Canada's National Laboratory for Particle and Nuclear Physics Laboratoire national canadien pour la recherche en physique nucléaire et en physique des particules



Electromagnetic strengths in ab-initio approaches

Sonia Bacca | TRIUMF

The 5th international conference on "COLLECTIVE MOTION IN NUCLEI UNDER EXTREME CONDITIONS









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Electromagnetic Reactions





"Ab-initio" methods

- Start from neutrons and protons as building blocks (centre of mass coordinates, spins, isospins)
- Solve the non-relativistic quantum mechanical problem of A-interacting nucleons

 $H|\psi_i\rangle = E_i|\psi_i\rangle$

 $H = T + V_{NN}(\Lambda) + V_{3N}(\Lambda) + \dots$



• Find numerical solutions with no approximations or controllable approximations (error bars)



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 Calculate low-energy observables and compare with experiment to test nuclear forces and provide predictions for future experiments or quantity that cannot be measured



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Dipole strength functions



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Dipole strength functions



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Dipole strength functions



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Electric dipole polarizability



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Electric dipole polarizability



Low-energy part of response dominates

Very interesting for neutron-rich nuclei:

soft modes at low energy enhance the polarizability



Experimental status

Stable Nuclei





From photoabsorption experiments



Unstable Nuclei



From Coulomb excitation experiments



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Experimental status

Stable Nuclei





Do we see the emergence of collective motions from first principle calculations?

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⁴⁸Ca - an interesting case

While neutron-rich, for all practical purposes it can be considered a stable nucleus

- + (p,p') scattering to extract the electric dipole polarizability at RCNP, Japan
 - $lpha_D\,$ is related to the symmetry energy in the EOS of nuclear matter

Parity violation electron scattering Calcium Radius Experiment (CREX) at JLab to measure R_{skin}

$$A_{pv} = \frac{d\sigma/d\Omega_R - d\sigma/d\Omega_L}{d\sigma/d\Omega_R + d\sigma/d\Omega_L} \approx -\frac{G_F q^2}{4\pi\alpha\sqrt{2}} \frac{Q_W F_W(q^2)}{ZF_{ch}(q^2)}$$

The weak force probes the neutron distribution

 $Q_W^n \approx -1$ $Q_W^p = 1 - 4\sin^2\theta_W \approx 0$





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Can we give a first principle predictions for these future experiments?

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- These observables on medium and heavy nuclei have been the subject of intense theoretical studies within density functional theory, shell model, etc...
- Not much has been done with ab-initio methods and we want to fill this gap!



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• Not much has been done with ab-initio methods and we want to fill this gap!

Electromagnetic Reactions on Light Nuclei S. Bacca and S. Pastore J. Phys. G: Nucl. Part. Phys. **41** 123002 (2014).



Ab-initio Approach



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Ab-initio Approach





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Quark/gluon (high energy) dynamics

$$\mathcal{L} = -\frac{1}{4}G^a_{\mu\nu}G^{\mu\nu}_a + \bar{q}_L i\gamma_\mu D^\mu q_L + \bar{q}_R i\gamma_\mu D^\mu q_R - \bar{q}\mathcal{M}q$$

In the limit of vanishing quark masses the QCD Lagrangian is invariant under chiral symmetry

QCD chiral symmetry



Chiral symmetry is explicit and spontaneous broken





Quark/gluon (high energy) dynamics

$$\mathcal{L} = -rac{1}{4}G^a_{\mu
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Nucleon/pion (low energy) dynamics

$$\mathcal{L}_{eff} = \mathcal{L}_{\pi\pi} + \mathcal{L}_{\pi N} + \mathcal{L}_{NN} + \dots$$

Compatible with explicit and spontaneous chiral symmetry breaking

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$$\mathcal{L} = \sum_{\nu} c_{\nu} \left(\frac{Q}{\Lambda_b} \right)^{\nu}$$

Details of short distance physics not resolved, but captured in low energy constants (LEC)



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Systematic expansion
$$\mathcal{L} = 2$$

$$=\sum_{\nu}c_{\nu}\left(\frac{Q}{\Lambda_{b}}\right)^{\nu}$$

Details of short distance physics not resolved, but captured in low energy constants (LEC)

LEC fit to experiment - NN sector -





Traditional Paradigm: (i) Fit NN on scattering data first

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LEC fit to experiment - NN sector -





Traditional Paradigm: (i) Fit NN on scattering data first (ii) add 3N forces fitting on ³H/³He

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Lorentz Integral Transform Method

Efros, et al., JPG.: Nucl.Part.Phys. **34** (2007) R459

Reduce the continuum problem to a bound-state problem

$$R(\omega) = \oint_{f} \left| \left\langle \psi_{f} \left| J^{\mu} \right| \psi_{0} \right\rangle \right|^{2} \delta(E_{f} - E_{0} - \omega)$$

$$L(\sigma, \Gamma) = \int d\omega \frac{R(\omega)}{(\omega - \sigma)^{2} + \Gamma^{2}} = \left\langle \tilde{\psi} \right| \tilde{\psi} \right\rangle < \infty$$
where $\left| \tilde{\psi} \right\rangle$ is obtained solving

$$(H - E_0 - \sigma + i\Gamma) |\tilde{\Psi}\rangle = J^{\mu} |\Psi_0\rangle$$

- Due to imaginary part $\Gamma_{\widetilde{\iota}}$ the solution $| ilde{\psi}
 angle$ is unique
- Since $\langle ilde{\psi} | ilde{\psi}
 angle$ is finite, $| ilde{\psi}
 angle$ has bound state asymptotic behaviour



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The exact final state interaction (FSI) is included in the continuum rigorously!

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 $L(\sigma,\Gamma) \xrightarrow{\text{inversion}} R(\omega)$

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Solved for A=3,4,6,7 with hyper-spherical harmonics expansions and for A=4 with NCSM

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Extension to medium-mass nuclei

Challenge: develop new ab-initio methods that can extend the frontiers to heavier nuclei



• Optimal for closed shell nuclei (±1,±2) $|\psi_0(\vec{r_1},\vec{r_2},...,\vec{r_A})\rangle = e^T |\phi_0(\vec{r_1},\vec{r_2},...,\vec{r_A})\rangle$

 $T = \sum T_{(A)}$ cluster expansion

Very successful in nuclear theory

ORNL group and collaborators: PRL **108**, 242501 (2012), PRL **109**, 032502 (2012); PRL **110**, 192502 (2013), PRL **113**, 262504 (2014), PRL **113**, 142502 (2014) ...

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LIT-CCSD

Merging the Lorentz integral transform method with coupled-cluster theory : New many-body method to extend *ab-initio* calculations of em reactions to medium-mass-nuclei

S.B. et al., PRL 111, 122502 (2013)

 $(\bar{H} - z^*) |\tilde{\Psi}_R(z^*)\rangle = \bar{\Theta} |\Phi_0\rangle$

$$\bar{H} = e^{-T} H e^{T}$$
$$\bar{\Theta} = e^{-T} \Theta e^{T}$$

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$$\bar{H} = e^{-T} H e^{T}$$
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Validation for ⁴He with exact hyperspherical harmonics

NN forces derived from chiral EFT (N³LO)

The comparison is very good Small difference due to missing triples and quadruples



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Extension to heavier nuclei

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S.B. et al., PRL 111, 122502 (2013)



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Extension to heavier nuclei

NN forces derived from chiral EFT (N³LO)

S.B. et al., PRL 111, 122502 (2013) $5 | ^{16}$ O △ Ahrens *et al*. $\sigma_{\gamma}(\omega)/4\pi^{2}$ αω [mb/MeV] Ishkanov et al. Δ LIT-CCSD 3 2 0₀ 20 60 80 100 40 ω[MeV]

The position of the GDR is described from first principles for the first time

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Extension to heavier nuclei

NN forces derived from chiral EFT (N³LO)



The position of the GDR is described from first principles for the first time

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Pigmy Dipole Resonances

Extension to neutron-rich nuclei

NN forces derived from chiral EFT (N³LO)



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Pigmy Dipole Resonances

Extension to neutron-rich nuclei

NN forces derived from chiral EFT (N³LO)



With Mirko Miorelli, PhD student

Soft dipole mode emerges from first principle calculations

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NN interactions





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NN interactions





We observe correlations between polarizability and radii (R_{ch}, R_p, R_n)



NN interactions





We observe correlations between polarizability and radii (R_{ch}, R_p, R_n) Two-body Hamiltonian underestimates both radii and electric dipole polarizabilities

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Including three-nucleon forces

We need accurate interactions able to reproduce both energies and radii



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Including three-nucleon forces

We need accurate interactions able to reproduce both energies and radii



Include radii in the fit of LEC for the three-body force

New Paradigm: NNLO_{sat}: Fit of all LEC at N²LO on NN data and nuclear radii Phys. Rev. C 91, 051301(R) (2015)

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with 3N forces ★ NNLO_{sat}



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with 3N forces \star NNLO_{sat}



Much better agreement with experimental data

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Results for ⁴⁸Ca

Hagen et al., (2015)



- Soft NN(N³LO)+3N(N²LO) Hebeler *et al.*
- Density Functional Theory



Results for ⁴⁸Ca

Hagen et al., (2015)



Density Functional Theory

Exploiting correlations among observables and the very precise measurement of Rp, we predict:

 $0.12 \le R_{
m skin} \le 0.15~{
m fm}$ $\,$ $\,$ Will be measured at JLab by CREX with parity-violation electron scattering

 $2.19 \le \alpha_D \le 2.60 {
m fm}^3$ • Being measured at RCNP (Osaka) wit (p,p')

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Conclusions and Outlook

- Electromagnetic observables are key to test our understanding of nuclear forces
- Extending first principles calculations to medium mass nuclei is possible and very exciting: more applications/impact on experiments in the future
- Monopole strengths, M1 and GT teller transitions

Thanks to my collaborators:

- N. Barnea, B. Carlsson, C. Drischler, A. Ekström, C. Forssén, G. Hagen, K. Hebeler,
- M. Hjorth-Jensen, G. R. Jansen, W. Leidemann, M.Miorelli, W. Nazarewicz, G. Orlandini,
- T. Papenbrock, J. Simonis, A. Schwenk, K. Went



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Thank you!



Backup

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Inversion Procedure

The inversion is performed numerically with a regularization procedure

Ansatz
$$R(\omega) = \sum_{i}^{I_{\max}} c_i \chi_i(\omega, \alpha)$$
 $\square L(\sigma, \Gamma) = \sum_{i}^{I_{\max}} c_i \mathcal{L}[\chi_i(\omega, \alpha)]$

Least square fit of the coefficients c_i to reconstruct the response function



Message: using bound-states techniques to calculate the LIT is correct and inversions are stable



LIT with Coupled Cluster Theory

New theoretical method aimed at extending ab-initio calculations towards medium-mass

S.B. et al., PRL 111, 122502 (2013)

$$\begin{split} (H - z^*) |\tilde{\Psi}\rangle &= J^{\mu} |\psi_0\rangle \\ \text{with } z = E_0 + \sigma + i\Gamma \\ \bar{H} = e^{-T} H e^T \\ \bar{\Theta} = e^{-T} \Theta e^T \\ L(\sigma, \Gamma) &= \left\langle \tilde{\Psi} | \tilde{\Psi} \right\rangle \\ & \bullet \\ L(\sigma, \Gamma) = \left\langle \tilde{\Psi}_L | \tilde{\Psi}_R \right\rangle = \\ & -\frac{1}{2\pi} \Im \left\{ \langle \bar{0}_L | \bar{\Theta}^{\dagger} \left[| \tilde{\Psi}_R(z^*) \rangle - | \tilde{\Psi}_R(z) \rangle \right] \\ \text{with } | \tilde{\Psi}_R(z^*) \rangle &= \hat{R}(z^*) |\Phi_0\rangle \end{split}$$

Formulation based on the solution of an Equation of Motion with source No approximations done so far!

Present implementation in the CCSD scheme

$$T = T_1 + T_2$$

$$\hat{R} = \hat{R}_0 + \hat{R}_1 + \hat{R}_2$$

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LIT with Coupled Cluster Theory

Extension to ¹⁶O with NN forces derived from chiral EFT (N³LO)



Convergence in the model space expansion







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Validation for ⁴He: comparison with exact hyperspherical harmonics

NN forces derived from chiral EFT (N³LO)



The comparison with exact theory is very good Small difference due to missing triples and quadruples

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Medium-mass nuclei with NN(N³LO)

M. Miorelli *et al.,* in preparation (2015)



The present Hamiltonian underestimates both radii and electric dipole polarizabilities

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Giant Dipole Resonance in A=6

with Hyperspherical Harmonics



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