^a, J. TIMÁR^a, A. ALGORA^a
ZS. DOMBRÁDI^a, G. KALINKA^a, L. ZOLNAI^b, K. JUHÁSZ^b, A.K. SINGH^c, H. HÜBEL^c
A. AL-KHATLÉ^a, P. BRINGEL^c, A. BÖRGER^c, A. NEUSSER^c, G. SCHÖNWASSER^c
B. HERSKIND^d, G.B. HAGEMANN^d, C.R. HANSEN^d, G. SLETTEN^d, J.N. SCHEURER^e
F. HANNACH^c, M. KMIECIK^c, A. MAJ^f, J. STYCZEÑ^f, K. ZUBER^f, K. HAUSCHILD^g
A. KORICH^f, A. LOPEZ-MARTENS^g, J. ROCCAZ^g, S. SIEM^g, P. BEDNARCZYK^h
TH. BYRSKI^h, D. CURIEN^h, O. DORVAUX^h, G. DUCHÉNE^h, B. GALL^h
F. KHALFALLAH^h, I. PIQUERAS^h, J. ROBIN^h, S.B. PATEL^f, A.O. EVANS^f
G. RAINOVSKI^f, A. AHOLDI^k, G. BENZONI^k, A. BRACCO^k, F. CAMERA^k
B. MILLION^k, P. MASON^k, A. PALEN^k, R. SACCH^k, O. WIELAND^k, G. LA RANA¹
R. MORO^f, C.M. PETRACHE^m, D. PETRACHE^m, G. DE ANGELB^a, P. FALLO^o
I.-Y. LEe^o, J.C. LISLE^p, B. CEDERWALL^a, K. LAGERGREN^a, R.M. LIEDER^r
E. PODSVIROVA⁷, W. GAST^r, H. JÄGER^r, N. REDON^s AND. A. GÖRCEN^t

JD, Strasbourg University, CNRS France

Extreme Deformations: "Super- and Hyper-defs."

Vol. 34 (2003)

ACTA PHYSICA POLONICA B

No 4

HUNTING GROUNDS FOR JACOBI TRANSITIONS AND HYPERDEFORMATIONS*

B. HERSKIND^a, G. BENZONI^b, J.N. WILSON^a, T. DØSSING^a
G.B. HAGEMANN^a, G. SLETTEN^a, C. RØNN HANSEN^a, D.R. JENSEN^a
A. BRACCO^b, F. CAMERA^b, S. LEONI^b, P. MASON^b, O. WIELAND^b
A. MAJ^c, M. BREKIESZ^c, M. KMIECIK^e, H. HÜBEL^d, P. BRINGEL^d
A. NEUSSER^d, A.K. SINGH^d, R.M. DIAMOND^e, R.M. CLARK^e
M. CROMAZ^e, P. FALLON^e, A. GÖRGEN^e, I.Y. LEE^e
A.O. MACCHIAVELLI^e, D. WARD^e, F. HANNACHI^f, A. KORICHI^f
A. LOPEZ-MARTENS^f, T. BYRSKI^g, D. CURIEN^g, P. BEDNARCZYK^{c,g}
J. DUDEK^g, H. AMRO^h, W.C. MA^h, J. LISLEⁱ, S. ØDEGÅRD^j
C. PETRACHE^k, D. PETRACHE^k, T. STEINHARDT^l, AND O. THELEN^l

JD, Strasbourg University, CNRS France

Before proceeding further towards the physics of high temperature, shape transitions and GDR

JD, Strasbourg University, CNRS France Between Copenhagen, PARIS and Cracow

Before proceeding further towards the physics of high temperature, shape transitions and GDR let us stop at PARIS

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PARIS Project

• It is difficult to under-estimate the importance for the nuclear structure physics, of the γ -calorimeter capable of measuring the γ -energies between 100 keV and 50 MeV

• PARIS, the detector under construction, will allow studying the decay of compound nuclei with the angular momentum up to $I_{\rm max.} \approx 100 \,\hbar$, or so

• The physics phenomena discussed today, such as symmetry breaking involved during the nuclear shape transitions, the high temperature phenomena, specific effect of the coherence in the nucleonic motion: Giant Resonances (e.g. dipole), the collective rotation at very high temperatures and spins, super-deformation and hyper-deformation^{*)} – and others – will greatly profit from PARIS

*) If the spin window under control, ask me if it interests you!

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Many Thanks Adam for the Engagement in the PARIS!



JD, Strasbourg University, CNRS France Between Copenhagen, PARIS and Cracow

Many Thanks Adam for the Engagement in the PARIS!



JD, Strasbourg University, CNRS France

Many Thanks Adam for the Engagement in the PARIS!



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By the way: Do you remember enlargement of this picture?



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How about enlarging this one, Adam?



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• Weeel, since you seem interested, let us compare:

JD, Strasbourg University, CNRS France Between Copenl

• Weeel, since you seem interested, let us compare:



JD, Strasbourg University, CNRS France
• Weeel, since you seem interested, let us compare:



• Question:

What is the fundamental (technical) difference between the two photos?

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• Good answer Adam:

You got it!! I took only one of them!!!

JD, Strasbourg University, CNRS France



• Good answer Adam:

You got it!! I took only one of them!!! Which one?

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• Good answer Adam:

You got it!! I took only one of them!!! Which one? Of course the bee, Adam, of course the bee!

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Between Copenhagen, PARIS and Cracow

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Greetings...

JD, Strasbourg University, CNRS France





Greetings... More greetings...

JD, Strasbourg University, CNRS France



Greetings... More greetings... Congratulations for Adam (for Paris)...

JD, Strasbourg University, CNRS France



Greetings... More greetings... Congratulations for Adam (for Paris)... Not Paris: PARIS...

JD, Strasbourg University, CNRS France



Greetings... More greetings... Congratulations for Adam (for Paris)... Not Paris: PARIS... ???...

JD, Strasbourg University, CNRS France



Greetings... More greetings... Congratulations for Adam (for Paris)... Not Paris: PARIS... ???... PARIS? Hm... Congratulations anyway...

JD, Strasbourg University, CNRS France



Greetings... More greetings... Congratulations for Adam (for Paris)... Not Paris: PARIS... ???... PARIS? Hm... Congratulations anyway... Et, passez les excelentes Emmerdeuses pour Adam!...

JD, Strasbourg University, CNRS France



Greetings... More greetings... Congratulations for Adam (for Paris)... Not Paris: PARIS... ???... PARIS? Hm... Congratulations anyway... Et, passez les excelentes Emmerdeuses pour Adam!... Mr le President : You mean these... ladies???

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JD, Strasbourg University, CNRS France Between Cope



Les Emmerdeuses...

JD, Strasbourg University, CNRS France



Les Emmerdeuses... These are not these ladies you know and I know...

JD, Strasbourg University, CNRS France



Les Emmerdeuses... These are not these ladies you know and I know... No! These ladies are already forgotten...

JD, Strasbourg University, CNRS France



Les Emmerdeuses... These are not these ladies you know and I know... No! These ladies are already forgotten... I mean the bottle!!!

JD, Strasbourg University, CNRS France



Les Emmerdeuses... These are not these ladies you know and I know... No! These ladies are already forgotten... I mean the bottle!!! It is excellent!

JD, Strasbourg University, CNRS France



Les Emmerdeuses... These are not these ladies you know and I know... No! These ladies are already forgotten... I mean the bottle!!! It is excellent! Yes, I know this wine...

JD, Strasbourg University, CNRS France



Les Emmerdeuses... These are not these ladies you know and I know... No! These ladies are already forgotten... I mean the bottle!!! It is excellent! Yes, I know this wine... Indeed...

JD, Strasbourg University, CNRS France



Les Emmerdeuses... These are not these ladies you know and I know... No! These ladies are already forgotten... I mean the bottle!!! It is excellent! Yes, I know this wine... Indeed... Au revoir Mr le President!

JD, Strasbourg University, CNRS France

Back to Physics: Jacobi and Poincaré Transitions



Nuclear Physics A731 (2004) 319-326



www.elsevier.com/locate/npe

Evidence for the Jacobi shape transition in hot ⁴⁶Ti

A. Maj^a, M. Kmiecik^a, A. Bracco^b, F. Camera^b, P. Bednarczyk^{ac}, B. Herskind^d,
S. Brambilla^b, G. Benzoni^b, M. Brekiesz^a, D. Curien^c, G. De Angelis^e, E. Farnea^f,
J. Grębosz^a, M. Kicińska-Habior^g, S. Leoni^b, W. Męczyński^a, B. Million^b, D.R. Napoli^e,
J. Nyberg^h, C.M. Petracheⁱ, J. Styczeń^a, O. Wieland^b, M. Ziębliński^a, K. Zuber^a,
N. Dubray^c, J. Dudek^c and K. Pomorski^j

Between Copenhagen, PARIS and Cracow

JD, Strasbourg University, CNRS France









Bundeskanzlei?...

Between Copenhagen, PARIS and Cracow

JD, Strasbourg University, CNRS France





Bundeskanzlei?... Frau Bundeskanzlerin? Ja, Guten Tag...





Bundeskanzlei?... Frau Bundeskanzlerin? Ja, Guten Tag... Frau Professor Angela Bracco?...





Bundeskanzlei?... Frau Bundeskanzlerin? Ja, Guten Tag... Frau Professor Angela Bracco?... Ja, ja, she is working on the Jakobi transitions...





Bundeskanzlei?... Frau Bundeskanzlerin? Ja, Guten Tag... Frau Professor Angela Bracco?... Ja, ja, she is working on the Jakobi transitions... Jakobi? Natürlich, ein Deutcher Mathematiker...





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Schloss von Staufenberg, Baden Würtemberg

JD, Strasbourg University, CNRS France


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Examples of Some Articles: Physics Behind



• The present work on the GDR γ -decay in the hot rotating nucleus, ⁴⁶Ti, shows evidence for the expected Jacobi shape transition.

- It is based on the observation of two particular features:
- The presence of a high energy component related to large deformations;
- The appearance of a GDR component at ≈ 10 MeV (in region where the statistics is very high), identified for the first time in the present experiment

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JD, Strasbourg University, CNRS France



JD, Strasbourg University, CNRS France

In the following, we present certain recent theoretical tools to study hightemperature nuclear states in PARIS



JD, Strasbourg University, CNRS France Betw

In the following, we present certain recent theoretical tools to study hightemperature nuclear states in PARIS

"He who would like to know about the Jacobi transitions must learn about tri-axiality"

[Dudecius: Follower, 2.5×10^3 y later]

In the following, we present certain recent theoretical tools to study hightemperature nuclear states in PARIS

"He who would like to know about the Jacobi transitions must learn about tri-axiality"

[Dudecius: Follower, 2.5×10^3 y later]





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The sharpening of the tools took place a while ago through preparation of the new product called LSD

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What does the term "LSD" stand for?

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A. Photon Array for studies with Radioactive Ion and Stable Beams

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A. Photon Array for studies with Radioactive Ion and Stable BeamsB. Lazily Sadistic Dentist

What does the term "LSD" stand for?

- A. Photon Array for studies with Radioactive Ion and Stable Beams
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- C. Ligament Sadly Damaged



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- D. Libidinal Satirist's Delectation

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Yes! You are the winner!!

JD, Strasbourg University, CNRS France

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Yes! You are the winner!! Lublin-Strasbourg Drop (LSD) is a nickname of a realistic nuclear-energy expression taking into account the curvature of the nuclear surface [K. Pomorski and JD, PRC 67, 044316 2003]

Lublin-Strasbourg Drop (LSD): The Principle



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Geometry and the Surface Energy Contribution

• The nuclear surface energy comes from the nuclear matter contained in a surface region determined by its diffusivity



• For thin skin (small surface region) the amount of nuclear matter contained there is proportional to its $skin \ volume = surface \ region$

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Geometry and the Surface Energy Contribution

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Mathematical Concept of the Steiner Sheets

• A mathematical comment about universally-equidistant surfaces



• Universally equidistant surfaces form a one-parameter family defined by using the distance parameter $\Delta s \leftrightarrow s$; they are called 'Steiner sheets'

JD, Strasbourg University, CNRS France

Mathematical Concept of the Steiner Sheets

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Nuclear Surface Energy with Curvature Terms

• Denote the two principal radii of the nuclear surface by R_1 and R_2 . The local curvature is:

$$K \equiv \frac{1}{R_1} + \frac{1}{R_2}$$

• Then the volume \mathcal{V} , the surface area \mathcal{S} and the average curvature \mathcal{L} are expressible with the help of the surface Σ :

$$\mathcal{V} \equiv \frac{1}{3} \int_{\Sigma} \vec{n} \cdot d\vec{S}; \quad \mathcal{S} \equiv \int_{\Sigma} dS; \quad \mathcal{L} \equiv \int_{\Sigma} dS \left(\frac{1}{R_1} + \frac{1}{R_2} \right),$$

• They satisfy:

$$\mathcal{L}(s) = \frac{d\mathcal{S}}{ds} = \frac{d^2\mathcal{V}}{ds^2}$$

• Therefore the volume and the surface satisfy

$$\mathcal{V}(s) = \mathcal{V}_0 + \mathcal{S}_0 s + \frac{1}{2}\mathcal{L}_0 s^2 + \dots; \ \mathcal{S}(s) = \mathcal{S}_0 + \mathcal{L}_0 s + \dots,$$

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Origin of the Curvature Energy - thus the LSD

• The energy associated with the volume of the skin region is:

$$\mathcal{E}_{surf} \sim \mathcal{V}_S \sim \int_{s_1}^{s_2} \mathcal{S}(s) ds \sim \int_{s_1}^{s_2} [\mathcal{S}_0 + \mathcal{L}_0 s] \, ds$$

• Given the fact that Taylor expansion 'constants' vary with Z & N

$$\mathcal{E}_{surf} \sim \mathcal{S}_0 \underbrace{(s_2 - s_1)}_{\mathcal{C}_S(Z,N)} + \mathcal{L}_0 \underbrace{(s_2^2 - s_1^2)}_{\mathcal{C}_L(Z,N)}$$

• It then follows that

$$\mathcal{L}(s) = \frac{d\mathcal{S}}{ds} = \frac{d^2\mathcal{V}}{ds^2}$$

• Therefore the surface energy contribution satisfies:

$$\mathcal{E}_{surf} = \mathcal{C}_S(Z, N) \cdot \mathcal{S}_0 + \mathcal{C}_L(Z, N) \cdot \mathcal{L}_0$$

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• The nuclear surface energy can be decomposed using two surface terms whose A-dependences are different: $A^{2/3}$ and $A^{1/3}$

At the surface areas S₀ equal, two nuclei differing in terms of the average curvatures L₀ and L'₀, will have <u>different surface energies</u>
The final deformation energy is

$$\begin{split} E(Z,N;\mathrm{def}) &\sim \quad b_{\mathrm{area}} \left(1 - \kappa_{\mathrm{area}} I^2\right) A^{2/3} B_{\mathrm{area}}(\mathrm{def}) \\ &+ \quad b_{\mathrm{curv}} \left(1 - \kappa_{\mathrm{cur1}} I^2\right) A^{1/3} B_{\mathrm{curv}}(\mathrm{def}) \\ &+ \quad \frac{3}{5} e^2 \frac{Z^2}{r_0^{ch} A^{1/3}} B_{\mathrm{Coul}}(\mathrm{def}) + E_{\mathrm{cong}}(Z,N) \end{split}$$

• By refitting parameters of the LSD-energy expression to nearly 3000 nuclear masses we obtain $\chi^2 = 0.72$ MeV

• The <u>errors of the fission barriers</u> 'automatically' (no fit to barriers) decrease by up to the factor of 4 (!). The final improvements come from the deformation-dependent congruence-energy term

JD, Strasbourg University, CNRS France

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• At the surface areas S_0 equal, two nuclei differing in terms of the average curvatures \mathcal{L}_0 and \mathcal{L}'_0 , will have <u>different surface energies</u>

• The final deformation energy is

$$\begin{array}{ll} E(Z,N;\mathrm{def}) & \sim & b_{\mathrm{area}} \left(1 - \kappa_{\mathrm{area}} \ I^2 \ \right) A^{2/3} B_{\mathrm{area}}(\mathrm{def}) \\ & + & b_{\mathrm{curv}} \left(1 - \kappa_{\mathrm{cur1}} \ I^2 \ \right) A^{1/3} B_{\mathrm{curv}}(\mathrm{def}) \\ & + & \frac{3}{5} e^2 \frac{Z^2}{r_0^{ch} A^{1/3}} \ B_{\mathrm{Coul}}(\mathrm{def}) + E_{\mathrm{cong}}(Z,N) \end{array}$$

 \bullet By refitting parameters of the LSD-energy expression to nearly 3000 nuclear masses we obtain $\chi^2=0.72~{\rm MeV}$

• The <u>errors of the fission barriers</u> 'automatically' (no fit to barriers) decrease by up to the factor of 4 (!). The final improvements come from the deformation-dependent congruence-energy term

Table : Comparison of the barrier heights: Experimental values [Exp], LSD-model results with no congruence [LSD No C], Congruence from Myers and Świątecki [C. M.-S.], and LSD with deformation-dependent congruence-energy term.

Nucleus	Exp	Ref	LSD No C.	C. MS.	LSD-Cong.
⁷⁰ Se	39.4	[1]	50.61	43.33	40.39
76 Se	44.5	[1]	54.32	49.62	45.08
$^{75}\mathrm{Br}$	41.0	[2]	52.60	47.06	43.41
⁹⁰ Mo	42.0	[3]	50.89	45.51	42.30
⁹⁸ Mo	46.0	[3]	54.57	50.65	47.44
¹⁷³ Lu	29.0	[4]	28.70	25.63	26.79
²²⁸ Ra	6.3	[4]	6.20	6.013	6.18

• With this agreement with the experimental data, we believe, the evolution of barrier heights with spin and deformation as well as the shape transitions have good chances to be realistic.

[K. Mazurek, JD, A. Maj and D. Rouvel, Phys. Rev. C 91, 034301 (2015)]

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Jacobi Transitions - Illustrations for ${\rm ^{46}Ti}$

• Let us consider an example of the Jacobi shape transition: 46 Ti; energy obtained by minimising over nonaxial α_{22} deformation



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Jacobi Transitions - Higher Order Triaxiality [1]

- Let us add an extra tri-axial deformation, α_{42} , while minimising
- Let us subtract the energy surfaces: $E_{22+42} E_{22}$ and compare



 \bullet Observation: The maximum difference of ${\sim}180$ keV superposes with the total energy at the level of 6 MeV.

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Jacobi Transitions - Higher Order Triaxiality [1]

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Jacobi Transitions - Higher Order Triaxiality [2]

- Let us add tri-axial deformations, α_{42} and α_{62} , while minimising
- Let us subtract the surfaces: $[E_{22+42+62} E_{22+42}]$ and compare



• Observation: The maximum difference of ~ 200 keV superposes with the total energy at the level of ~ 17 MeV.

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Jacobi Transitions - Higher Order Triaxiality [2]

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- Let us subtract the surfaces: $[E_{22+42+62} E_{22+42}]$ and compare



• Observation: The maximum difference of ~ 100 keV superposes with the total energy at the level of ~ 10 MeV.

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Triaxiality Stability Tests - Conclusions

• Jacobi transitions are determined, to a good approximation, by a single tri-axial quadrupole deformation α_{22}

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• Higher order tri-axiality multipoles $(\alpha_{\lambda,2} \text{ with } \lambda \geq 4)$ are not essential for the calculations of the Jacobi transitions

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He loves really big things...





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He loves really big things... Grandioso...





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He loves really big things... Grandioso... Super-big...





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He loves really big things... Grandioso... Super-big... Hyper-big... Super-deformation, for instance... Even better: hyper-deformation... And after all: Giant Resonance...





JD, Strasbourg University, CNRS France

He loves really big things... Grandioso... Super-big... Hyper-big... Super-deformation, for instance... Even better: hyper-deformation... And after all: Giant Resonance... I should pass regards to Adam...





JD, Strasbourg University, CNRS France

He loves really big things... Grandioso... Super-big... Hyper-big... Super-deformation, for instance... Even better: hyper-deformation... And after all: Giant Resonance... I should pass regards to Adam... ... and a bottle of vodka: "Donskaya"...





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Ouufff!!

Back to physics of nuclei

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• Let us consider the nuclear motion for spins in the vicinity of the critical (transition-) spin values [the Jacobi transitions to start with]

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• Let us consider the nuclear motion for spins in the vicinity of the critical (transition-) spin values [the Jacobi transitions to start with]

• The criticality of the nuclear motion consists in the fact that:

- Nuclear shapes change dramatically, cf. the previous illustrations
- The intrinsic occupancy of nucleonic orbitals changes dramatically
- And yet, the total nuclear energy varies by a few hundreds of keV only – a typical energy of a vibrational state

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• Consequently, we propose to solve quantum mechanical problem of the nuclear collective motion, find the wave functions and the most probable deformations, with clear-cut interpretation in the context!

• Despite the fact that *model* used here to parametrize the nuclear energy is classical – the *physical nuclear system* is of course quantum

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• The corresponding Schrödinger equation has a usual general from

 $[\hat{T} + V(\alpha)] \Psi_n(\alpha) = E_n \Psi_n(\alpha) \quad \text{with} \quad V(\alpha) \leftrightarrow V_{LSD}(\alpha)$



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$$[\hat{T} + V(\alpha)] \Psi_n(\alpha) = E_n \Psi_n(\alpha) \text{ with } V(\alpha) \leftrightarrow V_{LSD}(\alpha)$$

• Knowing solutions we can calculate the expected value $\bar{\alpha}_{\lambda\mu}$ taken as a measure of the most probable deformation can be obtained as:

$$\langle \alpha_{\lambda\mu}^2 \rangle \equiv \int d\alpha \, \Psi_n^*(\alpha) \, \alpha_{\lambda\mu}^2 \Psi_n(\alpha) \ \to \ \bar{\alpha}_{\lambda\mu} = \sqrt{\langle \alpha_{\lambda\mu}^2 \rangle}$$

• In this way we obtain two, different and non-equivalent realisations of the description of physical deformations: static and dynamical:

$$(\alpha_{20}, \alpha_{22})_{stat.}$$
 and $(\bar{\alpha}_{20}, \bar{\alpha}_{22})_{dyn.}$

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Jacobi Transitions: A Comparative Study

• Results of calculations obtained by solving Schrödinger equation



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Approaching the End of the Story

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• It consists in replacing all the simplified formulae of the traditional nuclear statistical model by the microscopically-calculated objects;

• Although many building blocks of this project have been prepared in Cracow and Strasbourg, combining them is still ahead of us;

Let me wish both Angela and Adam many happy years in good health and satisfaction with numerous successful projects yet to come!

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Let me wish both Angela and Adam many happy years in good health and satisfaction with numerous successful projects yet to come!

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