The 5th International Conference on

北京大学 **GUNIVERSIT** Collective Motion in Nuclei under Extreme Conditions (COMEX5)

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# **Rod-shaped nuclei at extreme spin and isospin**

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- Introduction
- Theoretical Framework
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Nuclear deformations provide us an excellent framework to investigate the fundamental properties of quantum many-body systems.



Courtesy of Bing-Nan Lu (吕炳楠)



## Nuclear super- (hyper) deformation

Evidence for the super- and hyperdeformation provide unique opportunity to study nuclear structure under extreme conditions



Twin PRL 1986

#### Harmonic oscillator



ő (Ihree dimensions).



Nuclear super- (hyper) deformation

There have been indications that even more exotic states above 1 : 3 might exist in light N = Z nuclei due to the a cluster structure.

Towards hyperdeformation



Cluster structure in light nuclei



- Clustering in nuclei is an old story: John Archibald Wheeler, Molecular Viewpoints in Nuclear Structure, Physical Review 52 (1937) 1083
- Lots of works have been done by, e.g. Ikeda, Horiuchi, Kanada-enyo, Freer, Itagaki, Khan, Maruhn, Schuck, Tohsaki, Zhou, Ichikawa, Funaki, Von Oertzen, …
- Linear-chain structure of three-α clusters was suggested about 60 years ago Morinaga, Phys. Rev. 101, 254 (1956) to explain the structure of the Hoyle state (the second 0<sup>+</sup> state at 7.65 MeV in <sup>12</sup>C) Hoyle, Astrophys J. Sup. 1, 121 (1954).
- However, Hoyle state was later found to be a mixing of the linearchain configuration and other three-α configurations, and recently reinterpreted as an α-condensate-like state Fujiwara et al, PTP Sup. 68, 29 (1980). Tohsaki et al PRL 87, 192501 (2001). Suhara et al PRL 112, 062501 (2014).



# Alpha cluster chain and rod shape

#### Harmonic oscillator density



Freer RPP 2007

#### Green Function Monto Carlo





Because of ✓ antisymmetrization effects ✓ weak-coupling nature

it is difficult to stabilize the rod-shaped configuration in nuclear systems.



# Long existing problem: how can we stabilize geometric cluster shapes for instance linear alpha chain?





- Most of the linear chain structure have been predicted by the conventional cluster model with effective interactions determined from the binding energies and scattering phase shifts of the clusters.
- Since the DFTs do not a priori assume the existence of α clusters, it is highly desirable to have investigations based on different approaches, such as density functional theories (DFTs).
  - □ ab initio calculation of the low-lying states of carbon-12 using effective field theory Evgeny Epelbaum, Hermann Krebs, Dean Lee, and Ulf-G. Meißner, Phys. Rev. Lett. 106, 192501 (2011)
  - □ ab initio lattice calculations of the low-energy even-parity states of 16O using chiral nuclear effective field theory.



Cluster structures in (C)DFT

Studies have shown that the nucleons are prone to form cluster structure in the nuclear system with

 high excitation energy and high spin with large deformation

W. Zhang, H.-Z. Liang, S.-Q. Zhang, and J. Meng, Chin. Phys. Lett. 27, 102103 (2010).

T. Ichikawa, J. A. Maruhn, N. Itagaki, and S. Ohkubo, Phys. Rev. Lett. 107, 112501 (2011).

L. Liu & P. W. Zhao, CPC36, 818 (2012)

- deep confining nuclear potential
   J.-P. Ebran, E. Khan, T. Niksic, and D. Vretenar, Nature 487, 341 (2012).
   J.-P. Ebran, E. Khan, T. Niksic, and D. Vretenar, Phys. Rev. C 87, 044307 (2013).
- or expansion with low density M. Girod and P. Schuck, Phys. Rev. Lett. 111, 132503 (2013).





#### y How to stabilize linear chain configurations?

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Using the nuclear energy density functional, the conditions for single nucleon localization and formation of cluster structures in finite nuclei are examined.



A localized equilibrium density and the formation of cluster structures are visible in (a) DD-ME2 but not in (b) Skyrme SLy4

J-P Ebran et al. Nature 487, 341-344 (2012) doi:10.1038/nature11246



<sup>240</sup>Pu: 3-dim. PES ( $\beta_{20}$ ,  $\beta_{22}$ ,  $\beta_{30}$ )



- □ AS & RS for g.s. & isomer, the latter is stiffer
- Triaxial & octupole shape around the outer barrier
- Triaxial deformation crucial around barriers



 $\beta_{22}$  Lu, Zhao, Zhou Phys. Rev. C 85, 011301(R) Zhao, Lu, Vretenar, Zhao, and Zhou, Phys. Rev. C 91 014321 (2015)



#### J. Meng, H. Toki, S.-G. Zhou, S.Q. Zhang, W.H. Long, ang L.S. Geng, Prog. Part. Nucl. Phys. 57 (2006) 470-563

孟杰, 郭建友, 李剑, 李志攀, 梁豪兆, 龙文辉, 牛一斐, 牛中明, 尧江明, 张颖, 赵鹏巍, 周善贵, 原子核物理中的协变密度泛函理论, 物理学进展, 第31卷04 期 (2011) 199-336

J. Meng, J. Peng, S.Q. Zhang, and P.W. Zhao, Front. Phys. 8 (2013) 55-79

- H. Z. Liang, J. Meng, and S.-G. Zhou, Phys. Rep. 570 (2015) 1-84
- J. Meng and S.-G. Zhou, J. Phys. G: Nucl. Part. Phys. 42 (2015) 093101



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Hyperdeformed Rod shaped α-Linear Chain Structure



- Cranking CDFT to investigate the stabilization of rod shape at extreme spin and isospin in a fully self-consistent and microscopic way.
- By adding valence neutrons and rotating the system, the mechanism stabilizing the rod shape will be explored.
- > CDFT configuration mixing of PN-AM projected calculation will be carried out to find evidence for  $4\alpha$  linear cluster structure.

Yao, Itagaki, Meng, Phys. Rev. C **90**, 054307 (2014) Zhao, Itagaki, Meng, Phys. Rev. Lett. 115, 022501 (2015)



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# Density functional theory

The many-body problem is mapped onto an one-body problem without explicitly involving inter-nucleon interactions!



Kohn-Sham Density Functional Theory

For any interacting system, there exists a **local single-particle potential** *h(r)*, such that the exact ground-state density of the interacting system can be reproduced by **non-interacting particles** moving in this local potential.

$$E[\rho] \Rightarrow \hat{h} = \frac{\delta E}{\delta \rho} \Rightarrow \hat{h} \varphi_i = \varepsilon_i \varphi_i \Rightarrow \rho = \sum_{i=1}^A |\varphi_i|^2$$

The practical usefulness of the Kohn-Sham scheme depends entirely on whether Accurate Energy Density Functional can be found!



• For nuclei, the energy density functional has been introduced by effective Hamiltonians

$$E = \langle \Psi | H | \Psi \rangle \approx \langle \Phi | \hat{H}_{eff}(\hat{\rho}) | \Phi \rangle = E[\hat{\rho}]$$

- More degrees of freedom: spin, isospin, pairing, ...
- Nuclei are self-bound systems;
   ρ(r) here denotes the intrinsic density.
- Density functional is probably not exact, but a very good approximation.
- The functional are adjusted to properties of nuclear matter and/or finite nuclei and (in future) to ab-initio results.

## Why Covariant?

P. Ring Physica Scripta, T150, 014035 (2012)



### Covariant Density Functional Theory

Elementary building blocks

 $(\bar{\psi}\mathcal{O}_{\tau}\Gamma\psi) \qquad \mathcal{O}_{\tau}\in\{1,\tau_i\} \qquad \Gamma\in\{1,\gamma_{\mu},\gamma_5,\gamma_5\gamma_{\mu},\sigma_{\mu\nu}\}$ 

#### **Densities and currents**

Isoscalar-scalar  $\rho_{S}(\mathbf{r}) = \sum_{k}^{occ} \bar{\psi}_{k}(\mathbf{r})\psi_{k}(\mathbf{r})$ Isoscalar-vector  $j_{\mu}(\mathbf{r}) = \sum_{k}^{occ} \bar{\psi}_{k}(\mathbf{r})\gamma_{\mu}\psi_{k}(\mathbf{r})$ Isovector-scalar  $\bar{\rho}_{S}(\mathbf{r}) = \sum_{k}^{occ} \bar{\psi}_{k}(\mathbf{r})\vec{\tau}\psi_{k}(\mathbf{r})$ Isovector-vector  $\bar{j}_{\mu}(\mathbf{r}) = \sum_{k}^{occ} \bar{\psi}_{k}(\mathbf{r})\vec{\tau}\gamma_{\mu}\psi_{k}(\mathbf{r})$  **Energy Density Functional** 

$$egin{aligned} E_{kin} &= \sum_k v_k^2 \int ar{\psi}_k \left( -\gamma 
abla + m 
ight) \psi_k d\mathbf{r} \ E_{2nd} &= rac{1}{2} \int (lpha_S 
ho_S^2 + lpha_V 
ho_V^2 + lpha_{tV} 
ho_{tV}^2) d\mathbf{r} \ E_{hot} &= rac{1}{12} \int (4 eta_S 
ho_S^3 + 3 \gamma_S 
ho_S^4 + 3 \gamma_V 
ho_V^4) d\mathbf{r} \ E_{der} &= rac{1}{2} \int (\delta_S 
ho_S riangle 
ho_S + \delta_V 
ho_V riangle 
ho_V + \delta_{tV} 
ho_{tV} riangle 
ho_{tV}) d\mathbf{r} \ E_{em} &= rac{e}{2} \int j_\mu^p A^\mu d\mathbf{r} \end{aligned}$$

#### Cranking Covariant Density Functional Theory

Transform to the frame rotating with a uniform velocity

$$x^{\alpha} = \begin{pmatrix} t \\ \boldsymbol{x} \end{pmatrix} \to \tilde{x}^{\mu} = \begin{pmatrix} \tilde{t} \\ \tilde{\boldsymbol{x}} \end{pmatrix} = \begin{pmatrix} 1 & \boldsymbol{0} \\ \boldsymbol{0} & R_{x}(t) \end{pmatrix} \begin{pmatrix} t \\ \boldsymbol{x} \end{pmatrix}$$

**Rotating Density Functional** 



Peng, Meng, P. Ring, and S. Q. Zhang, Phys. Rev. C 78, 024313 (2008).
Zhao, Zhang, Peng, Liang, Ring, and Meng, Phys. Lett. B 699, 181 (2011).
Zhao, Peng, Liang, Ring, and Meng, Phys. Rev. Lett. 107, 122501 (2011).
Zhao, Peng, Liang, Ring, and Meng, Phys. Rev. C 85, 054310 (2012).
Meng, Peng, Zhang, and Zhao, Front. Phys. 8, 55 (2013).

# Kohn-Sham/Dirac Equation:

Dirac equation for single nucleon

$$\begin{pmatrix} m+S+V-\Omega \bullet J & \sigma(\rho-V) \\ \sigma(\rho-V) & -m-S+V-\Omega \bullet J \end{pmatrix} \begin{pmatrix} f \\ g \end{pmatrix} = \varepsilon \begin{pmatrix} f \\ g \end{pmatrix}$$

$$\mathbf{V}(\mathbf{r}) = \alpha_{v}\rho_{v} + \gamma_{v}\rho_{v}^{s} + \delta_{v}\Delta\rho_{v} + \tau_{v}\alpha_{v}\rho_{v} + \tau_{v}\delta_{v}\Delta\rho_{v} + e^{\frac{1-\tau_{v}}{2}A}$$
$$\mathbf{V}(\mathbf{r}) = \alpha_{v}\mathbf{j}_{v} + \gamma_{v}\mathbf{j}_{v}^{s} + \delta_{v}\Delta\mathbf{j}_{v} + \tau_{v}\alpha_{v}\mathbf{j}_{v}\mathbf{j}_{v} + \tau_{v}\delta_{v}\mathbf{v}\Delta\mathbf{j}_{v} + e^{\frac{1-\tau_{v}}{2}A}$$
$$\mathbf{S}(\mathbf{r}) = \alpha_{v}\rho_{s} + \beta_{s}\rho_{s}^{s} + \gamma_{s}\rho_{v}^{s} + \delta_{s}\Delta\rho_{v}$$

V(r) vector potential time-likeV(r) vector potential space-likeS(r) scalar potential

# Observables

Binding energy

$$E_{\text{tot}} = \sum_{k=1}^{A} \epsilon_{k} - \int d^{3}r \left\{ \frac{1}{2} \alpha_{S} \rho_{S}^{2} + \frac{1}{2} \alpha_{V} j_{V}^{\mu} (j_{V})_{\mu} \right. \\ \left. + \frac{1}{2} \alpha_{TV} j_{TV}^{\mu} (j_{TV})_{\mu} + \frac{2}{3} \beta_{S} \rho_{S}^{3} + \frac{3}{4} \gamma_{S} \rho_{S}^{4} \right. \\ \left. + \frac{3}{4} \gamma_{V} \left( j_{V}^{\mu} (j_{V})_{\mu} \right)^{2} + \frac{1}{2} \delta_{S} \rho_{S} \Delta \rho_{S} + \frac{1}{2} \delta_{V} (j_{V})_{\mu} \Delta j_{V}^{\mu} \right. \\ \left. + \frac{1}{2} \delta_{TV} j_{TV}^{\mu} \Delta (j_{TV})_{\mu} + \frac{1}{2} e j_{p}^{0} A_{0} \right\} + \sum_{k=1}^{A} \langle k | \boldsymbol{\Omega} \, \boldsymbol{\hat{J}} | k \rangle \\ \left. + E_{\text{c.m.}} \right\}$$

Angular momentum

$$J = \sqrt{\langle \hat{J}_x \rangle^2 + \langle \hat{J}_z \rangle^2} \equiv \sqrt{I(I+1)},$$

Quadrupole moments and magnetic moments

$$Q_{20} = \sqrt{\frac{5}{16\pi}} \langle 3z^2 - r^2 \rangle,$$
  

$$Q_{22} = \sqrt{\frac{15}{32\pi}} \langle x^2 - y^2 \rangle,$$
  

$$\mu = \sum_{i=1}^{A} \int d^3r \left[ \frac{mc^2}{\hbar c} q \psi_i^{\dagger}(\mathbf{r}) \mathbf{r} \times \boldsymbol{\alpha} \psi_i(\mathbf{r}) + \kappa \psi_i^{\dagger}(\mathbf{r}) \beta \boldsymbol{\Sigma} \psi_i(\mathbf{r}) \right],$$



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DD-ME2, 3D HO basis with N = 12 major shells



- ➢ C-12, C-13, C-14
  - constant moments of inertia (MOI); like a rotor
- C-15, C-16, C-17, C-18

abrupt increase of MOI; some changes in structure

➤ C-19; C-20

constant moments of inertia; much larger

Rod shape are obtained in all isotopes by tracing the corresponding rod-shaped configuration.

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Zhao, Itagaki, Meng, Phys. Rev. Lett. 115, 022501 (2015)



Zhao, Itagaki, Meng, Phys. Rev. Lett. 115, 022501 (2015)









Related experiment is highly demanded !



Zhao, Itagaki, Meng, Phys. Rev. Lett. 115, 022501 (2015)





#### Beyond RMF calculation with GCM for low-spin states

The wave function of nuclear low-spin state is given by the superposition of a set of both particle-number and angular-momentum projected (PNAMP) quadrupole deformed mean-field states in the framework of GCM

$$|JNZ;\alpha\rangle = \sum_{q,K} f_{\alpha}^{JNZK}(q) \hat{P}_{MK}^J \hat{P}^N \hat{P}^Z |q(\beta,\gamma)\rangle.$$

Minimization of nuclear total energy with respect to the coefficient f leads to the Hill-Wheeler-Griffin (HWG) equation (Restricted to be axially deformed, and K=0)

$$\sum_{\beta'} [\mathcal{H}^J(\beta, \beta') - E^J_\alpha \mathcal{N}^J(\beta, \beta')] f^{JNZ}_\alpha(\beta') = 0,$$



CDFT+GCM: clustering in light nuclei



- Linear-Chain-Structure (LCS) in the low-spin GCM states with moment of inertia around 0.11 MeV is found.
- 4-alpha clusters stay in z-axis and nucleons occupy the states in a nonlocal way.
- Spin and orbital angular momenta of all nucleons are parallel in the LCS states.
- Fully microscopic GCM calculation has reproduced the excitation energies and B(E2) values rather well for the rotational band built on the second 0<sup>+</sup> state.



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# Summary

- Novel shape, rod-shaped C isotopes, known to be difficult to stabilize for a long time, has been studied
- The advantages of cranking CDFT include (i) the cluster structure is investigated without assuming the existence of clusters a priori, (ii) the nuclear currents are treated self-consistently, (iii) the density functional is universal, and (iv) a microscopic picture can be provided in terms of intrinsic shapes and single-particle shells self-consistently.
- Two mechanisms to stabilize the rod shape: rotation (high spin) and adding neutrons (high Isospin), coherently work in C isotopes
- Coherent Effects: Rotation makes the valence sigma neutron-orbital lower, and thus 1) lower the sigma proton orbitals 2) enhances the prolate deformation of protons

Outlook: bend motion? valence proton? ...



#### In collaboration with

#### Naoyuki Itagaki, Jiangming Yao, Pengwei Zhao

# Thank you for your attention!