

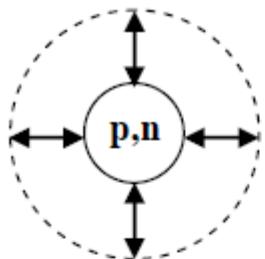
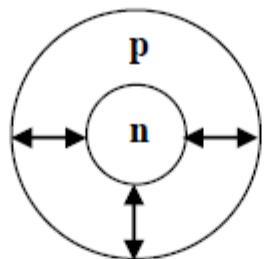
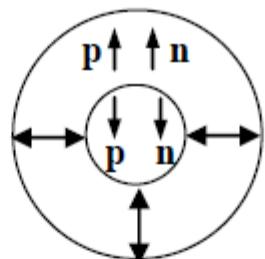
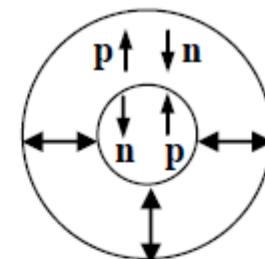
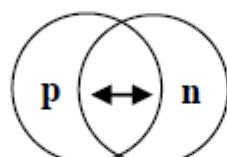
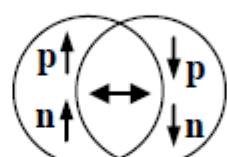
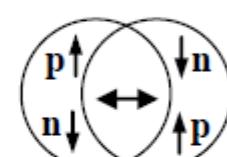
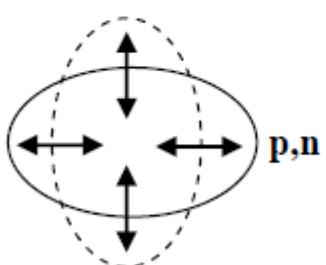
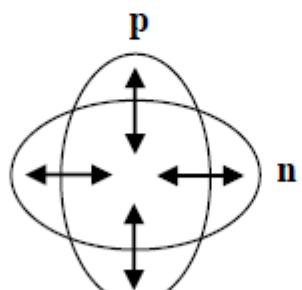
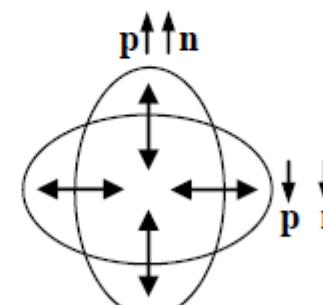
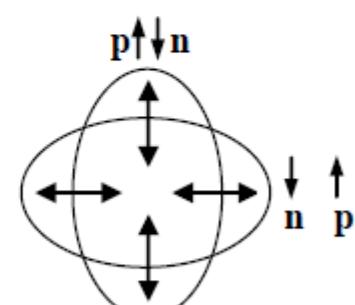
COLLECTIVE EXCITATIONS OF ATOMIC NUCLEI

Muhsin N. Harakeh

KVI-CART, Groningen & GANIL, Caen

Collective Motion of Nuclei under Extreme
Conditions (COMEX 5)

Kraków, Poland

$\Delta L = 0$ **ISGMR****IVGMR****ISSGMR****IVSGMR** $\Delta L = 1$ **ISGDR**
??**IVGDR****ISSGDR****IVSGDR** $\Delta L = 2$ **ISGQR****IVGQR****ISSGQR****IVSGQR** $\Delta T = 0$ $\Delta S = 0$ $\Delta T = 1$ $\Delta S = 0$ $\Delta T = 0$ $\Delta S = 1$ $\Delta T = 1$ $\Delta S = 1$

Microscopic picture: GRs are coherent (1p-1h) excitations induced by single-particle operators.

- Excitation energy depends on
 - i) multipole L ($L\hbar\omega$, since radial operator $\propto r^L$; except for ISGMR and ISGDR, $2\hbar\omega$ & $3\hbar\omega$, respectively),
 - ii) strength of effective interaction and
 - iii) collectivity.
- Exhaust appreciable % of EWSR
- Acquire a width due to coupling to continuum and to underlying 2p-2h configurations.

Microscopic structure of ISGMR & ISGDR

Transition operators:

$$O^{L=0} = \sum_i r_i^0 Y_0^0 + \frac{1}{2} \sum_i r_i^2 Y_0^0 + \dots$$

Constant Overtone

$2\hbar\omega$ excitation

$$O^{L=1} = \sum_i r_i^1 Y_0^1 + \frac{1}{2} \sum_i r_i^3 Y_0^1 + \dots$$

Spurious Overtone
c.o.m. motion

$3\hbar\omega$ excitation (overtone of c.o.m. motion)

Nucleus \longrightarrow Many-body system with a finite size

Vibrations \longrightarrow Multipole expansion with r, Y_{lm}, τ, σ

$\Delta S=0, \Delta T=0$ $\Delta S=0, \Delta T=1$ $\Delta S=0, \Delta T=1$ $\Delta S=1, \Delta T=1$ $\Delta S=1, \Delta T=1$

L=0: Monopole	ISGMR $r^2 Y_0$	IAS τY_0	IVGMR $\tau r^2 Y_0$	GTR $\tau \sigma Y_0$	IVSGMR $\tau \sigma r^2 Y_0$
L=1: Dipole	ISGDR $r^3 Y_1 (-5/3 \langle r^2 \rangle r Y_1)$		IVGDR $\tau r Y_1$		IVSGDR $\tau \sigma r Y_1$
L=2: Quadrupole	ISGQR $r^2 Y_2$		IVGQR $\tau r^2 Y_2$		IVSGQR $\tau \sigma r^2 Y_2$
L=3: Octupole	LEOR, HEOR $r^3 Y_3$				

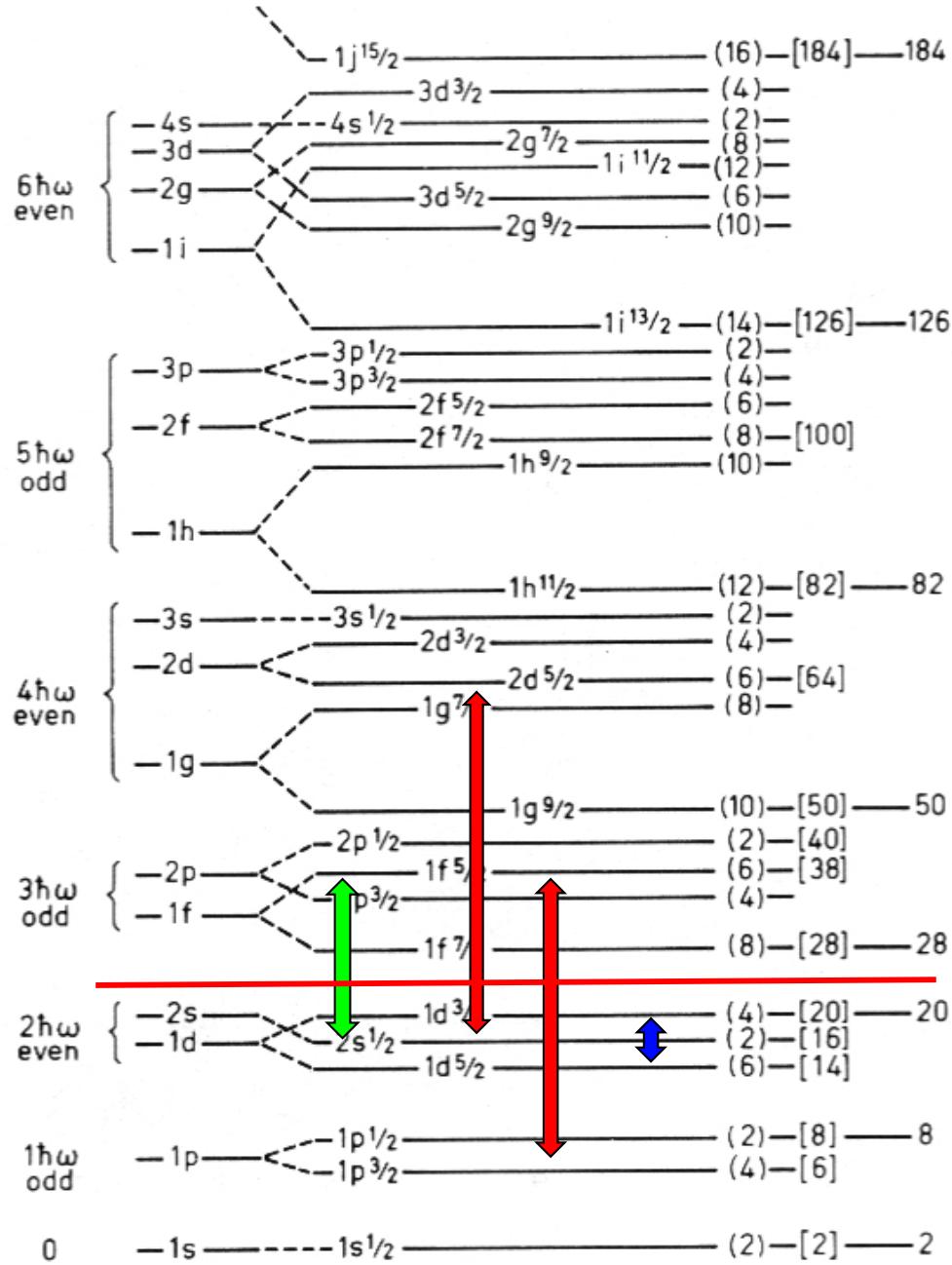
IVGDR
 τrY_1

↔ **$\Delta N = 1$ E1 (IVGDR)**

↔ **$\Delta N = 2$** } **E2 (ISGQR)**
↔ **$\Delta N = 0$** } **&**
↔ **$\Delta N = 0$** } **E0 (ISGMR)**

ISGMR
 r^2Y_0

ISGQR
 r^2Y_2



Decay of giant resonances

■ Width of resonance

$$\Gamma, \Gamma^\uparrow, \Gamma^\downarrow (\Gamma^{\downarrow\uparrow}, \Gamma^{\downarrow\downarrow})$$

■ Γ^\uparrow : direct or escape width

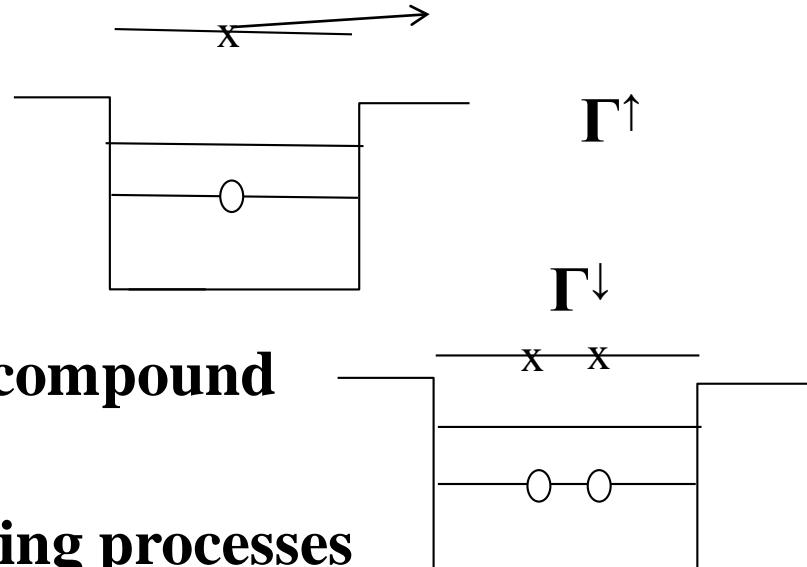
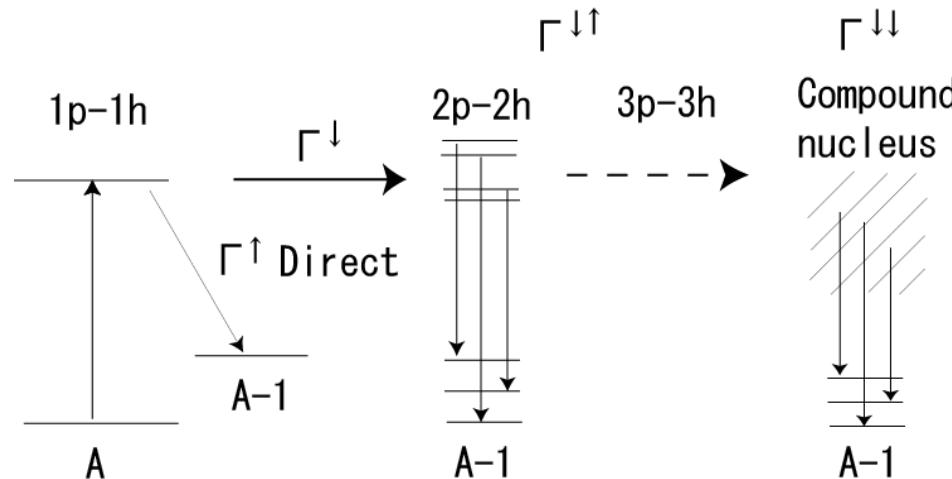
■ Γ^\downarrow : spreading width

$\Gamma^{\downarrow\uparrow}$: pre-equilibrium, $\Gamma^{\downarrow\downarrow}$: compound

■ Decay measurements

⇒ Direct reflection of damping processes

Allows detailed comparison with theoretical calculations

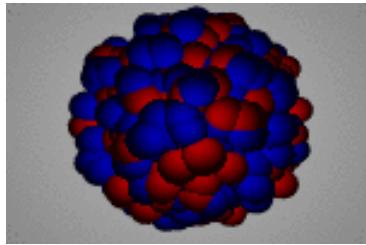


The collective response of the nucleus

Giant Resonances

Electric giant resonances

Isoscalar



Monopole
(GMR)

Dipole
(GDR)

Quadrupole
(GQR)

Isovector

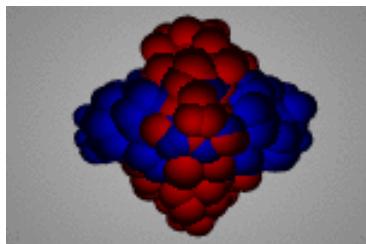
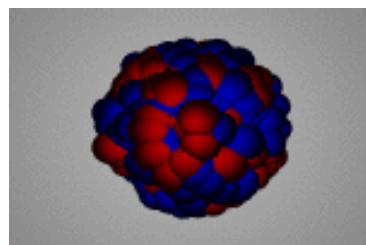
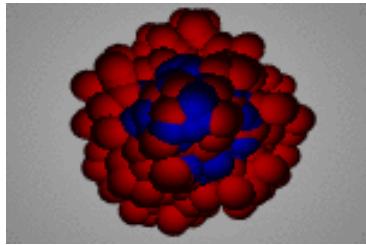
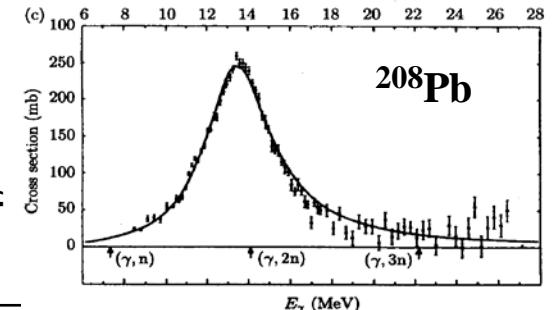
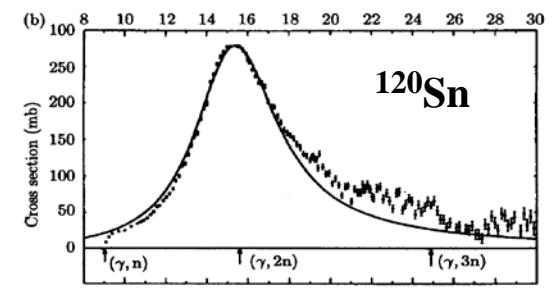
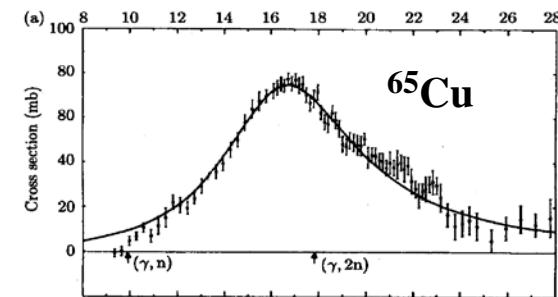
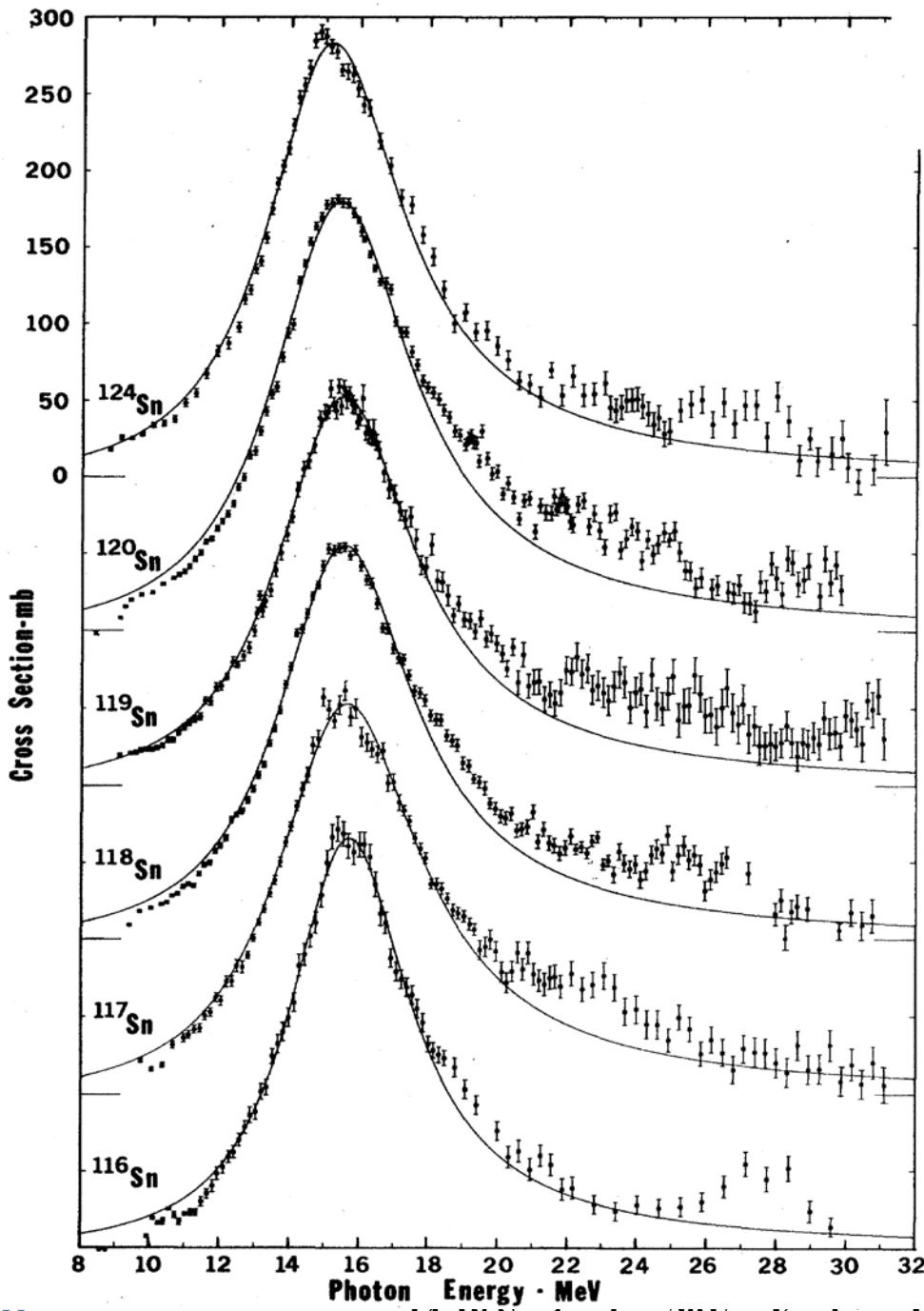


Photo-neutron
cross sections



Berman and Fultz, Rev. Mod. Phys. 47 (1975)

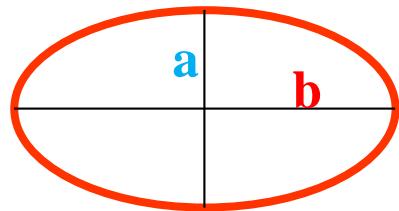
47



Measurement of the giant dipole resonance with mono-energetic photons

B.L. Berman and S.C. Fultz
Rev. Mod. Phys. 47 (1975) 713

Nucleus	Centroid (MeV)	Width (MeV)
116Sn	15.68	4.19
117Sn	15.66	5.02
118Sn	15.59	4.77
119Sn	15.53	4.81
120Sn	15.40	4.89
124Sn	15.19	4.81

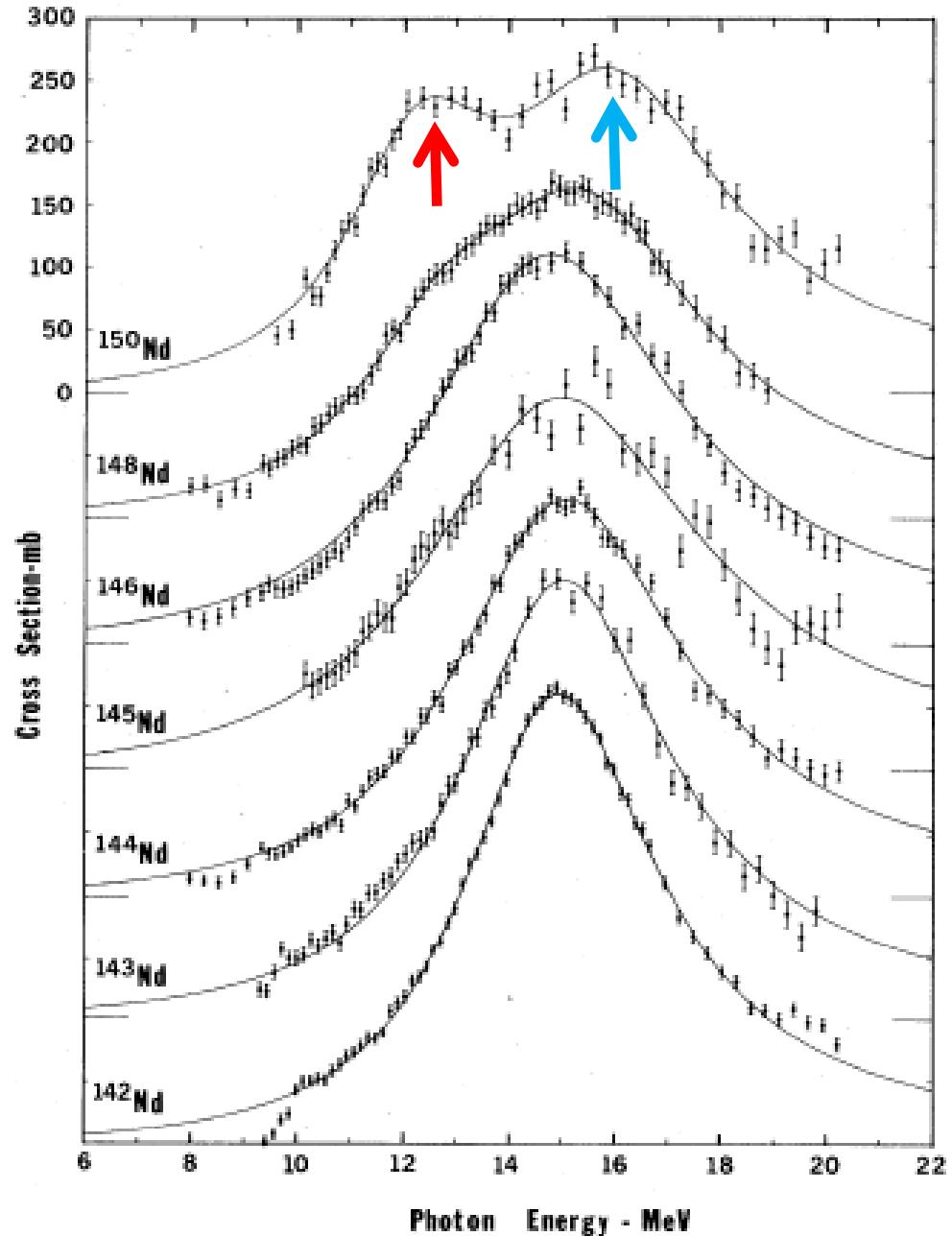
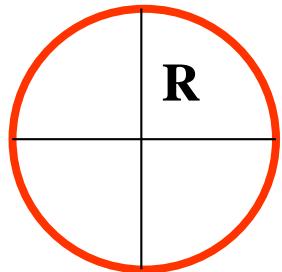


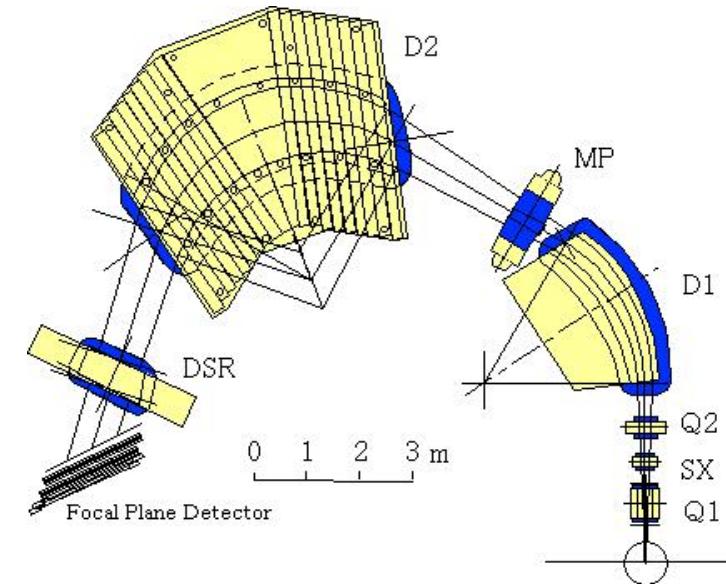
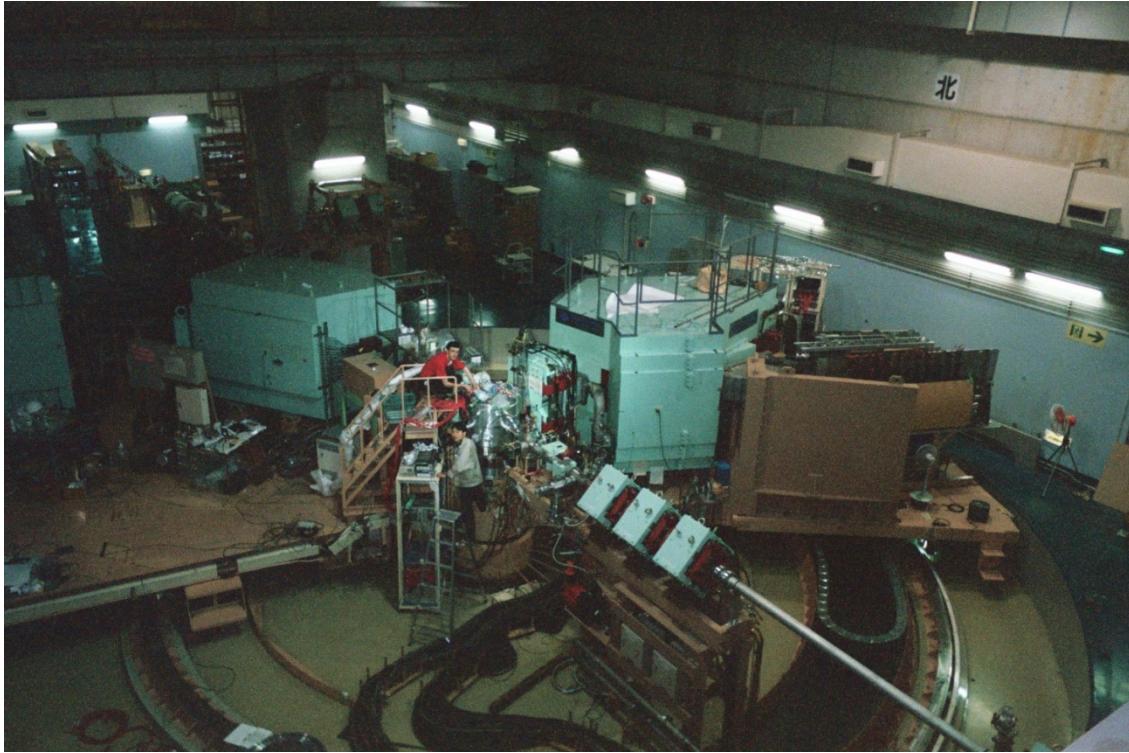
Quadrupole deformation:
 $\beta_2 = 0.275$

Excitation energies:
 $E_2/E_1 = 0.911\eta + 0.089$

Where $\eta = b/a$

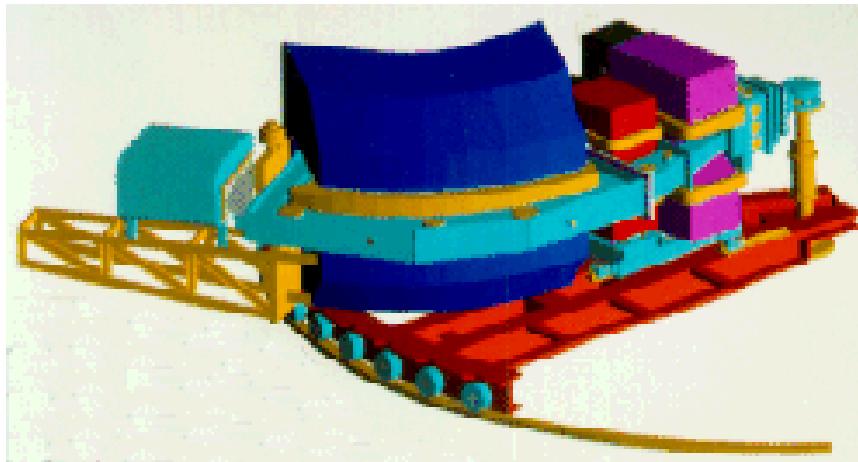
$$S_1/S_2 = 1/2$$



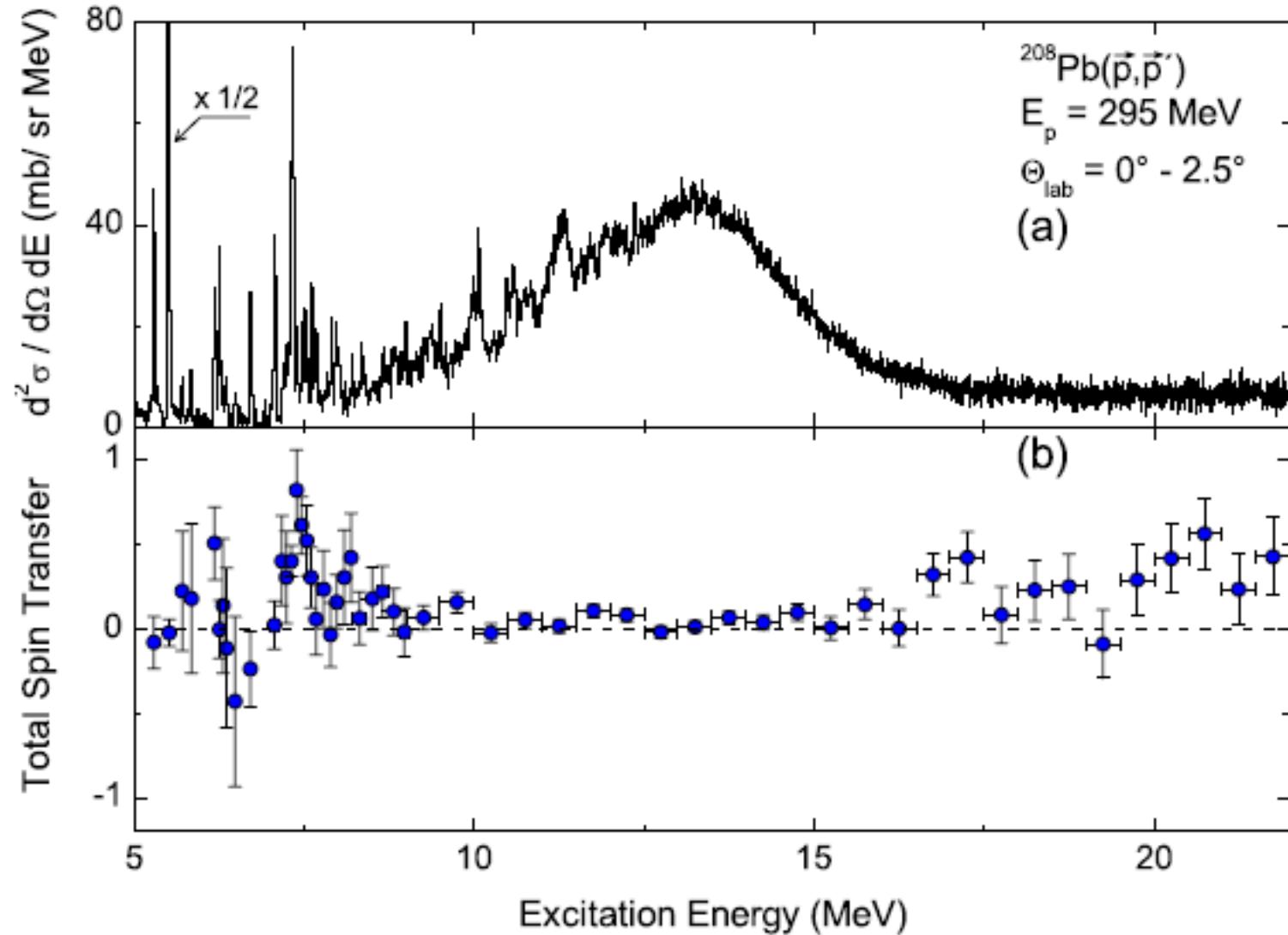


Grand Raiden@ RCNP

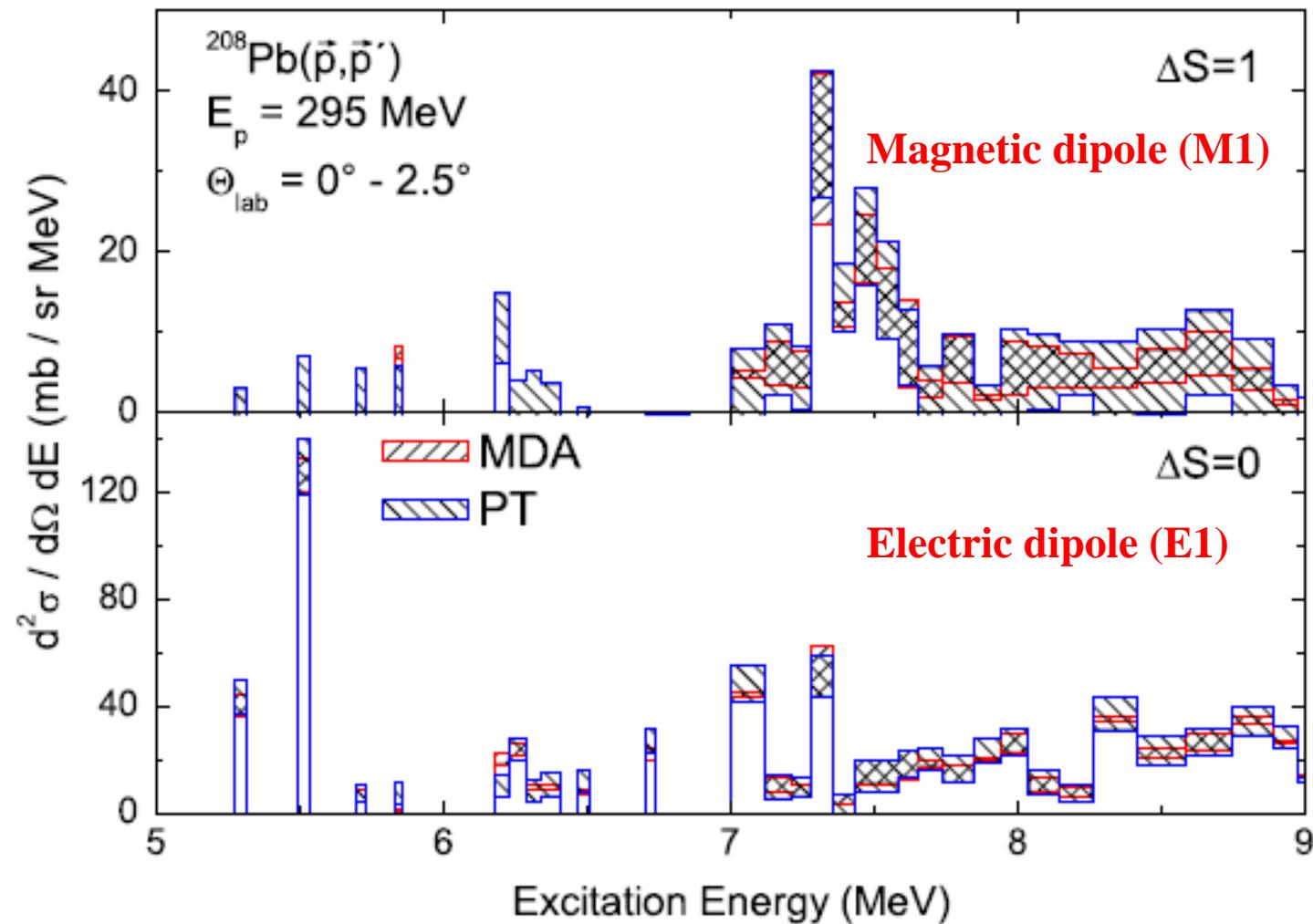
(p, p') at $E_p \sim 300$
 (α, α') at $E_\alpha \sim 400$
& 200 MeV at
RCNP & KVI,
respectively



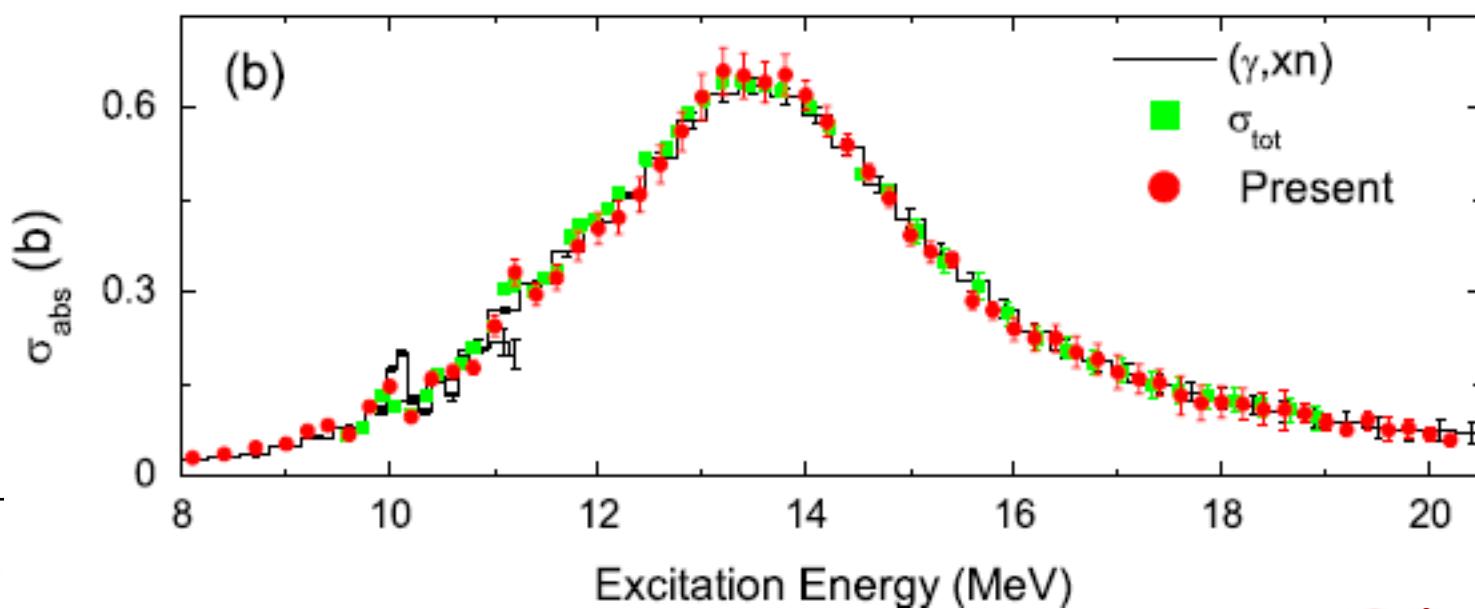
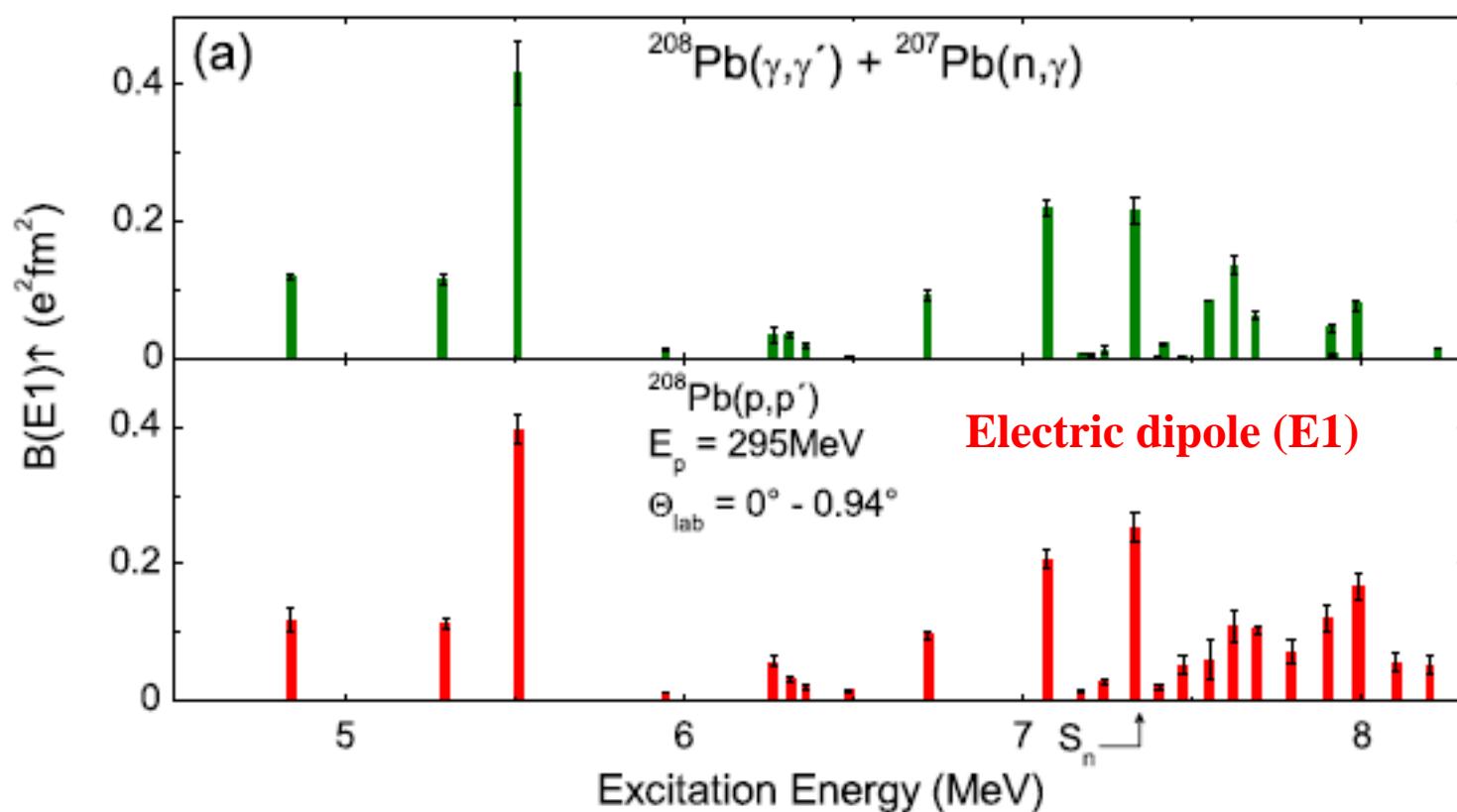
BBS@KVI



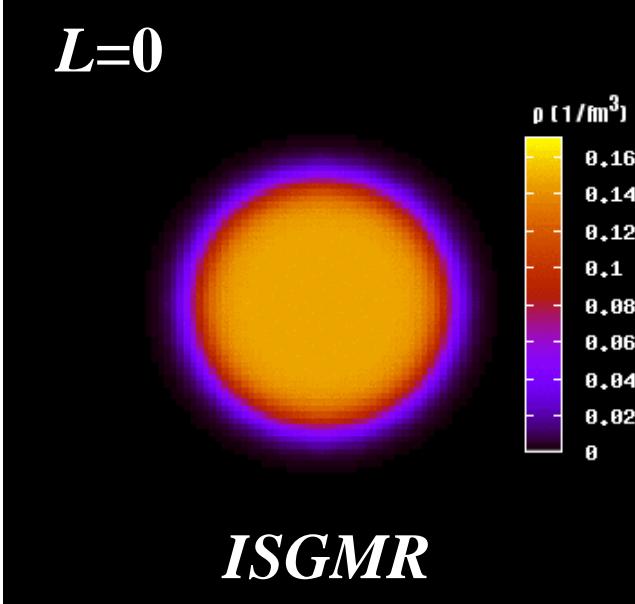
A. Tamii *et al.*, PRL 107 (2011) 062502



A. Tamii *et al.*, PRL 107 (2011) 062502

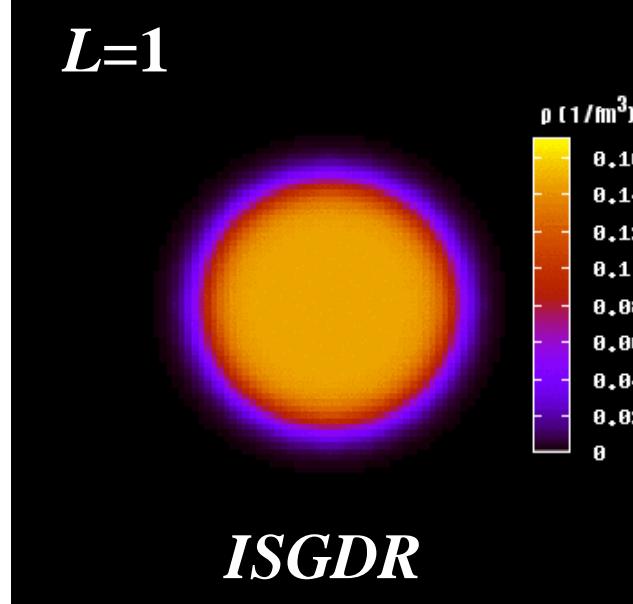


$L=0$



ISGMR

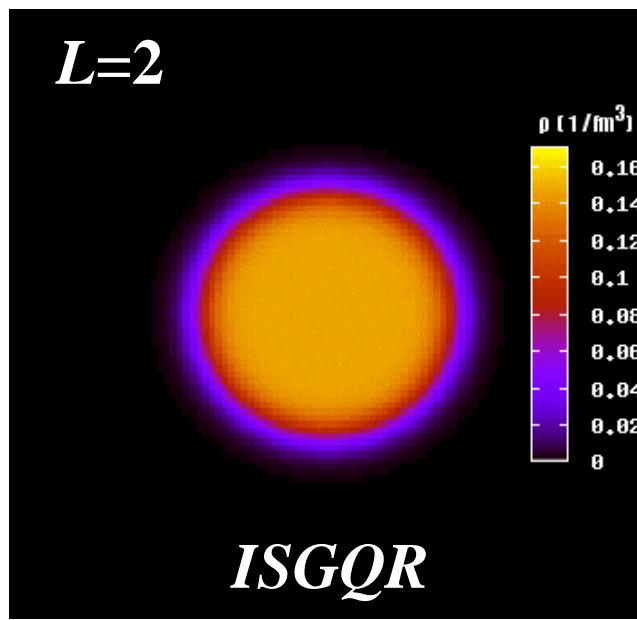
$L=1$



ISGDR

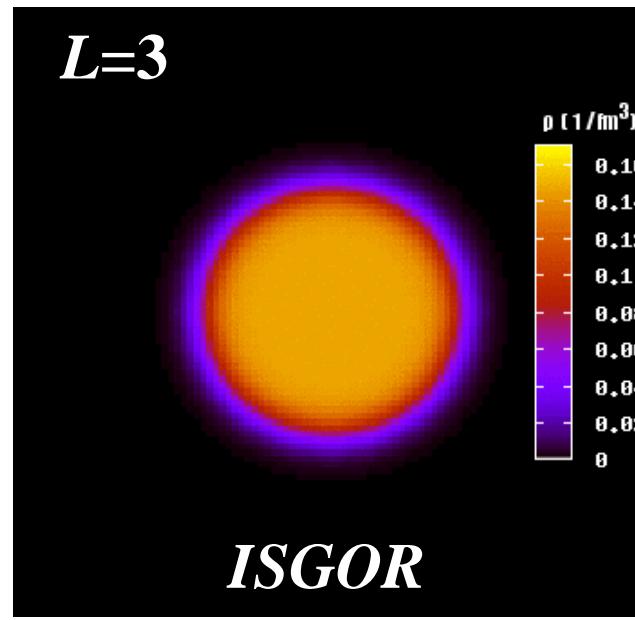
M. Itoh

$L=2$



ISGQR

$L=3$



ISGOR

In fluid mechanics, **compressibility** is a measure of the relative volume change of a fluid as a response to a pressure change.

$$\beta = -\frac{1}{V} \frac{\partial V}{\partial P}$$

where P is pressure, V is volume.

Incompressibility or **bulk modulus** (K) is a measure of a substance's resistance to uniform compression and can be formally defined:

$$K = -V \frac{\partial P}{\partial V}$$

For the equation of state of symmetric nuclear matter at saturation nuclear density:

$$\left[\frac{d(E/A)}{d\rho} \right]_{\rho=\rho_0} = 0$$

and one can derive the incompressibility of nuclear matter:

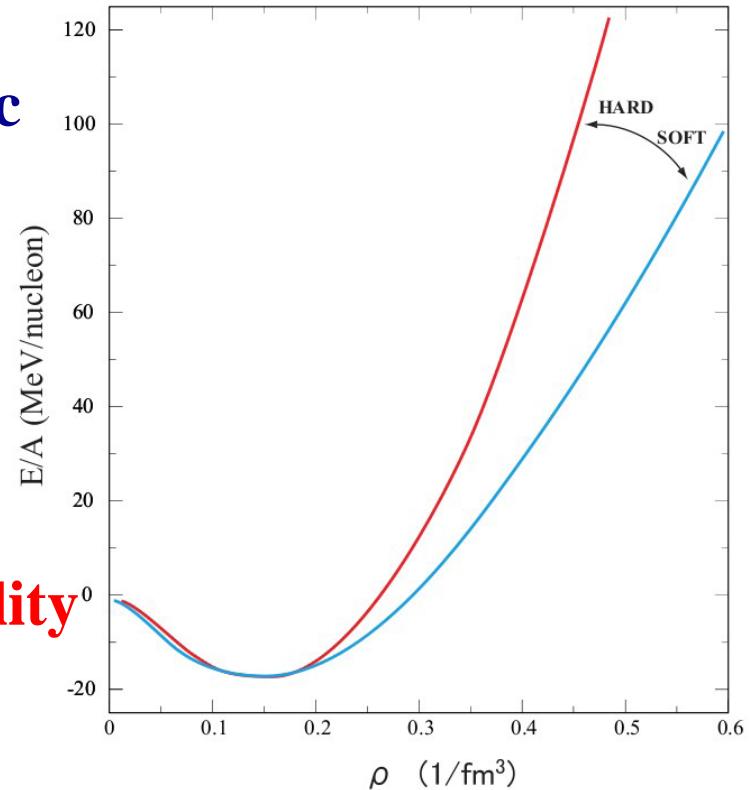
$$K_{nm} = \left[9\rho^2 \frac{d^2(E/A)}{d\rho^2} \right]_{\rho=\rho_0}$$

E/A: binding energy per nucleon

ρ : nuclear density

J.P. Blaizot, Phys. Rep. 64 (1980) 171

ρ_0 : nuclear density at saturation



Equation of state (EOS) of nuclear matter:

**More complex than for infinite neutral liquids:
Neutrons and protons with different interactions
Coulomb interaction of protons**

1. **Governs the collapse and explosion of giant stars (supernovae)**
2. **Governs formation of neutron stars (mass, radius, crust)**
3. **Governs collisions of heavy ions.**
4. **Important ingredient in the study of nuclear properties.**

Isoscalar Excitation Modes of Nuclei

Hydrodynamic models/Giant Resonances

Coherent vibrations of nucleonic fluids in a nucleus.

Compression modes : ISGMR, ISGDR

In Constrained and Scaling Models:

$$E_{ISGMR} = \hbar \sqrt{\frac{K_A}{m \langle r^2 \rangle}}$$

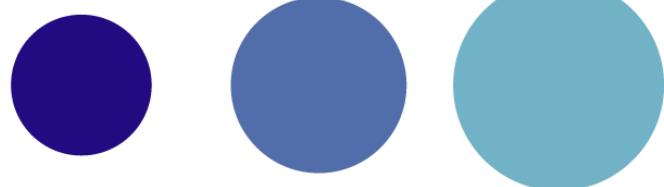
$$E_{ISGDR} = \hbar \sqrt{\frac{7}{3} \frac{K_A + \frac{27}{25} \varepsilon_F}{m \langle r^2 \rangle}}$$

ε_F is the Fermi energy and the nucleus incompressibility:

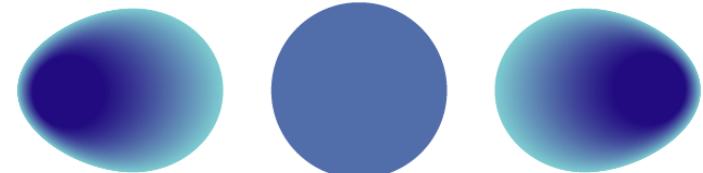
$$\rightarrow K_A = \left[r^2 (d^2(E/A)/dr^2) \right]_{r=R_0}$$

J.P. Blaizot, Phys. Rep. 64 (1980) 171

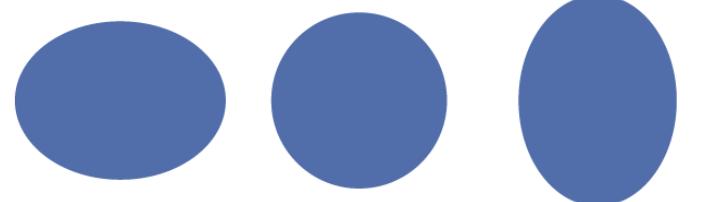
ISGMR (T=0, L=0)



ISGDR (T=0, L=1)



ISGQR (T=0, L=2)

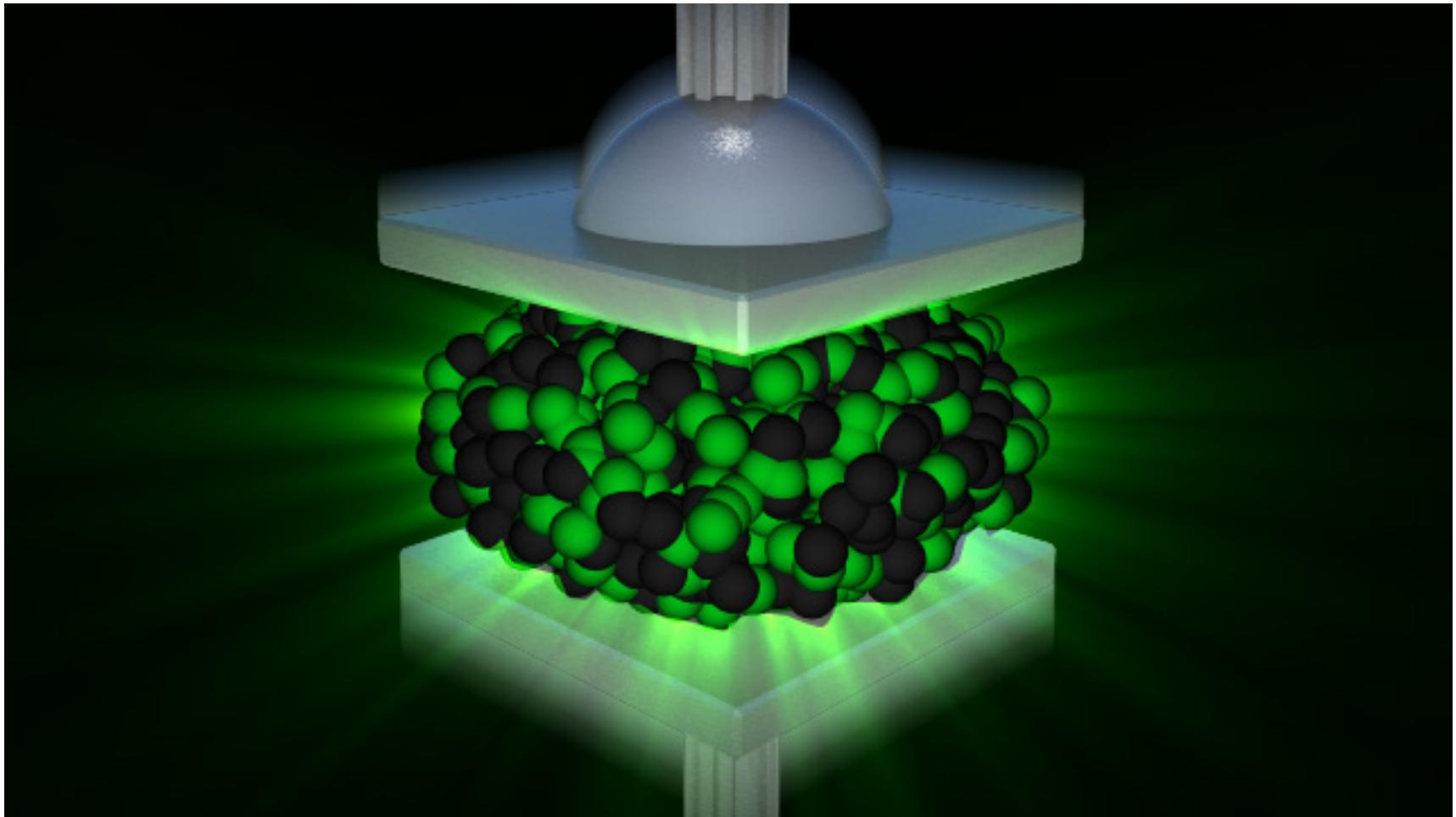


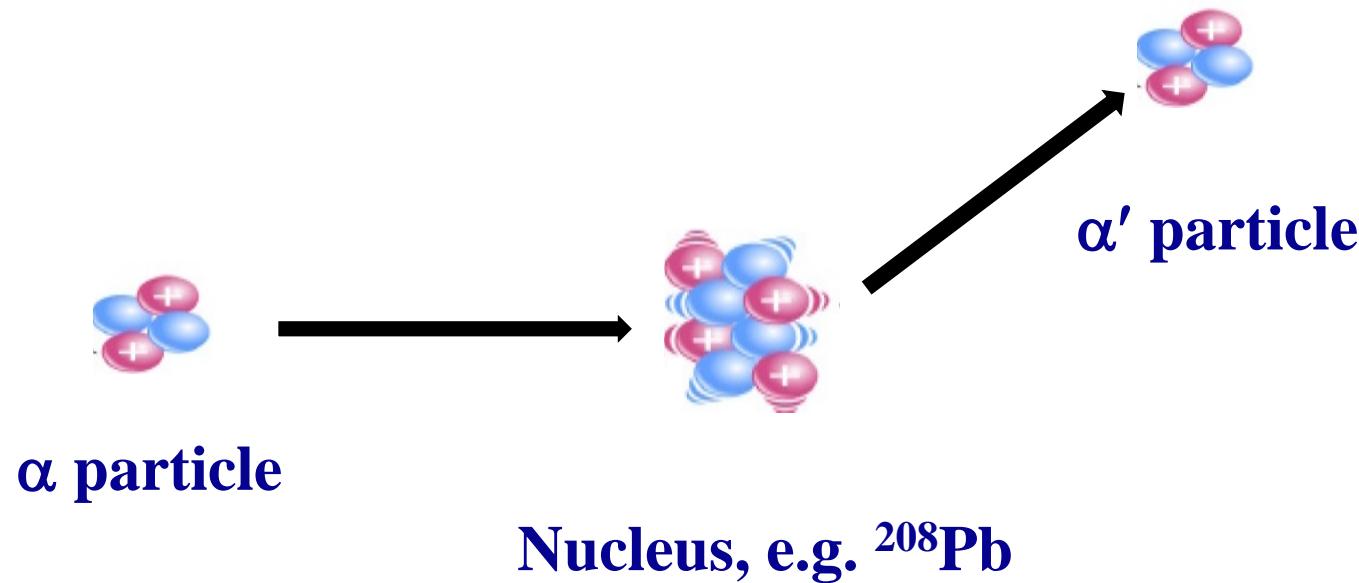
Giant resonances

- **Macroscopic properties:** E_x , Γ , %EWSR
- **Isoscalar giant resonances; compression modes**

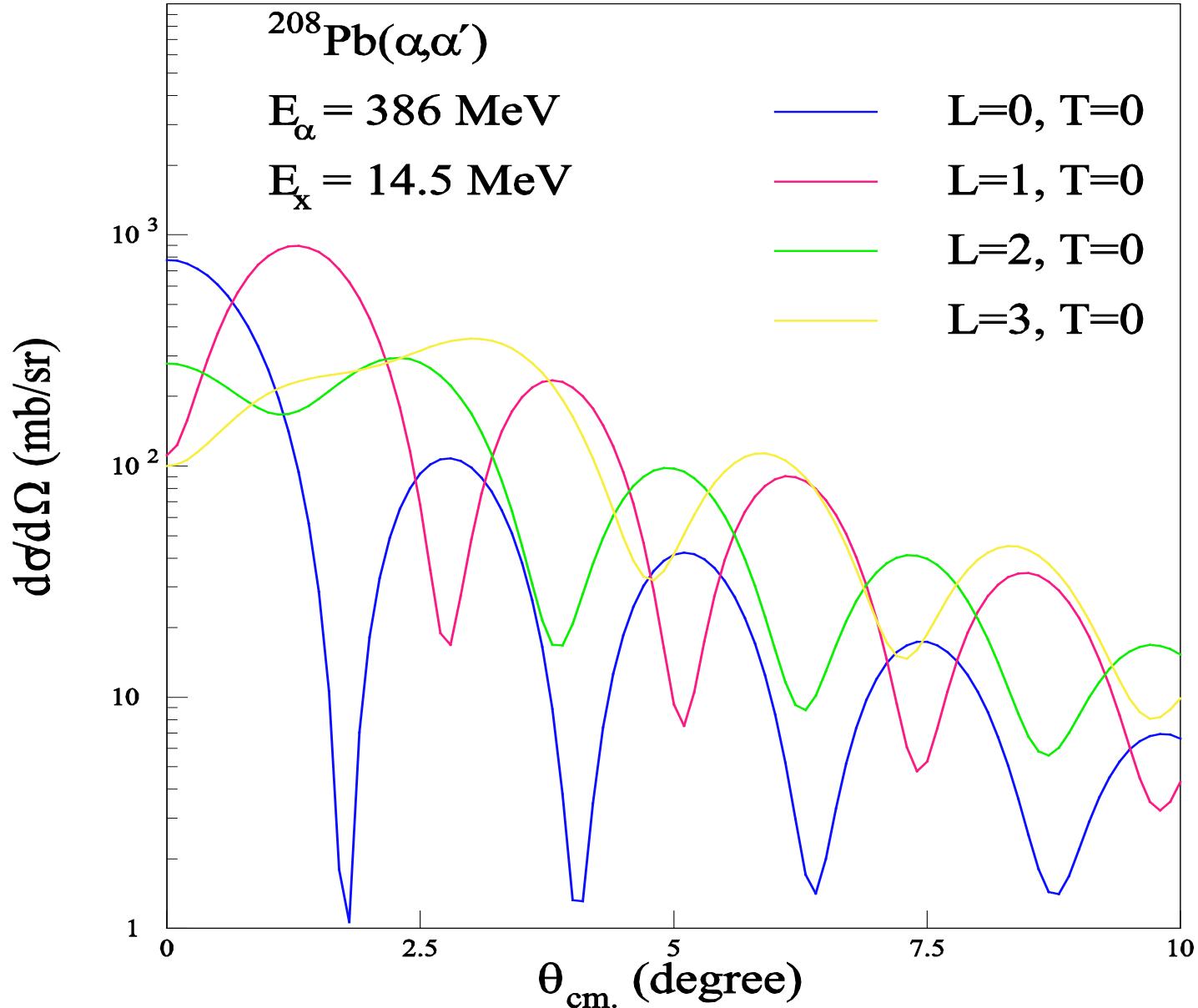
ISGMR, ISGDR \Rightarrow Incompressibility, symmetry energy

$$K_A = K_{vol} + K_{surf} A^{-1/3} + K_{sym} ((N-Z)/A)^2 + K_{Coul} Z^2 A^{-4/3}$$





Inelastic α scattering



ISGMR, ISGDR

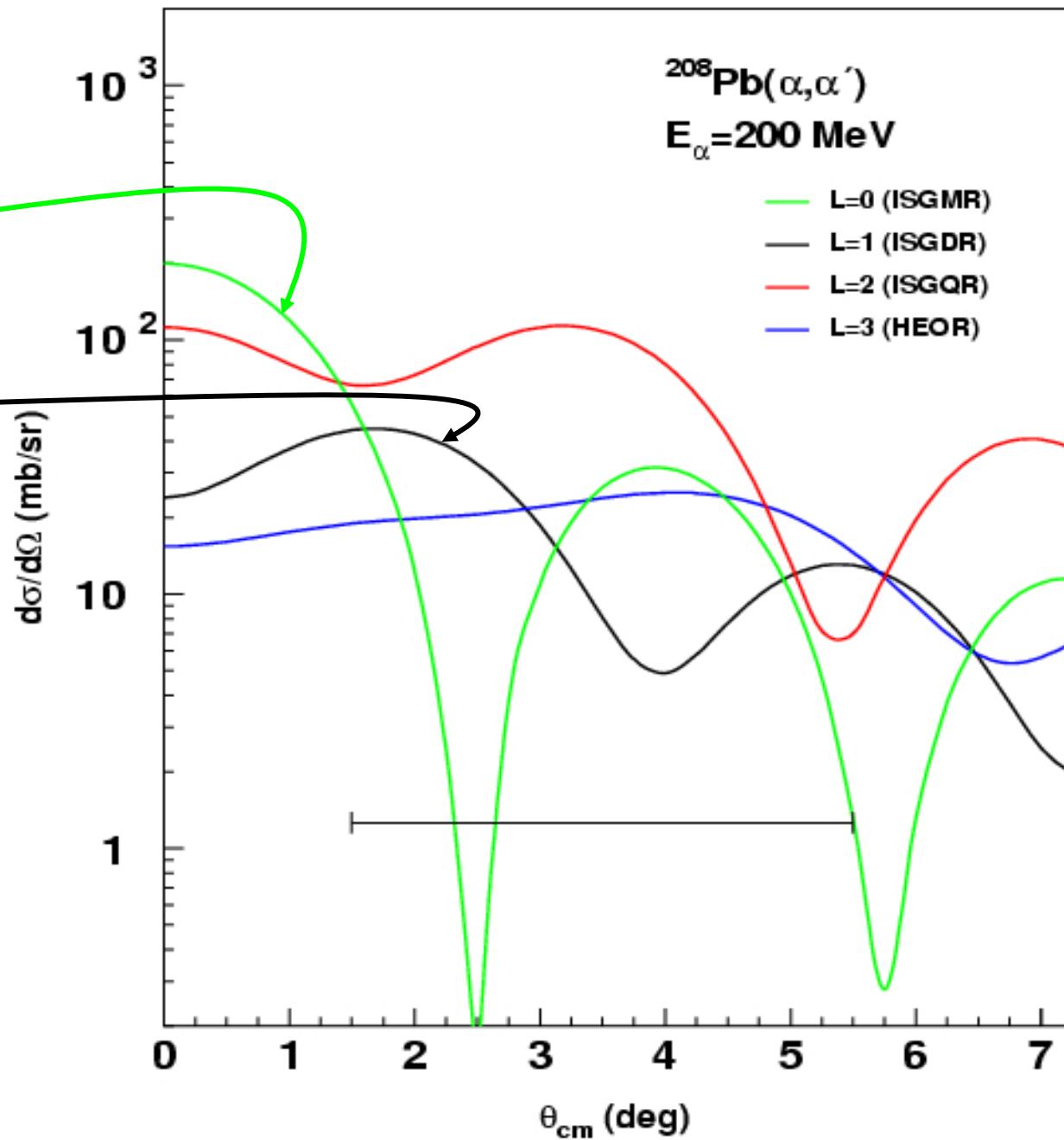
ISGQR, HEOR

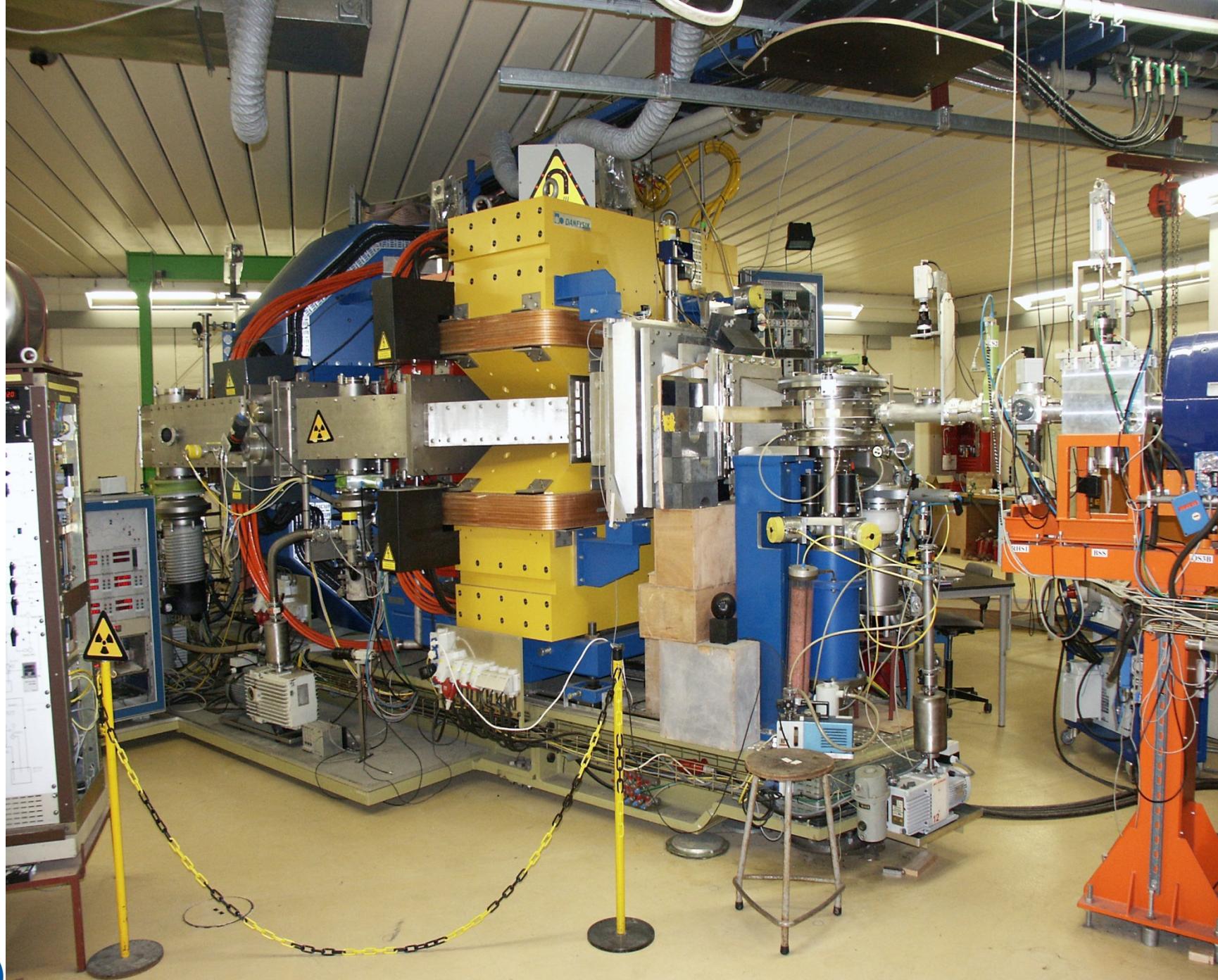
100 % EWSR

At $E_x = 14.5$
MeV

ISGMR $L = 0$

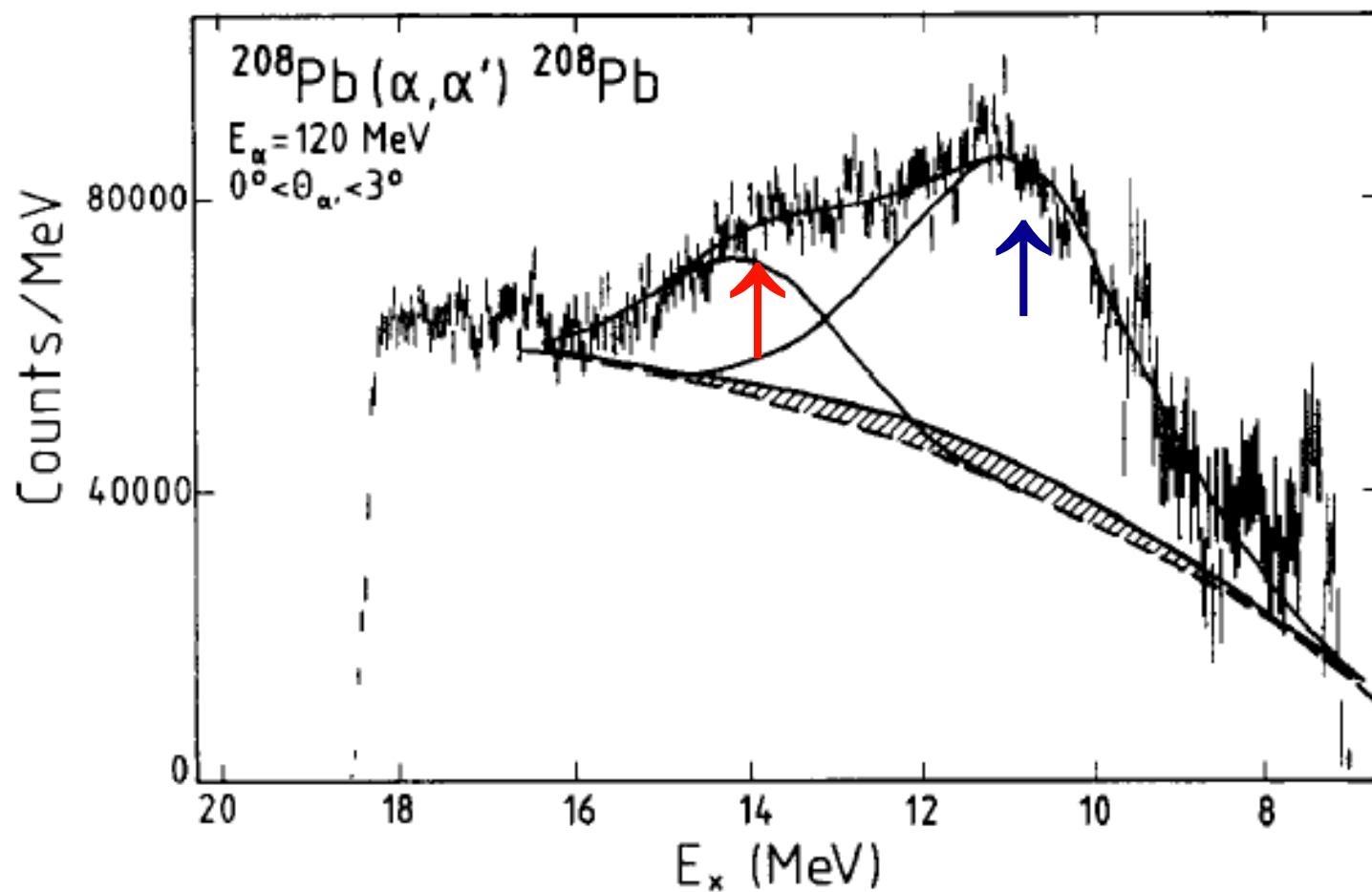
ISGDR $L = 1$





University of
Bergen

ISGQR at 10.9 MeV
ISGMR at 13.9 MeV



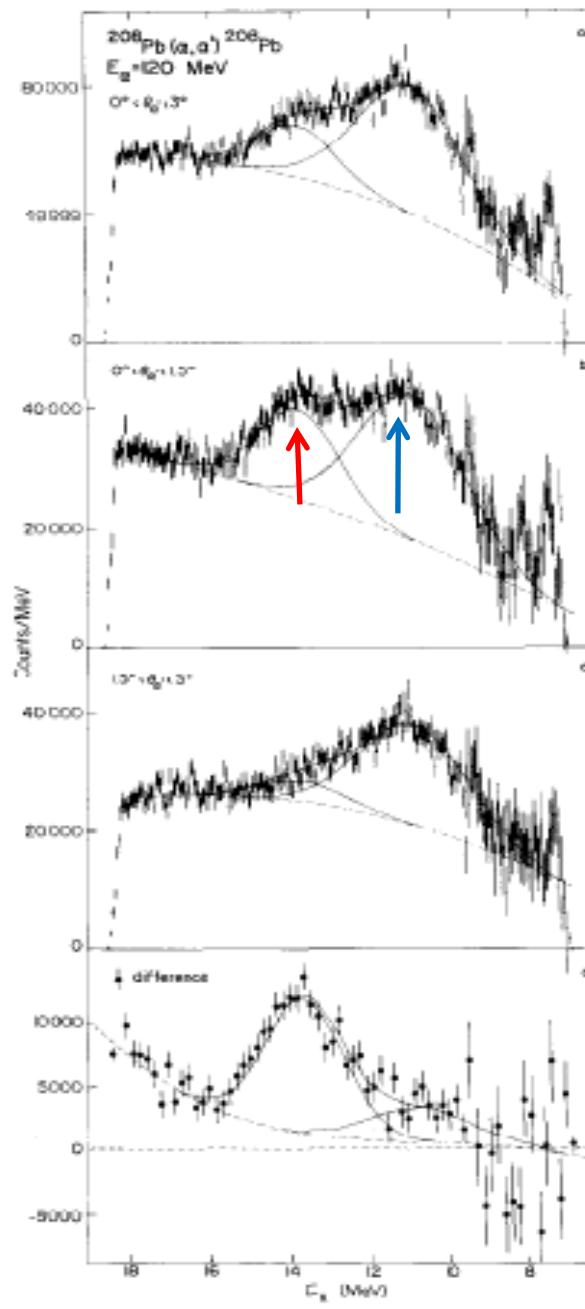
Difference of spectra

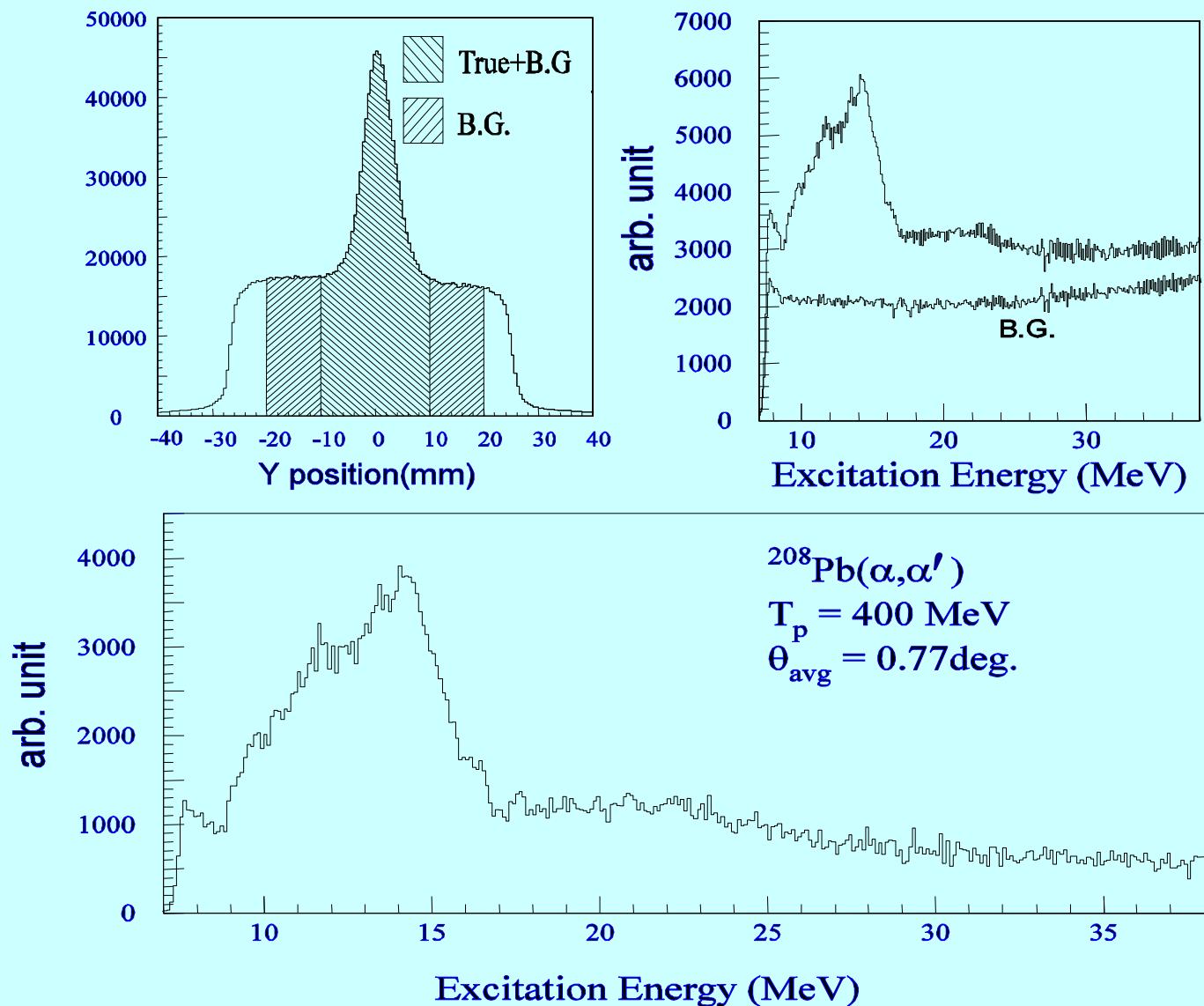
$$0^\circ < \theta_{\alpha'} < 3^\circ$$

$$0^\circ < \theta_{\alpha'} < 1.5^\circ$$

$$1.5^\circ < \theta_{\alpha'} < 3^\circ$$

Difference





Multipole decomposition analysis (MDA)

$$\left(\frac{d^2\sigma}{d\Omega dE}(\mathcal{G}_{c.m.}, E) \right)^{\text{exp.}} = \sum_L a_L(E) \left(\frac{d^2\sigma}{d\Omega dE}(\mathcal{G}_{c.m.}, E) \right)_L^{\text{calc.}}$$

$\left(\frac{d^2\sigma}{d\Omega dE}(\mathcal{G}_{c.m.}, E) \right)^{\text{exp.}}$: Experimental cross section

$\left(\frac{d^2\sigma}{d\Omega dE}(\mathcal{G}_{c.m.}, E) \right)_L^{\text{calc.}}$: DWBA cross section (unit cross section)

$a_L(E)$: EWSR fraction

- a. ISGR (L<15)+ IVGDR (through Coulomb excitation)
- b. DWBA formalism; single folding \Rightarrow transition potential

$$\delta U(r, E) = \int d\vec{r}' \delta\rho_L(\vec{r}', E) [V(|\vec{r} - \vec{r}'|, \rho_0(r')) + \rho_0(r') \frac{\partial V(|\vec{r} - \vec{r}'|, \rho(r'))}{\partial \rho_0(r')}]$$

$$U(r) = \int d\vec{r}' V(|\vec{r} - \vec{r}'|, \rho_0(r')) \rho_0(r')$$

Transition density

- ISGMR Satchler, Nucl. Phys. A472 (1987) 215

$$\delta\rho_0(r, E) = -\alpha_0 [3 + r \frac{d}{dr}] \rho_0(r)$$

$$\alpha_0^2 = \frac{2\pi\hbar^2}{mA < r^2 > E}$$

- ISGDR Harakeh & Dieperink, Phys. Rev. C23 (1981) 2329

$$\delta\rho_1(r, E) = -\frac{\beta_1}{R\sqrt{3}} [3r^2 \frac{d}{dr} + 10r - \frac{5}{3} < r^2 > \frac{d}{dr} + \varepsilon(r \frac{d^2}{dr^2} + 4 \frac{d}{dr})] \rho_0(r)$$

$$\beta_1^2 = \frac{6\pi\hbar^2}{mAE} \frac{R^2}{(11 < r^4 > - (25/3) < r^2 >^2 - 10\varepsilon < r^2 >)}$$

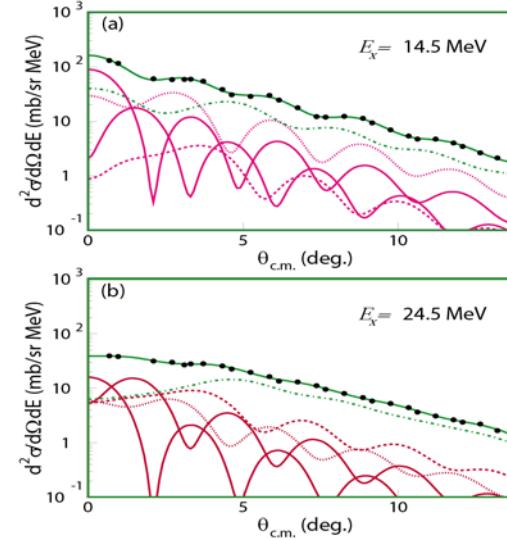
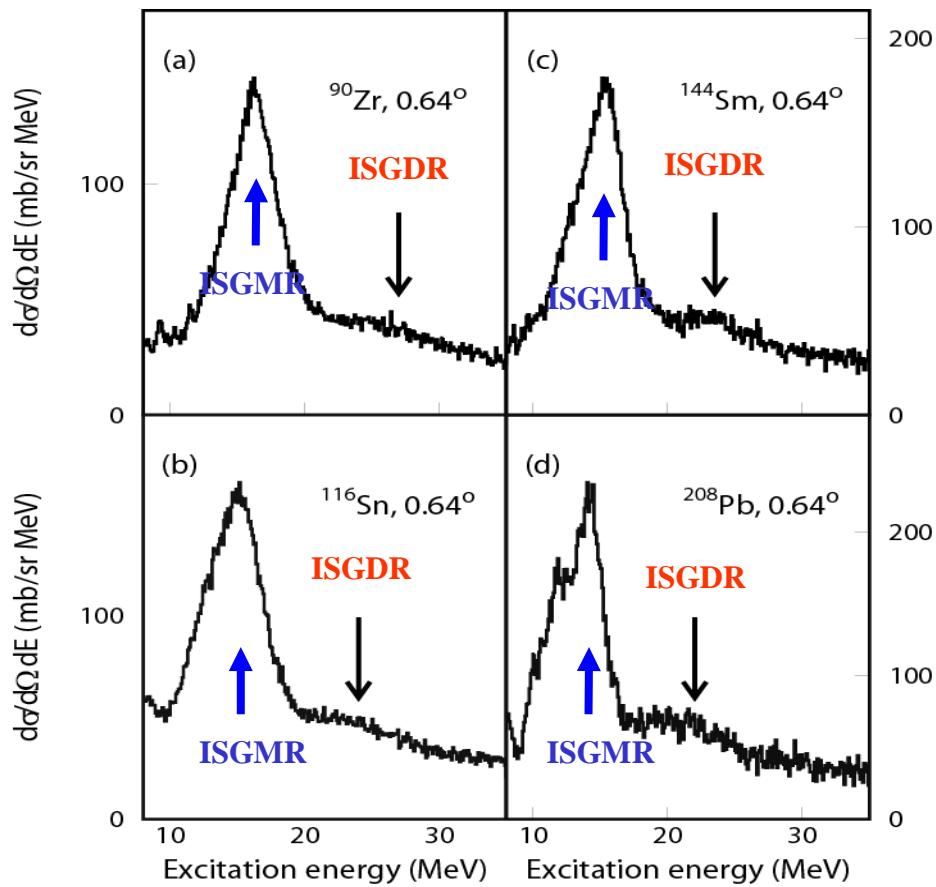
- Other modes Bohr-Mottelson (BM) model

$$\delta\rho_L(r, E) = -\delta_L \frac{d}{dr} \rho_0(r)$$

$$\delta_L^2 = (\beta_L c)^2 = \frac{L(2L+1)^2}{(L+2)^2} \frac{2\pi\hbar^2}{mAE} \frac{< r^{2L-2} >}{< r^{L-1} >^2}$$

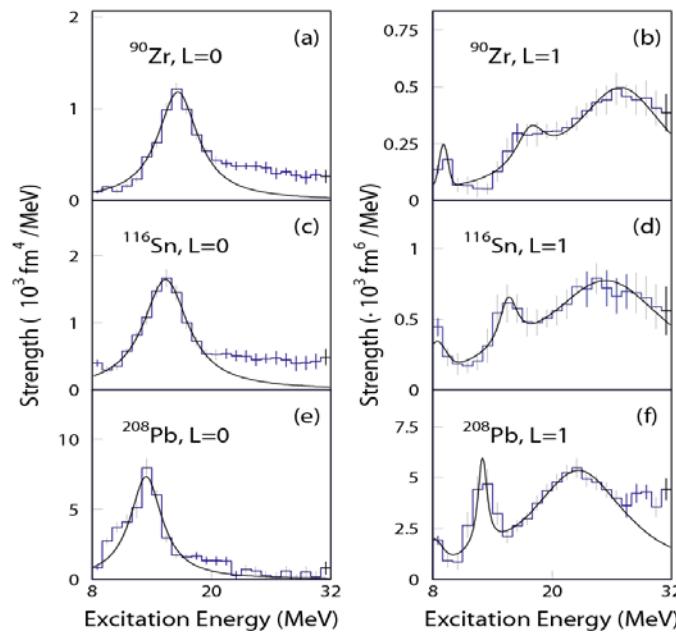
Uchida *et al.*,
 Phys. Lett. B557 (2003) 12
 Phys. Rev. C69 (2004) 051301

(α, α') spectra at 386 MeV



^{116}Sn

MDA results for L=0 and L=1



In HF+RPA calculations,

$$K_{nm} = \left[9\rho^2 \frac{d^2(E/A)}{d\rho^2} \right]_{\rho=\rho_0}$$

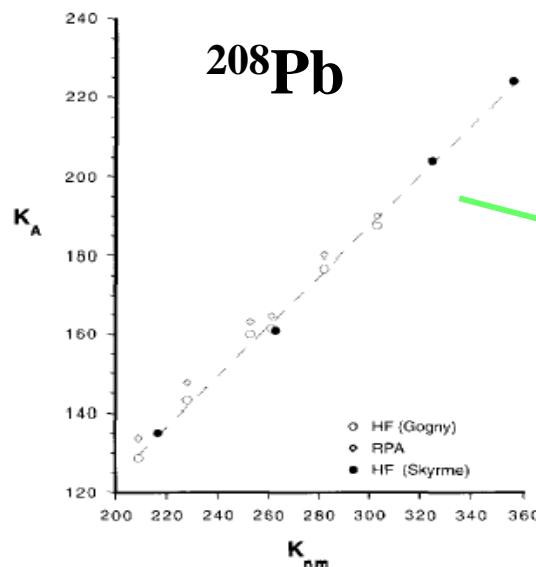
Nuclear matter

E/A : binding energy per nucleon

ρ : nuclear density

ρ_0 : nuclear density at saturation

K_A : incompressibility



K_A is obtained from excitation
energy of ISGMR & ISGDR

$$K_A = 0.64K_{nm} - 3.5$$

J.P. Blaizot, NPA591 (1995) 435

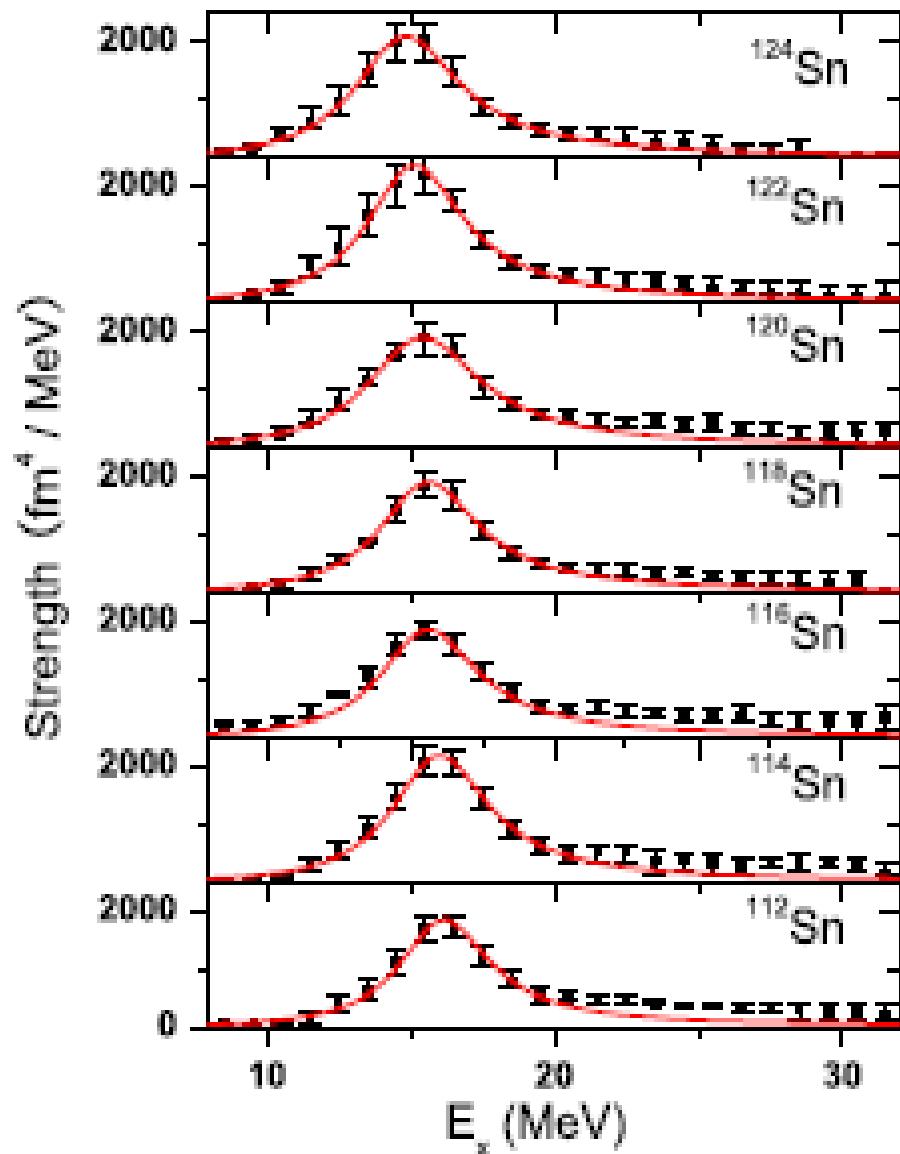
From GMR data on ^{208}Pb and ^{90}Zr ,

$$K_\infty = 240 \pm 10 \text{ MeV} \quad [\pm 20 \text{ MeV}]$$

[See, *e.g.*, G. Colò *et al.*, Phys. Rev. C 70 (2004) 024307]

This number is consistent
with both ISGMR and ISGDR Data
and
with non-relativistic and relativistic calculations

Isoscalar GMR strength distribution in Sn-isotopes obtained by Multipole Decomposition Analysis of singles spectra obtained in $^A\text{Sn}(\alpha, \alpha')$ measurements at incident energy 400 MeV and angles from 0° to 9°



$$K_A = K_{vol} + K_{surf} A^{-1/3} + K_{sym} ((N-Z)/A)^2 + K_{coul} Z^2 A^{-4/3}$$

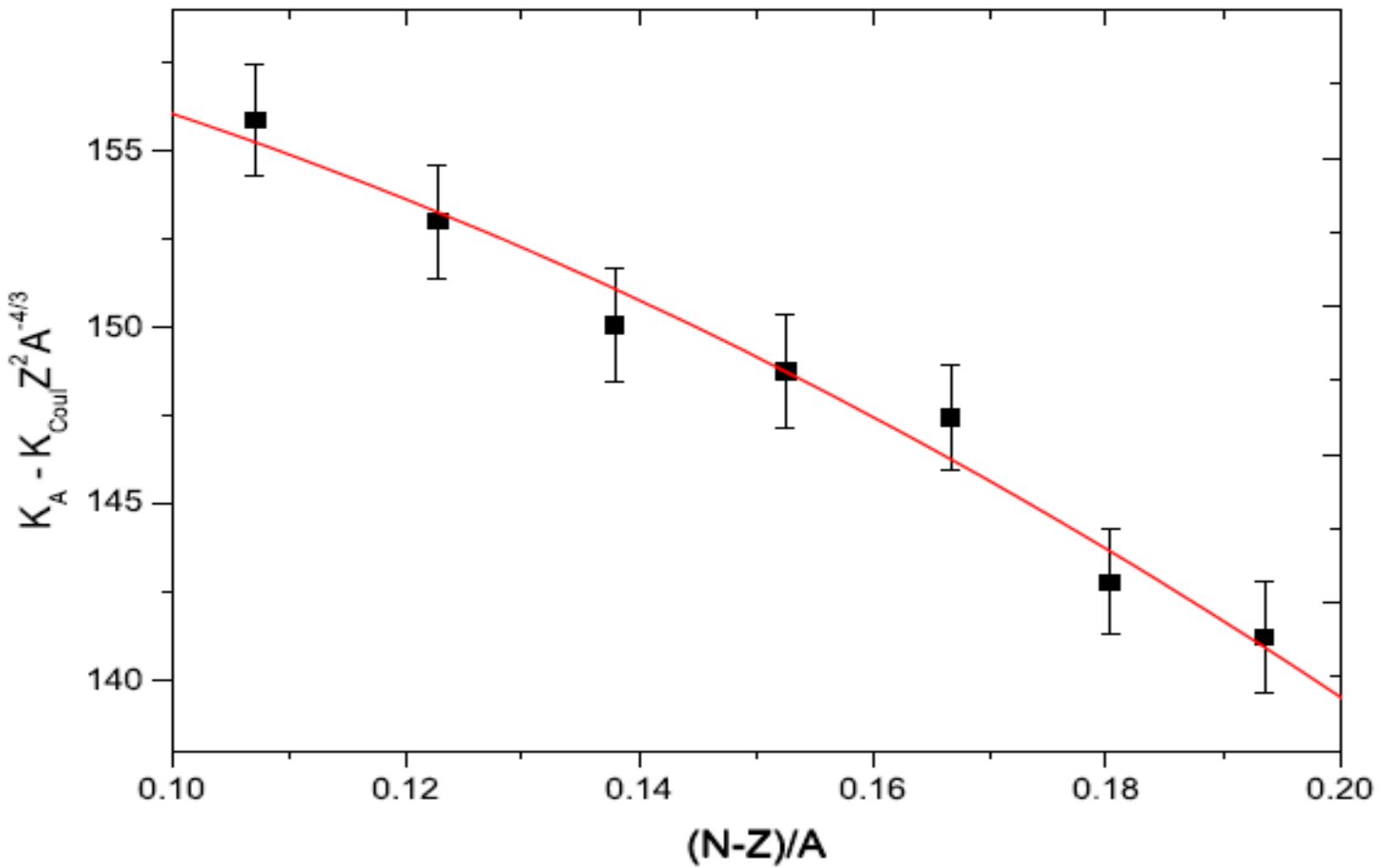
$$K_A \sim K_{vol} (1 + c A^{-1/3}) + K_\tau ((N - Z)/A)^2 + K_{Coul} Z^2 A^{-4/3}$$

$$K_A - K_{Coul} Z^2 A^{-4/3} \sim K_{vol} (1 + c A^{-1/3}) + K_\tau ((N - Z)/A)^2$$

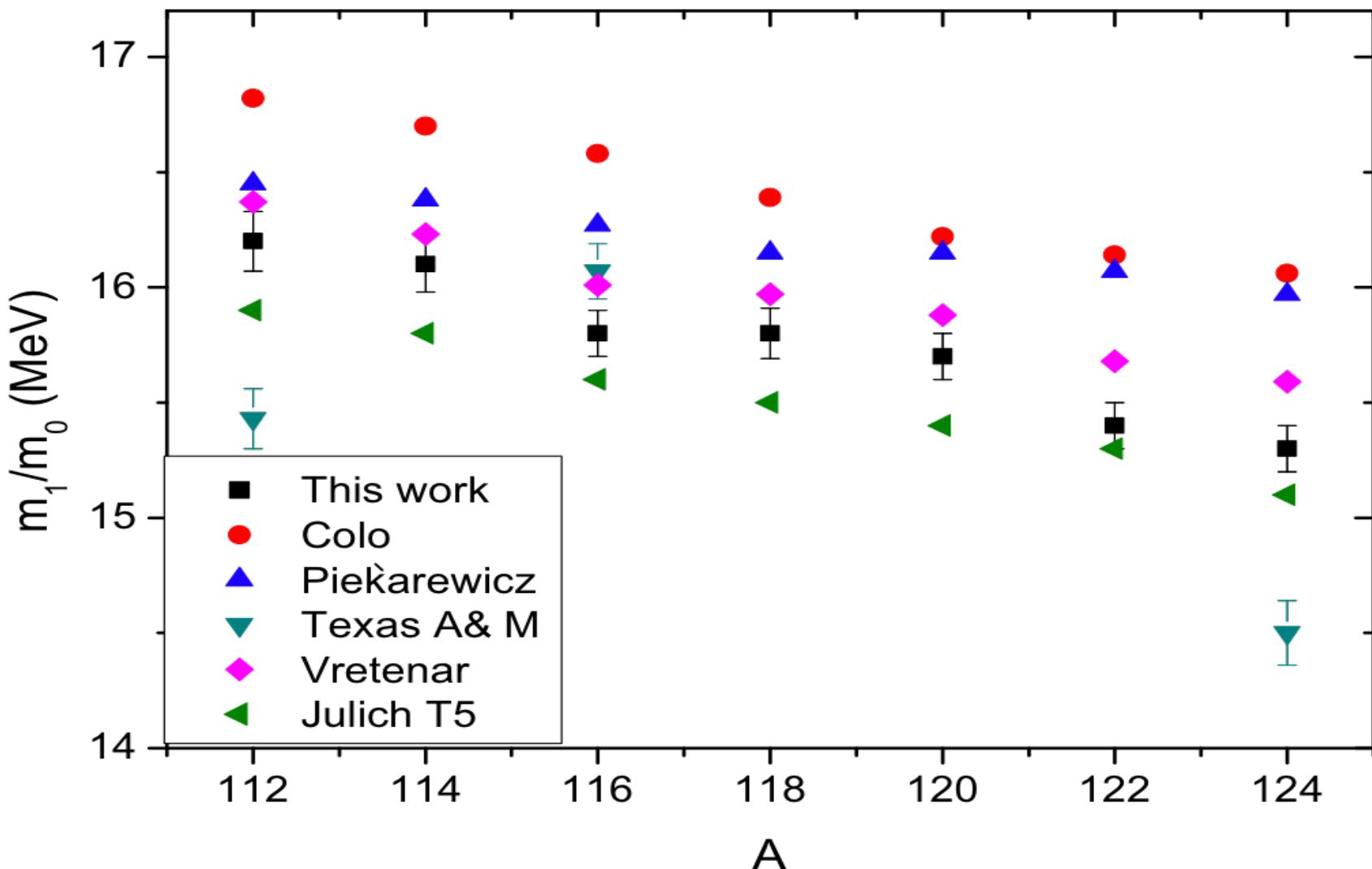
$$\sim \text{Constant} + K_\tau ((N - Z)/A)^2$$

$$K_{Coul} = -5.2 \text{ MeV (from Sagawa)}$$

$$(N - Z)/A \\ ^{112}\text{Sn} - ^{124}\text{Sn}: \text{ 0.107 - 0.194}$$



$$K_\tau = -550 \pm 100 \text{ MeV}$$



Colò *et al.*: Non-relativistic RPA (without pairing) reproduces ISGMR in ^{208}Pb and ^{90}Zr [$K_\infty = 240$ MeV]

Piekarewicz: Relativistic RPA (FSUGold model) reproduces g.s. observables and ISGMR in ^{208}Pb , ^{144}Sm and ^{90}Zr [$K_\infty = 230$ MeV]

**Vretenar: Relativistic mean field (DD-ME2: density-dependent mean-field effective interaction).
[$K_\infty = 240$ MeV].**

**Tselyaev *et al.*: Quasi-particle time-blocking approximation (QTBA) (T5 Skyrme interaction)
[$K_\infty = 202$ MeV?!!]**

Softness of Sn and Cd nuclei (compared to ^{208}Pb and ^{90}Zr) is still unresolved.

Spin-isospin excitations

Neutral (ν, ν') and charged (ν_e, e^-), (ν_e, e^+) currents

NC \Rightarrow Inelastic electron and proton scattering

\Rightarrow M0, M1, M2

CC \Rightarrow Charge-exchange reactions

Isovector charge-exchange modes

\Rightarrow GTR, IVSGMR, IVSGDR, etc.

Importance for nuclear astrophysics,

ν -physics, 2β -decay, n-skin thickness, etc.

(p, n), (${}^3\text{He}, t$) {GT $^-$ }; (n, p), ($d, {}^2\text{He}$) & ($t, {}^3\text{He}$) {GT $^+$ }

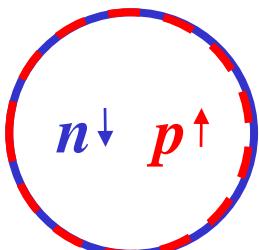
Nucleus \longrightarrow Many-body system with a finite size

Vibrations \longrightarrow Multipole expansion with r, Y_{lm}, τ, σ

$\Delta S=0, \Delta T=0$ $\Delta S=0, \Delta T=1$ $\Delta S=0, \Delta T=1$ $\Delta S=1, \Delta T=1$ $\Delta S=1, \Delta T=1$

L=0: Monopole	ISGMR $r^2 Y_0$	IAS τY_0	IVGMR $\tau r^2 Y_0$	GTR $\tau \sigma Y_0$	IVSGMR $\tau \sigma r^2 Y_0$
L=1: Dipole	ISGDR $(r^3 - 5/3 \langle r^2 \rangle r) Y_1$		IVGDR $\tau r Y_1$		IVSGDR $\tau \sigma r Y_1$
L=2: Quadrupole	ISGQR $r^2 Y_2$		IVGQR $\tau r^2 Y_2$		IVSGQR $\tau \sigma r^2 Y_2$
L=3: Octupole	LEOR, HEOR $r^3 Y_3$				

Spin-isospin excitations



$\Delta L=0$ $\Delta S=1$ $\Delta T=1$
GTR

- Gamow-Teller transitions;
Isospin ($\Delta T=1$)
Spin ($\Delta S=1$)

Advantages

- Cross section peaks at 0° ($\Delta L=0$)
- Strong excitation of GT states at $E/A=100-500$ MeV/u

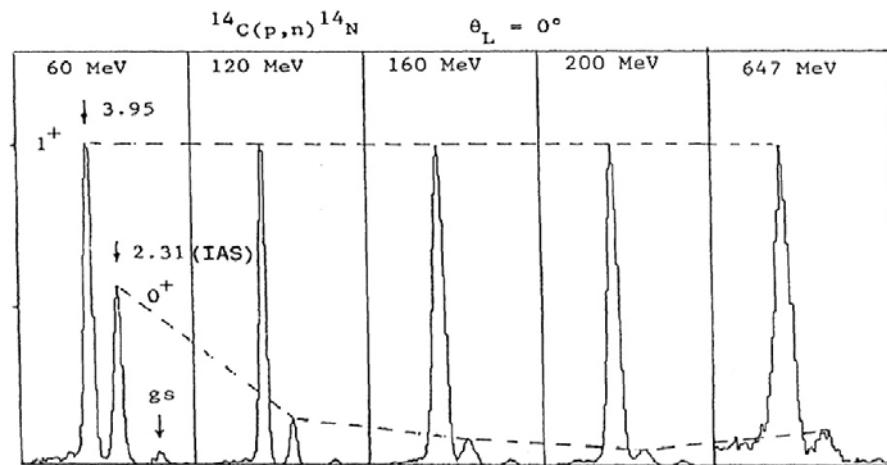
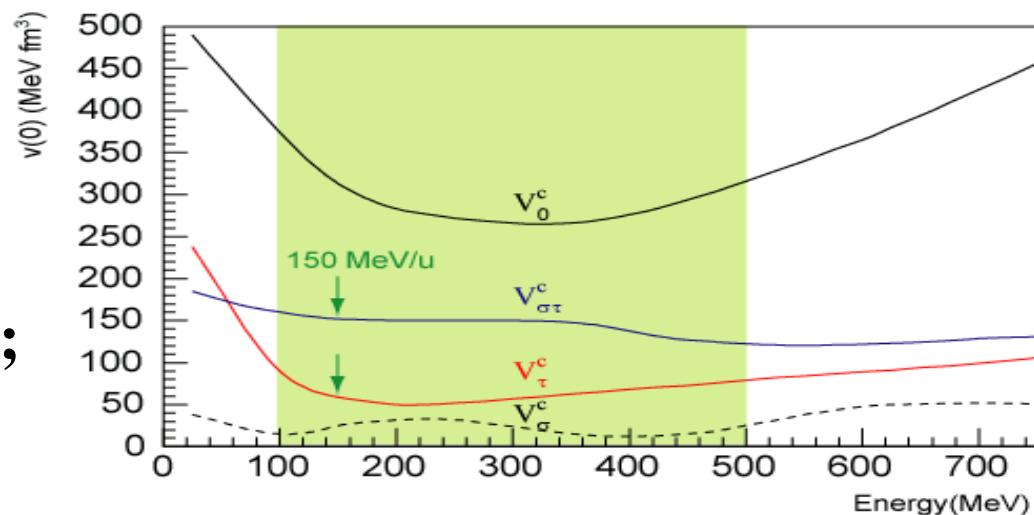
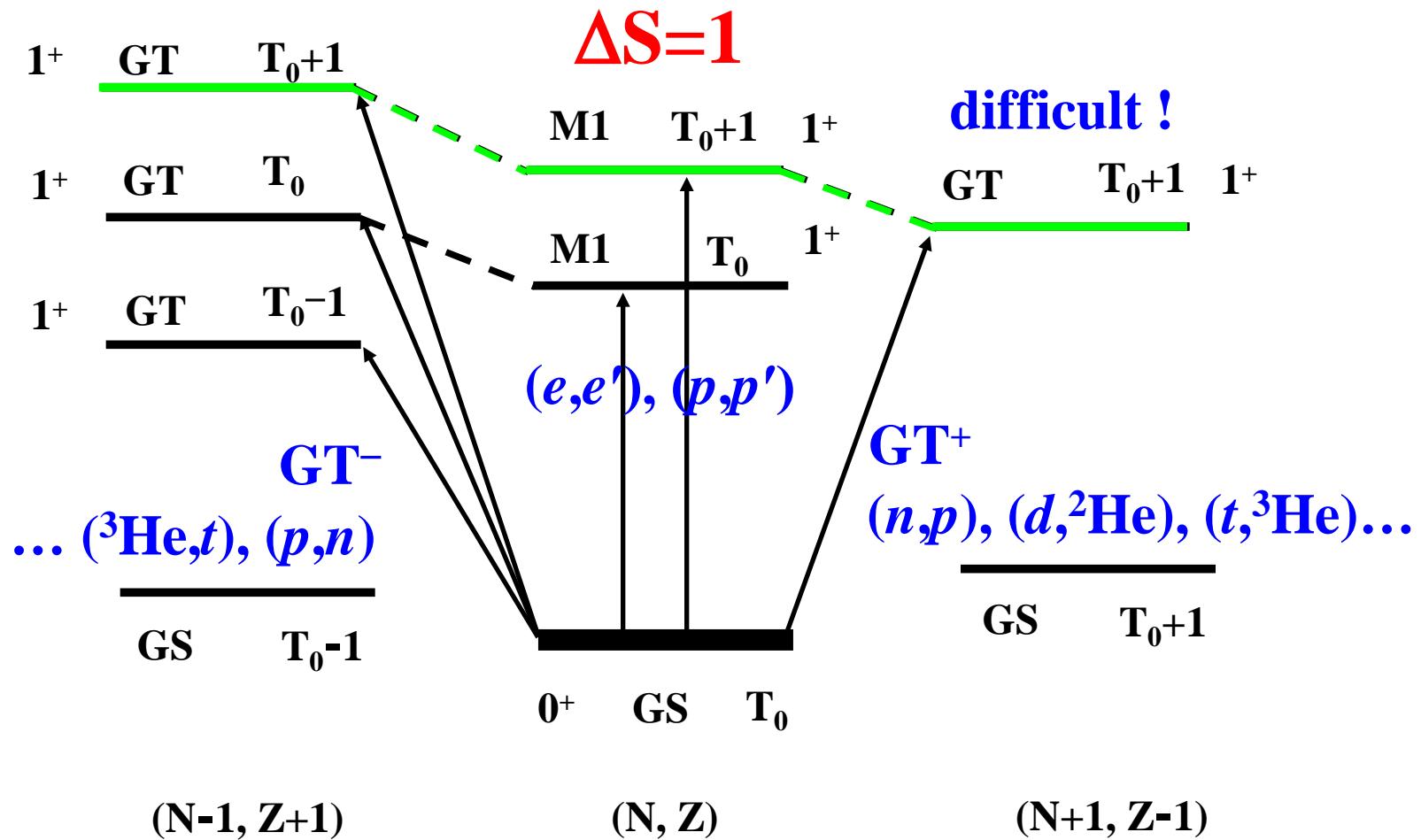


FIG. 4. Zero-degree cross-section spectra for the $^{14}\text{C}(p,n)^{14}\text{N}$ reactions at the indicated bombarding energies. The spectra have been arbitrarily normalized. From Gaarde (1985) and Ra-
paport (1989).

Spin-flip & GT transitions



The (${}^3\text{He},t$) reaction at 0 degree

- Cross sections at $E({}^3\text{He})=450 \text{ MeV}$, $q=0$ for (${}^3\text{He},t$) reactions

$$\frac{d\sigma}{d\Omega} = \frac{\mu_i \mu_f}{(\pi \hbar^2)^2} \left(\frac{k_f}{k_i} \right) (N_{\tau}^D |J_{\tau}|^2 B(F) + N_{\sigma\tau}^D |J_{\sigma\tau}|^2 B(GT))$$

T. N. Taddeucci *et al.*, Nucl. Phys. A469, 125 (1987)

I. Bergqvist *et al.*, Nucl. Phys. A469, 648 (1987)

- Neutrino absorption cross sections

$$\sigma = \frac{1}{\pi \hbar^4 c^3} [G_V^2 B(F) + G_A^2 B(GT)] \times F(Z, E_e) p_e E_e$$

$F(Z, E_e)$ is the relativistic Coulomb barrier factor

Importance of charge-exchange reactions at intermediate energies

IUCF

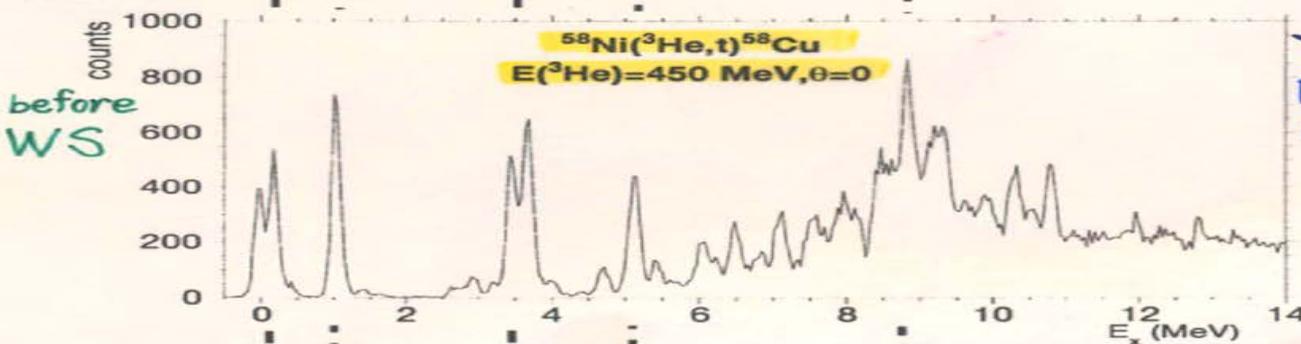
Evolution of Resolution
in Charge-Exchange Reactions
at Intermediate Energies

$^{58}\text{Ni}(p,n)$
 $E_p = 160\text{ MeV}$, 0-deg., IUCF

J. Rapaport et al.,
Nucl. Phys. A410 (1983) 371.

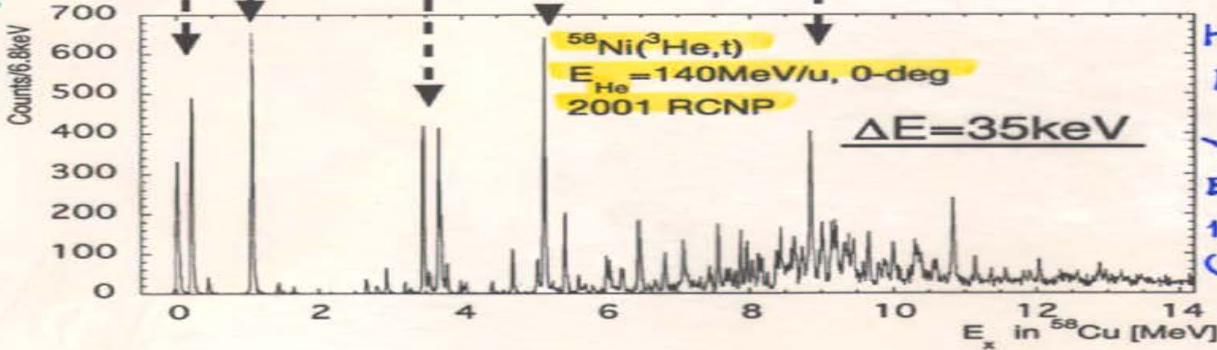
$\Delta E = \sim 400\text{ keV}$

RCNP



Y. Fujita et al.
Phys. Lett. B365
(1996) 29

WS



H. Fujita et al.
PhD thesis

Y. Fujita et al.
Euro. Phys. J. A
13 (2002) 411
($E_x \leq 8\text{ MeV}$)

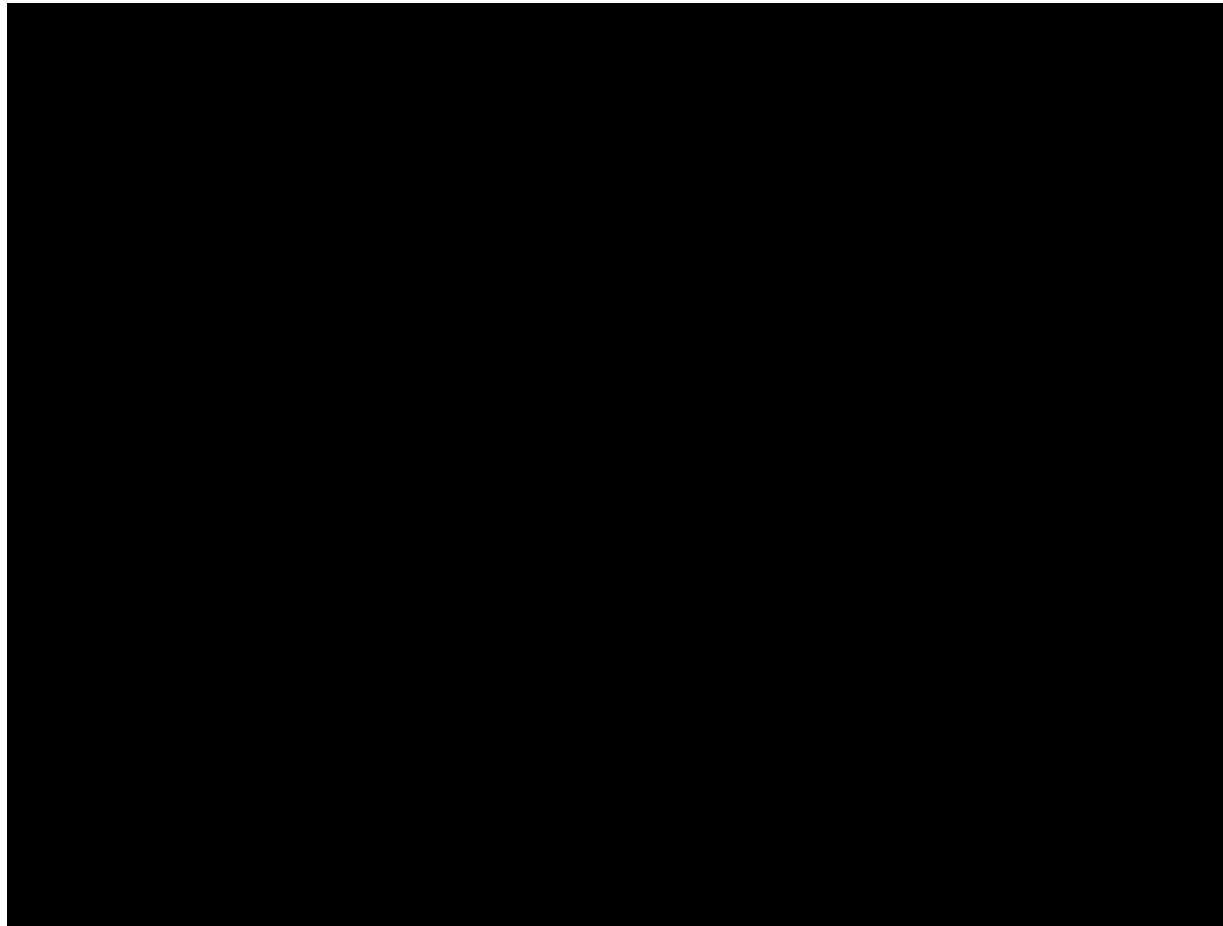
Determination of GT⁺ Strength and its Astrophysical Implications

In supernova explosions, electron capture (EC) on *fp*-shell nuclei plays a dominant role during the last few days of a heavy star with $M > 10 M_{\odot}$

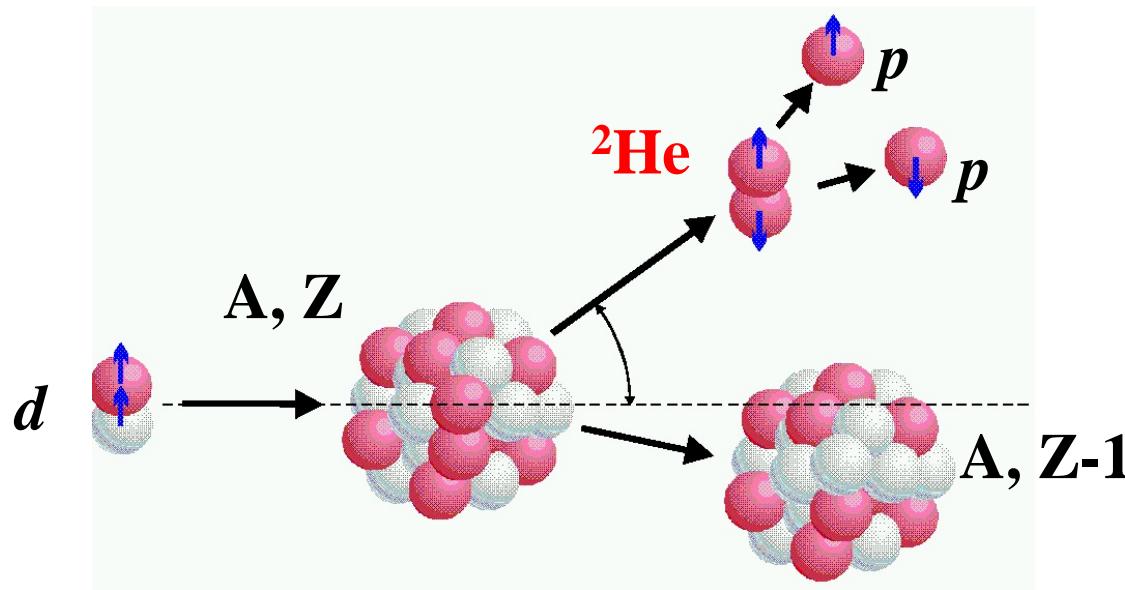
Presupernova stage; deleptonization \Rightarrow core collapse \Rightarrow subsequent type IIa Supernova (SN) explosion

H.A. Bethe *et al.*, Nucl. Phys. A324 (1979) 487

Supernova Simulatie



Exclusive excitations $\Delta S = \Delta T = 1$: ($d, {}^2\text{He}$)

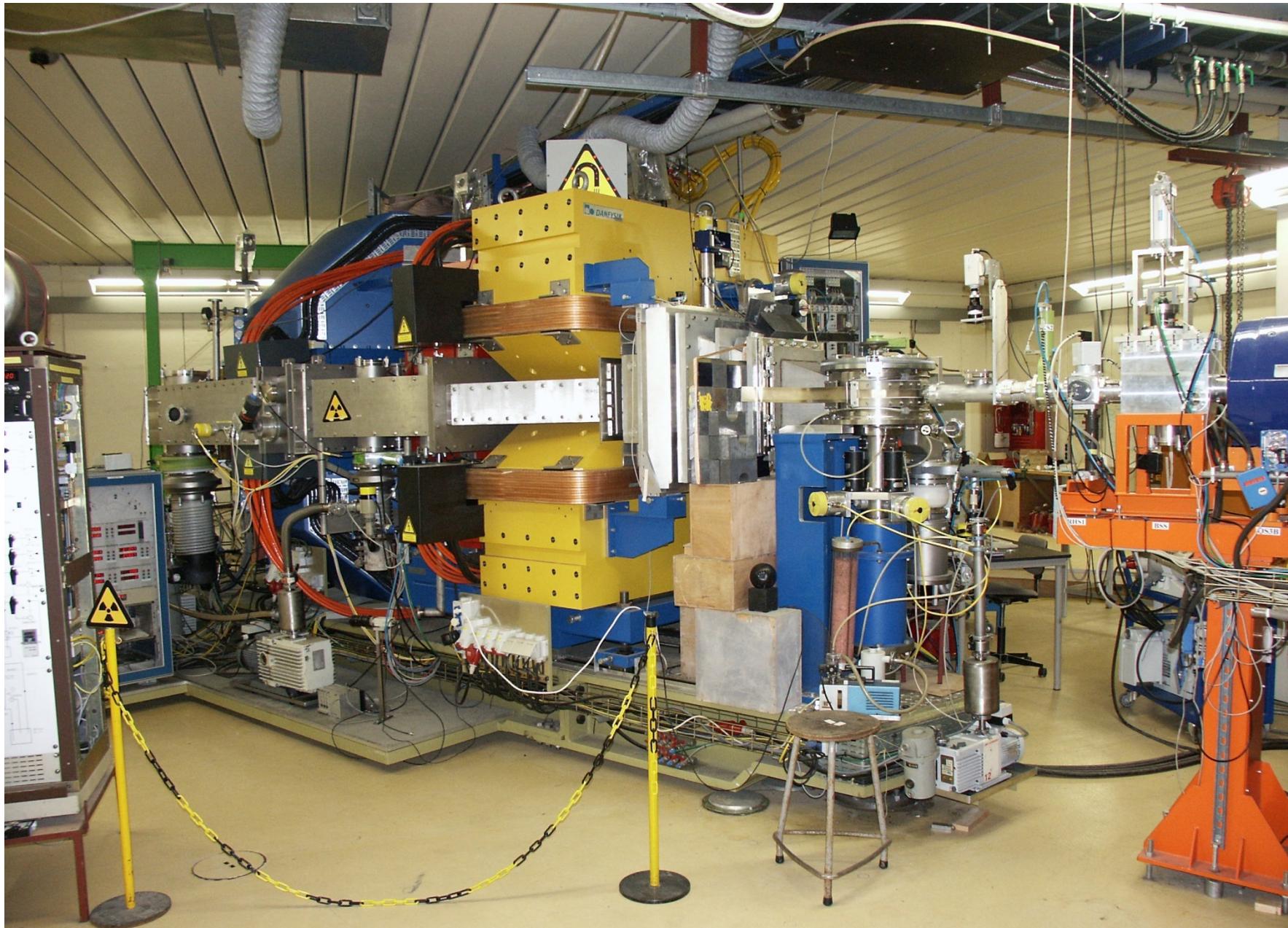


${}^3\text{S}_1$ deuteron $\Rightarrow {}^1\text{S}_0$ di-proton (${}^2\text{He}$)

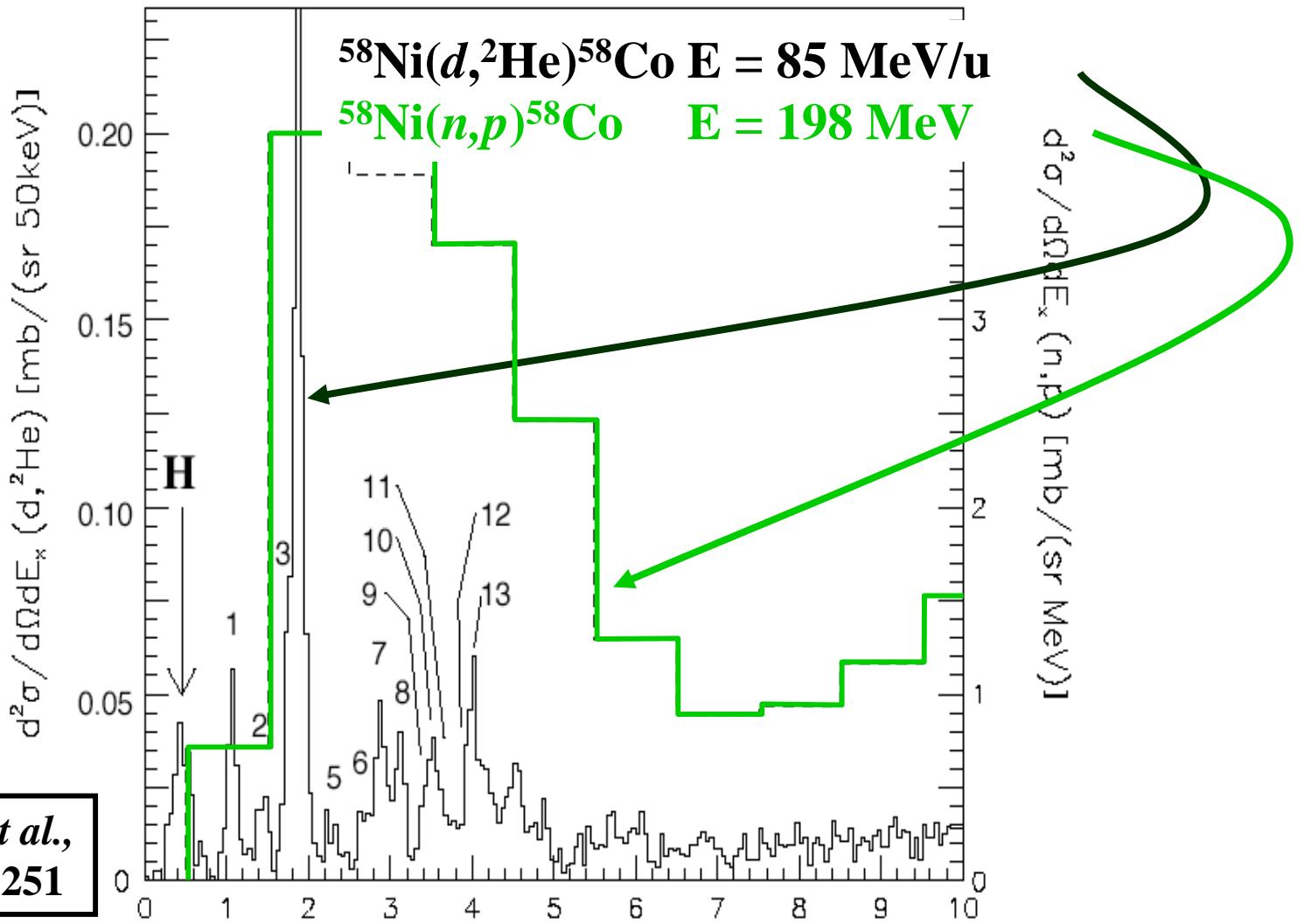
${}^1\text{S}_0$ dominates if (relative) 2-proton kinetic energy $\varepsilon < 1$ MeV

(n, p)-type probe with exclusive $\Delta S = 1$ character (GT⁺ transitions)

But near 0°, tremendous background from d -breakup

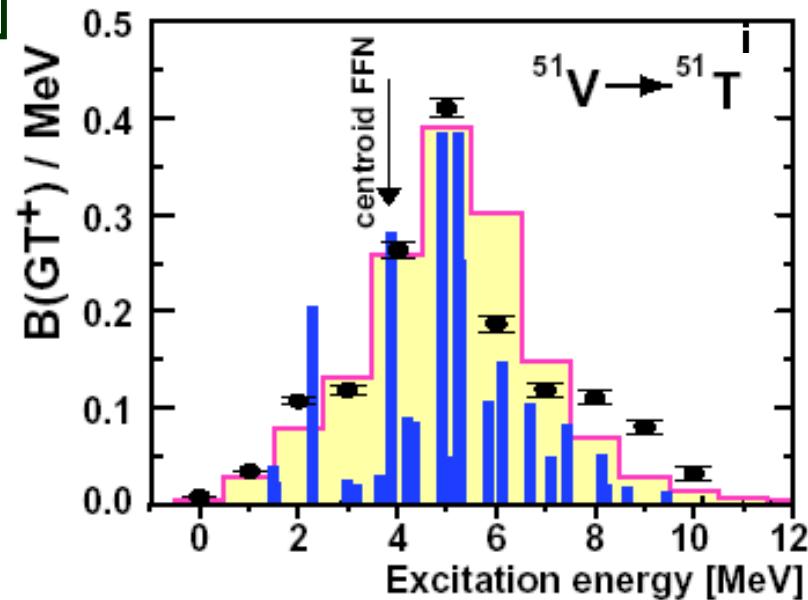
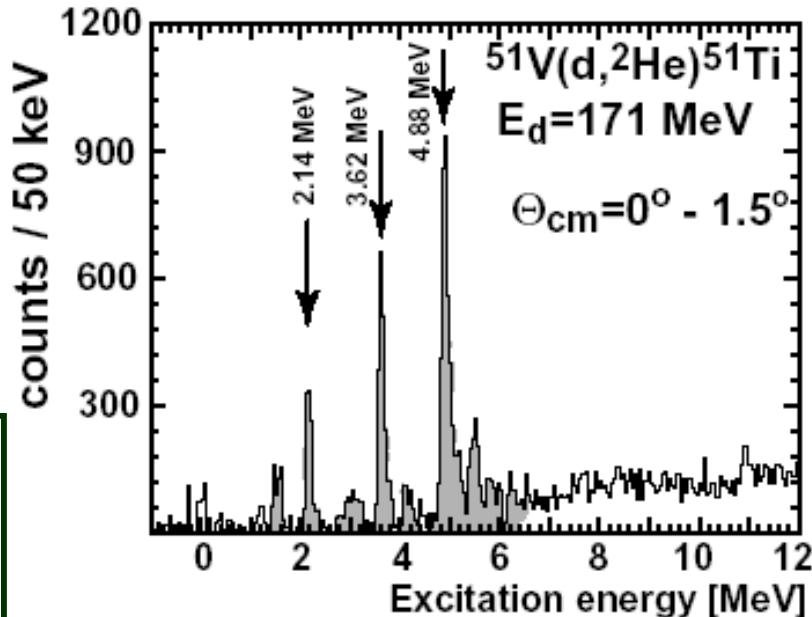


$(d,^2\text{He})$ as GT⁺ probe in *fp*-shell nuclei

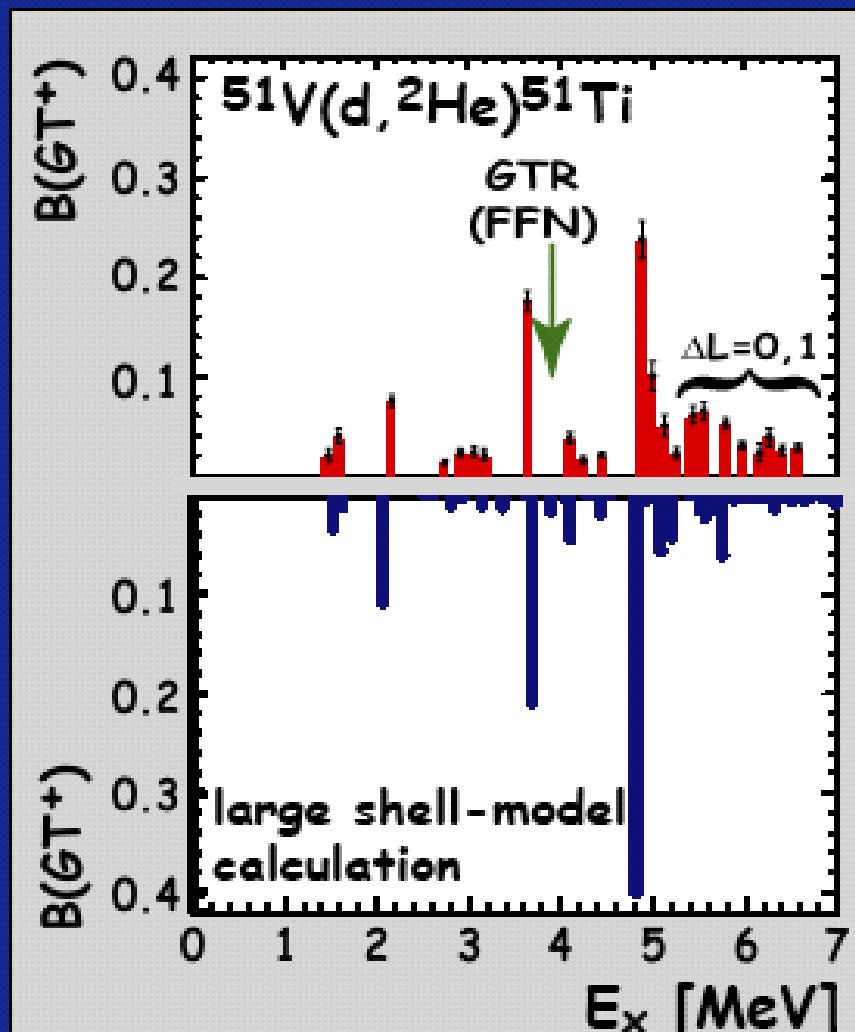


M. Hagemann *et al.*,
PLB 579 (2004) 251

C. Bäumer *et al.*,
PRC **68**, 031303(R)
(2003)



$^{51}\text{V}(d,^2\text{He})$: Comparison with shell-model calculations



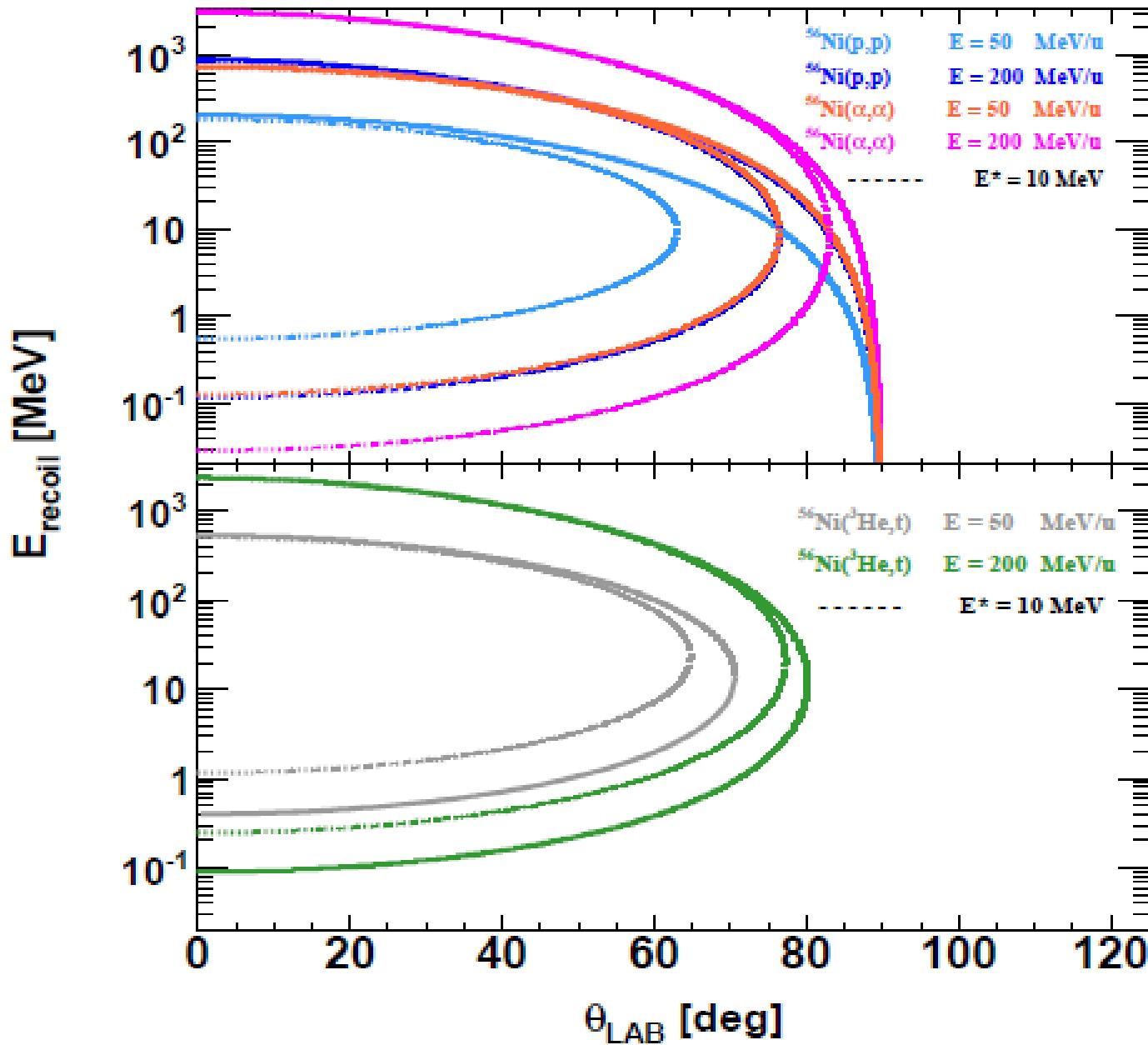
← Experimental result

← Full *fp*-shell model
calculations
quenching factor $(0.74)^2$
G. Martínez-Pinedo,
K. Langanke

Outlook

Radioactive ion beams will be available at energies where it will be possible to study ISGMR, ISGDR and GT transitions (RIKEN, NSCL, FAIR, SPIRAL2)

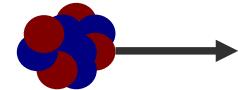
- Determine GT strength in unstable *sd* & *fp* shell nuclei
- Measure ISGMR and ISGDR in extended isotope chain
- Unravel the nature of the pygmy dipole resonance
- Use IV(S)GDR as tool to determine n-skin [IV(S)GDR]
- Exotic excitations such as double GT (SHARAQ)



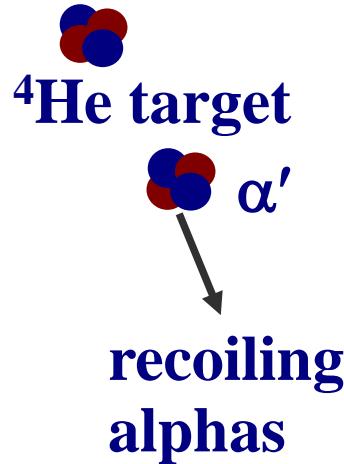
Nuclear structure studies with reactions in inverse kinematics

- Possible at FAIR, RIKEN and NSCL
(beam energies of 50-100 MeV/u are needed!)

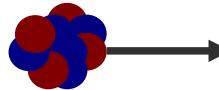
(α, α')



heavy projectile



heavy ejectile



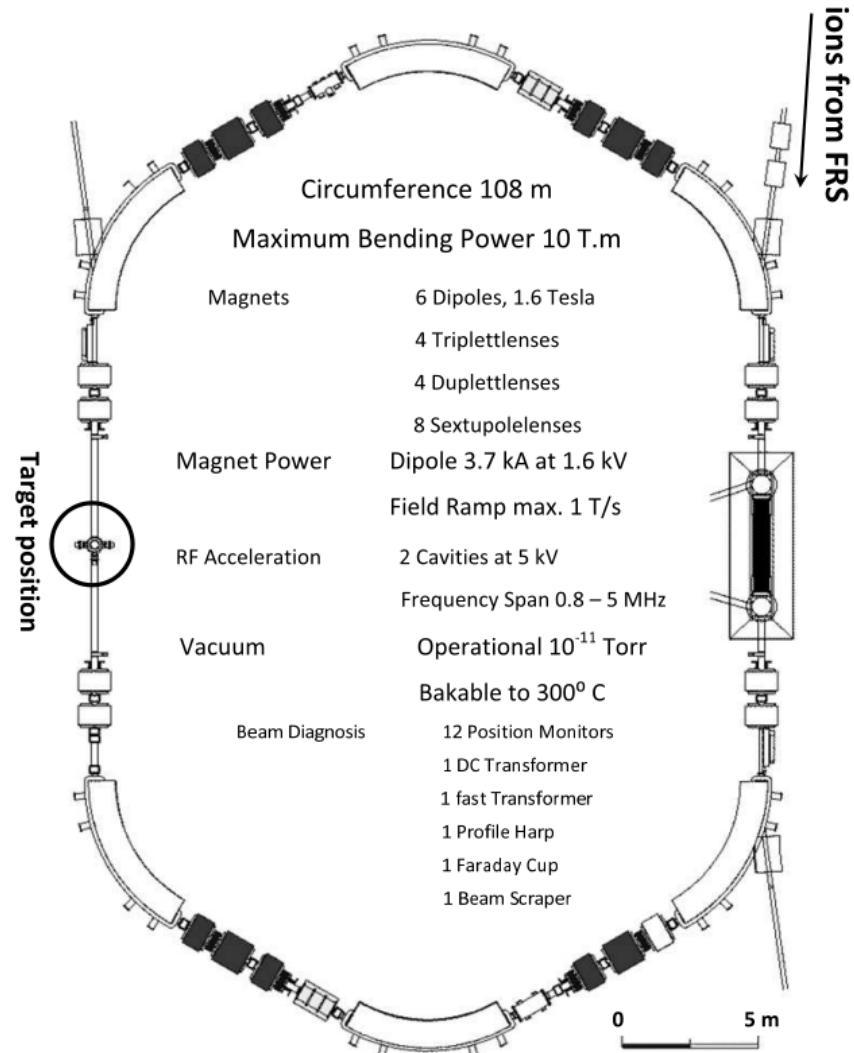
Approach:
measure the recoiling alphas

Inconvenience:
difficulty to detect the low-energy alphas

Storage Ring

Experimental storage ring at GSI
Luminosity: $10^{26} - 10^{27} \text{ cm}^{-2}\text{s}^{-1}$

EPJ Web of Conferences 66, 03093 (2014)



Detection system @ FAIR

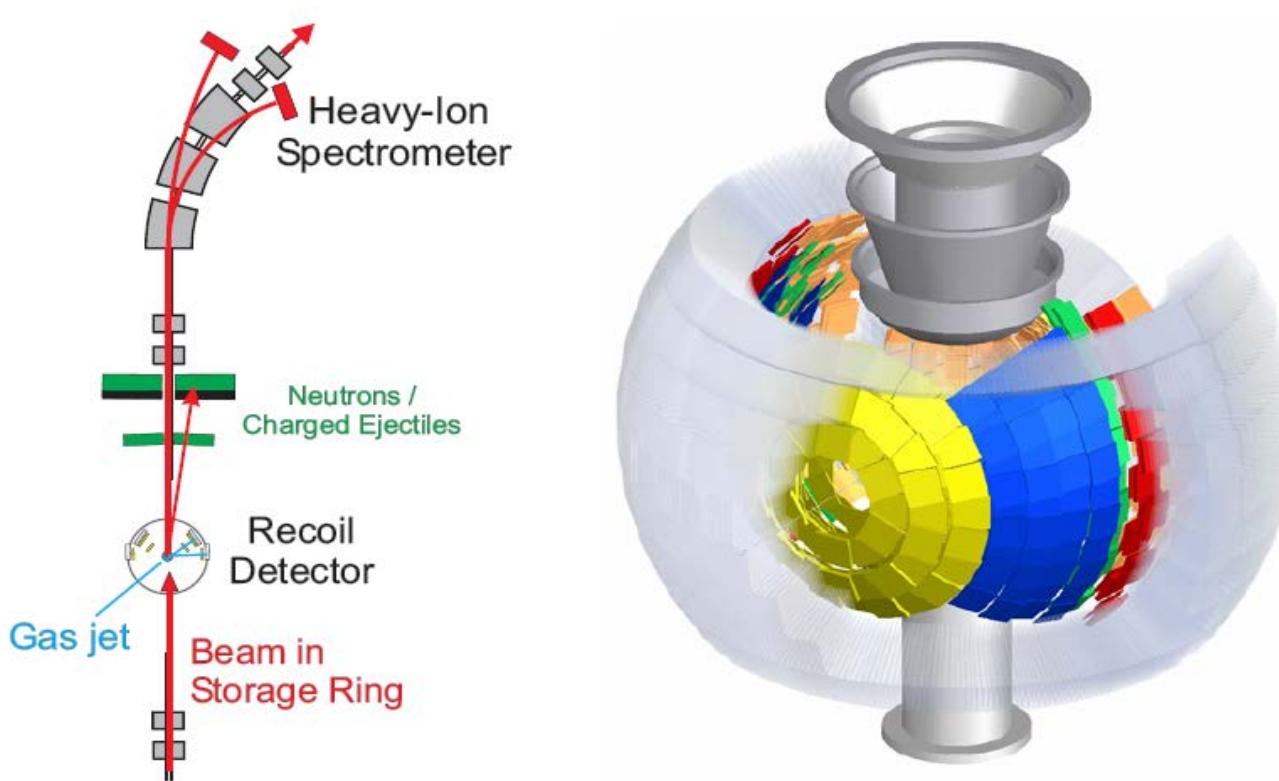
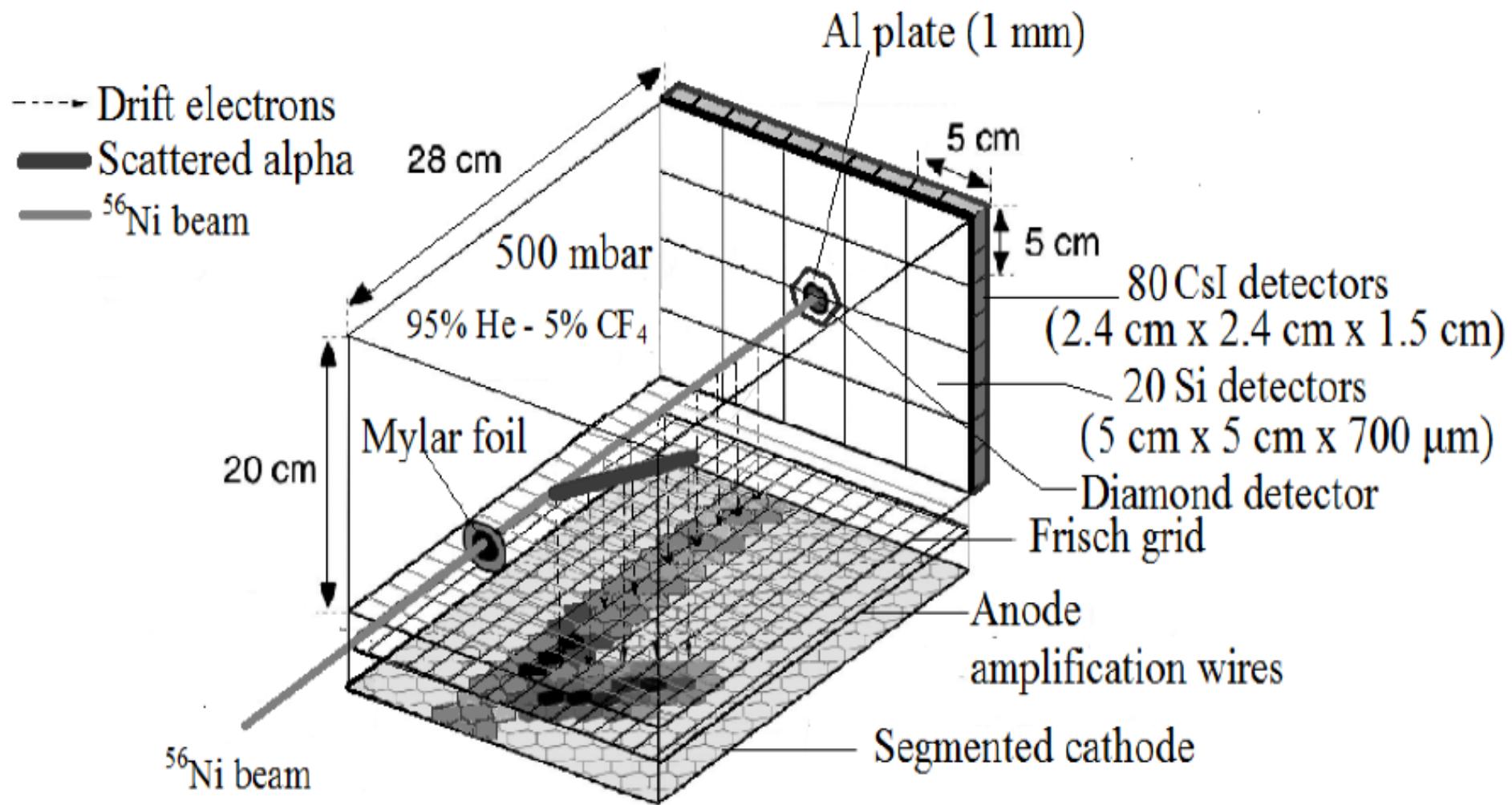


Figure 1: Schematic view of the EXL detection systems. Left: Set-up built into the NESR storage ring. Right: Target-recoil detector surrounding the gas-jet target.

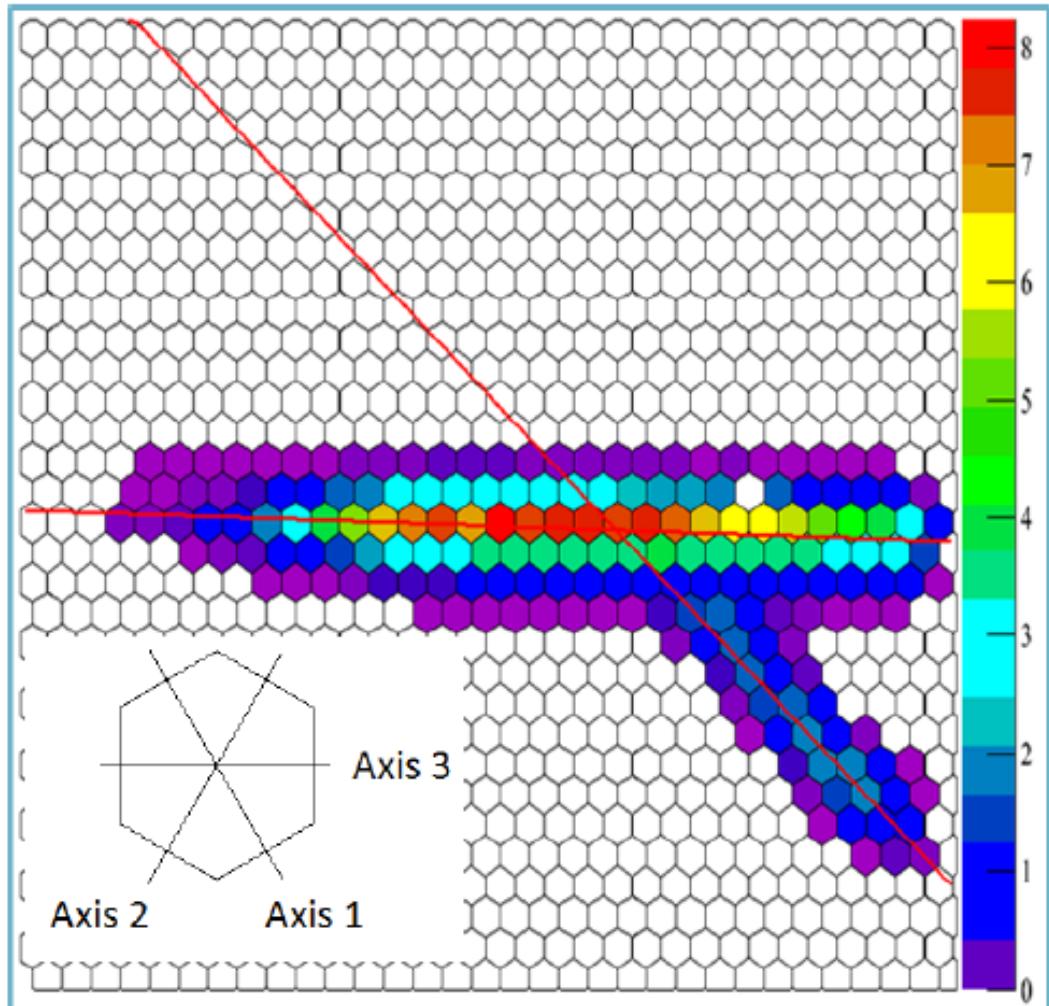
Use of EXL recoil detector prototype has been successfully tested [Nasser Kalantar talk on Tuesday afternoon]

Schematic view of MAYA active target detector



Marine Vandebrouck talk on Tuesday afternoon

Recoil Track



- Recoil alpha particle track due to inelastic scattering with ^{56}Ni .
- Background events can be separated from the range of the recoil particles and also from the magnitude of charges induced on the pads.

- Pygmy Dipole Resonance (PDR): Tuesday morning
- IVGMR: Tuesday afternoon (Remco Zegers)
- Anti-analogue GDR and n-skin:
Tuesday afternoon (Attila Krasznahorkay)
- Hot IVGDR: Wednesday morning

Etc.

*Thank you for your
attention*